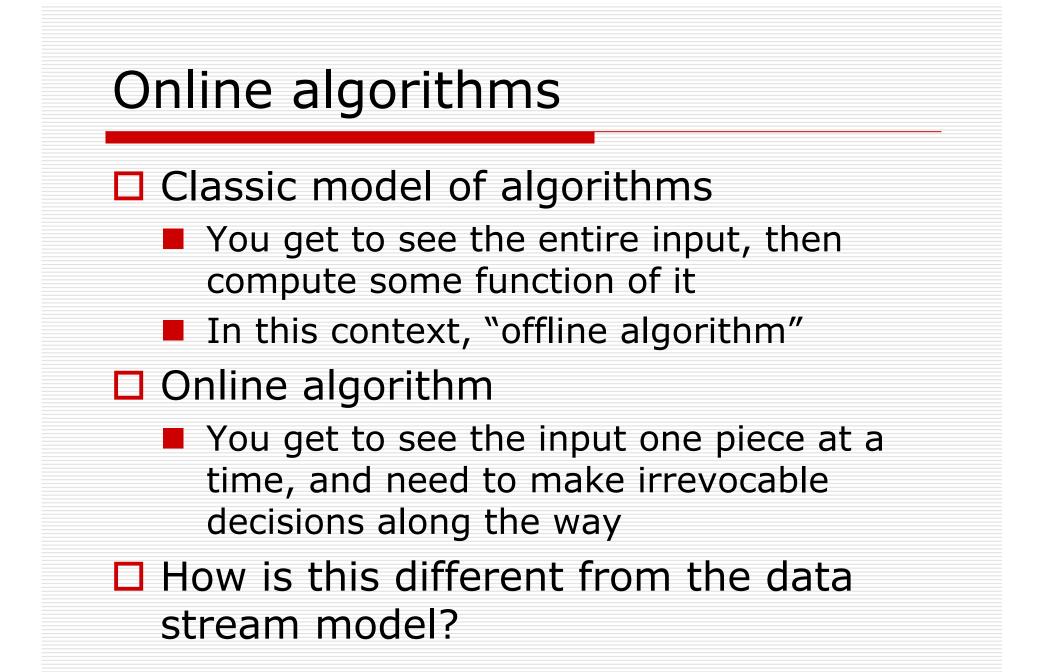
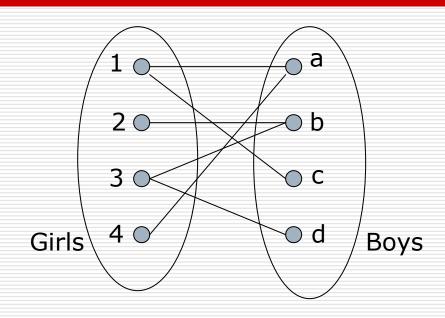
CS 345 Data Mining

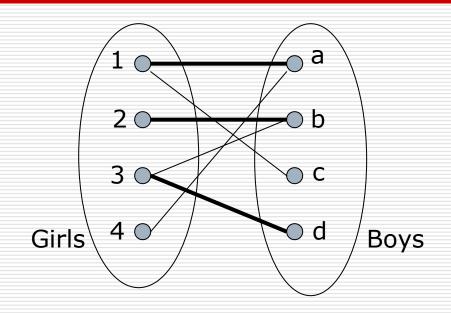
Online algorithms Search advertising



Example: Bipartite matching

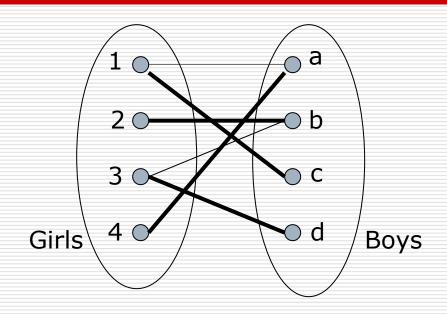


Example: Bipartite matching

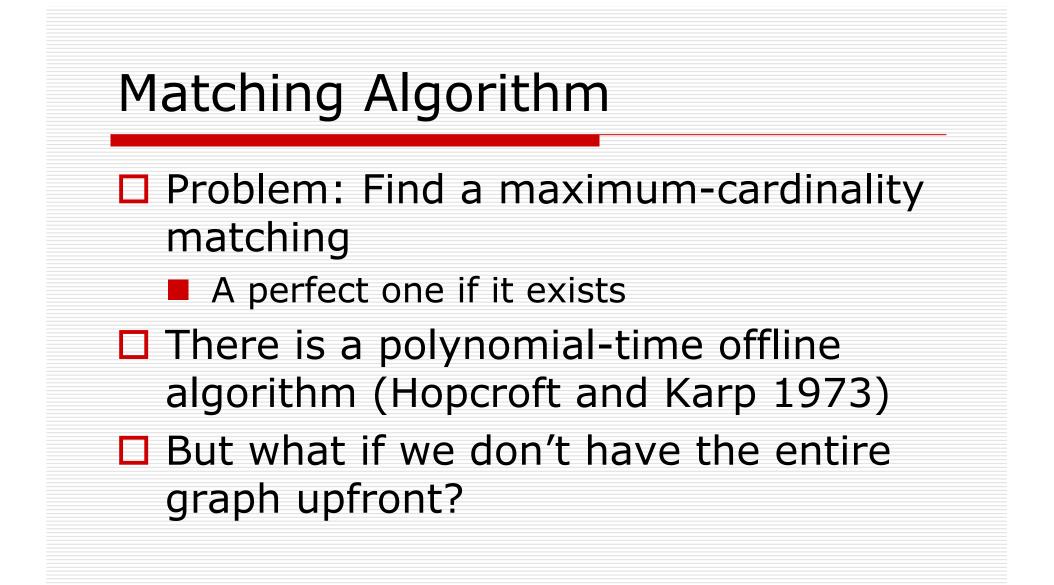


 $M = \{(1,a),(2,b),(3,d)\}$ is a matching Cardinality of matching = |M| = 3

Example: Bipartite matching



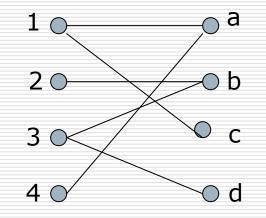
M = {(1,c),(2,b),(3,d),(4,a)} is a **perfect matching**



Online problem

- □ Initially, we are given the set Boys
- In each round, one girl's choices are revealed
- At that time, we have to decide to either:
 - Pair the girl with a boy
 - Don't pair the girl with any boy
- Example of application: assigning tasks to servers

Online problem



(1,a) (2,b) (3,d)

Greedy algorithm Pair the new girl with any eligible boy If there is none, don't pair girl How good is the algorithm?

Competitive Ratio

For input I, suppose greedy produces matching M_{greedy} while an optimal matching is M_{opt}

Competitive ratio =

min_{all possible inputs I} (|M_{greedy}|/|M_{opt}|)

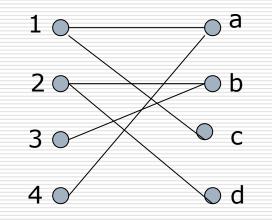
Analyzing the greedy algorithm

- Consider the set G of girls matched in M_{opt} but not in M_{greedy}
- Then it must be the case that every boy adjacent to girls in G is already matched in M_{greedy}
- There must be at least |G| such boys
 - Otherwise the optimal algorithm could not have matched all the G girls

□ Therefore

$$|M_{greedy}|, |G| = |M_{opt} - M_{greedy}|$$
$$|M_{greedy}|/|M_{opt}|, 1/2$$

Worst-case scenario



(1,a) (2,b)



Banner ads (1995-2001)

- Initial form of web advertising
- Popular websites charged X\$ for every 1000 "impressions" of ad
 - Called "CPM" rate
 - □ Modeled similar to TV, magazine ads
- Untargeted to demographically tageted
- Low clickthrough rates
 - Iow ROI for advertisers

Performance-based advertising □ Introduced by Overture around 2000 Advertisers "bid" on search keywords When someone searches for that keyword, the highest bidder's ad is shown Advertiser is charged only if the ad is clicked on Similar model adopted by Google with some changes around 2002 Called "Adwords"

Ads vs. search results

Web

GEICO Car Insurance. Get an auto insurance quote and save today ...

GEICO auto insurance, online car insurance quote, motorcycle insurance quote, online insurance sales and service from a leading insurance company. www.geico.com/ - 21k - Sep 22, 2005 - Cached - Similar pages

Auto Insurance - Buy Auto Insurance Contact Us - Make a Payment More results from www.geico.com »

Geico, Google Settle Trademark Dispute

The case was resolved out of court, so advertisers are still left without legal guidance on use of trademarks within ads or as keywords. www.clickz.com/news/article.php/3547356 - 44k - Cached - Similar pages

Google and GEICO settle AdWords dispute | The Register

Google and car insurance firm **GEICO** have settled a trade mark dispute over ... Car insurance firm **GEICO** sued both Google and Yahool subsidiary Overture in ... www.theregister.co.uk/2005/09/09/google_geico_settlement/ - 21k - Cached - Similar pages

GEICO v. Google

... involving a lawsuit filed by Government Employees Insurance Company (GEICO). GEICO has filed suit against two major Internet search engine operators, ... www.consumeraffairs.com/news04/geico_google.html - 19k - <u>Cached</u> - <u>Similar pages</u>

Results 1 - 10 of about 2,230,000 for geico. (0.04 secc

Sponsored Links

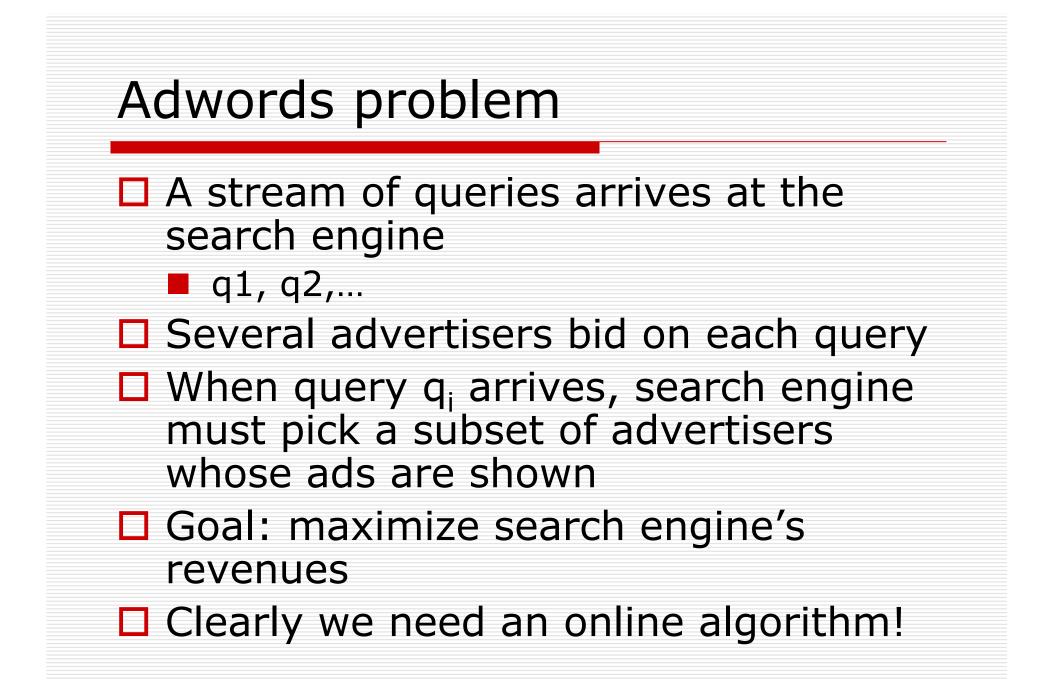
<u>Great Car Insurance Rates</u> Simplify Buying Insurance at Safeco See Your Rate with an Instant Quote www.Safeco.com

Free Insurance Quotes Fill out one simple form to get multiple quotes from local agents. www.HometownQuotes.com

5 Free Quotes. 1 Form. Get 5 Free Quotes In Minutes! You Have Nothing To Lose. It's Free sayyessoftware.com/Insurance Missouri

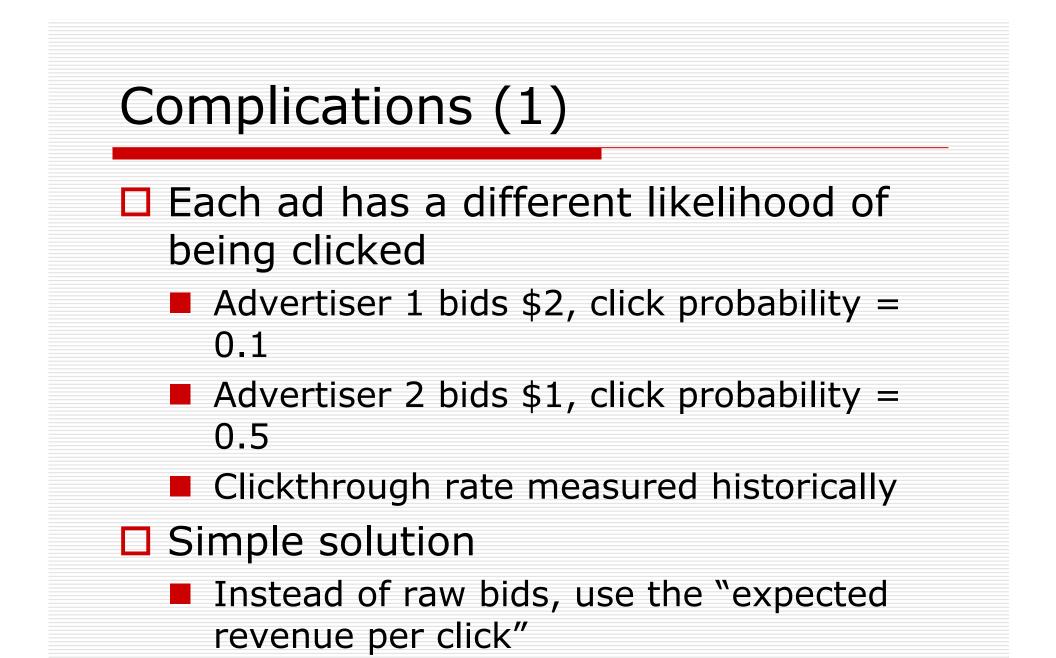
Web 2.0

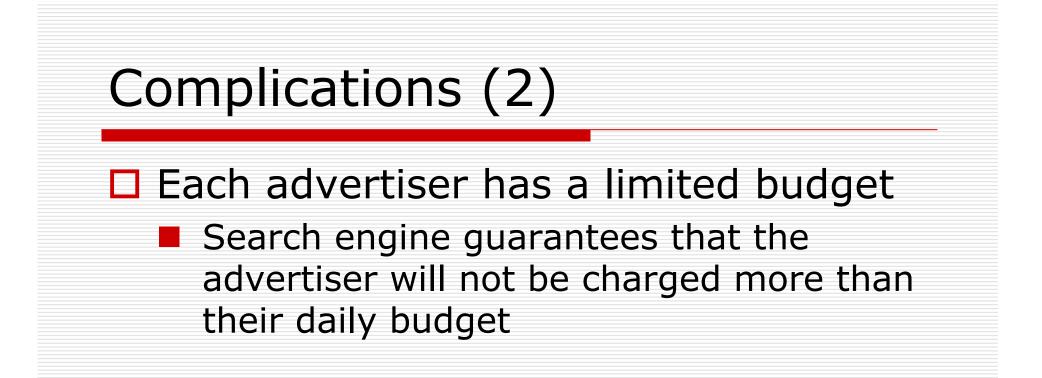
- Search advertising is the revenue model
 - Multi-billion-dollar industry
 - Advertisers pay for clicks on their ads
- Interesting problems
 - What ads to show for a search?
 - If I'm an advertiser, which search terms should I bid on and how much to bid?



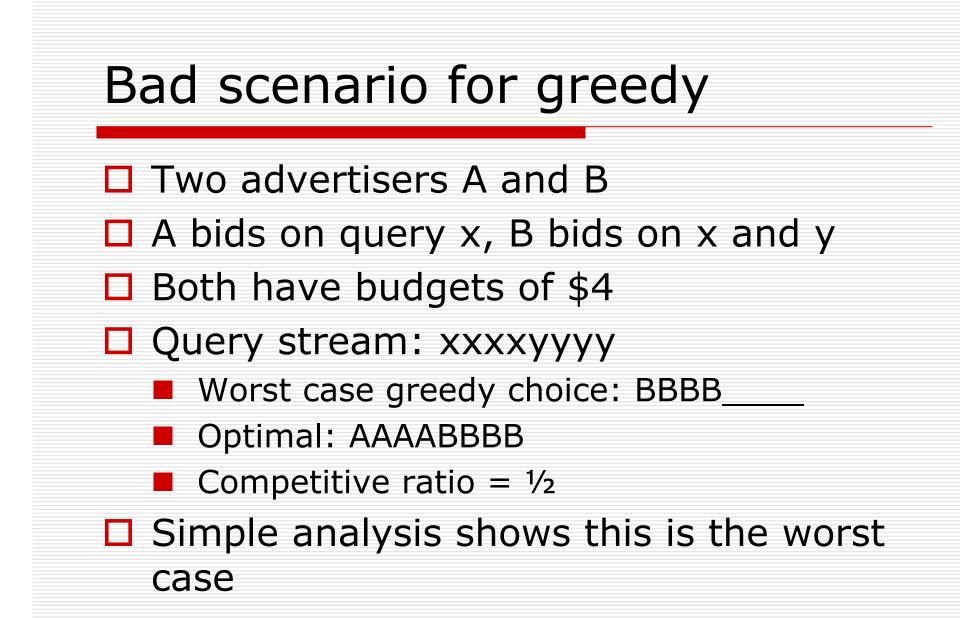
Greedy algorithm

- □ Simplest algorithm is greedy
- It's easy to see that the greedy algorithm is actually optimal!



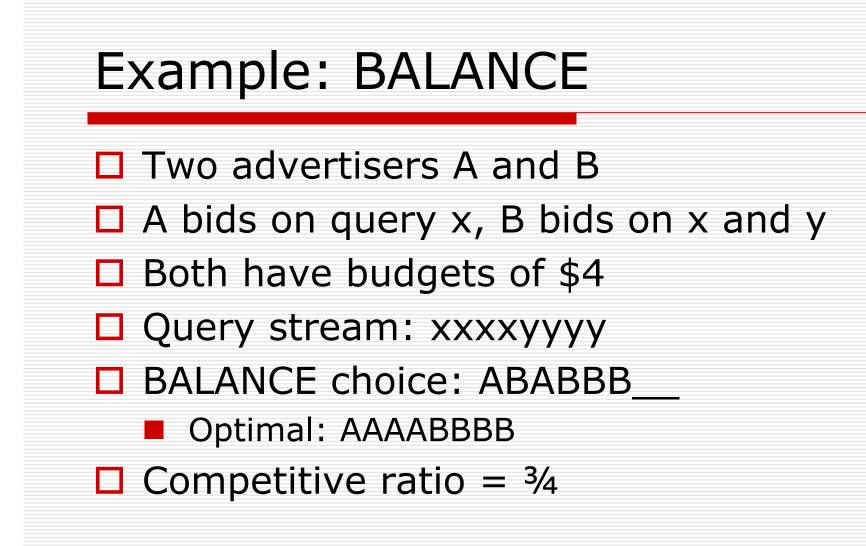


Simplified model Assume all bids are 0 or 1 Each advertiser has the same budget B Let's try the greedy algorithm Arbitrarily pick an eligible advertiser for each keyword



BALANCE algorithm [MSVV]

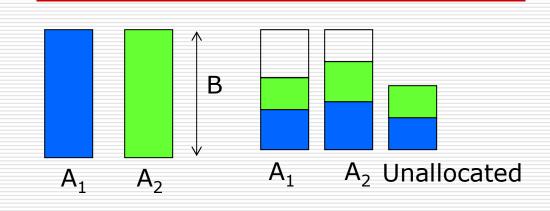
- [Mehta, Saberi, Vazirani, and Vazirani]
- For each query, pick the advertiser with the largest unspent budget
 - Break ties arbitrarily

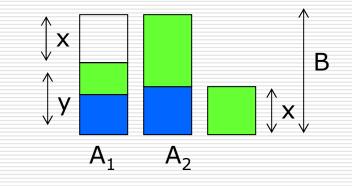


Analyzing BALANCE

- Consider simple case: two advertisers, A₁ and A₂, each with budget B (assume B À 1)
- Assume optimal solution exhausts both advertisers' budgets

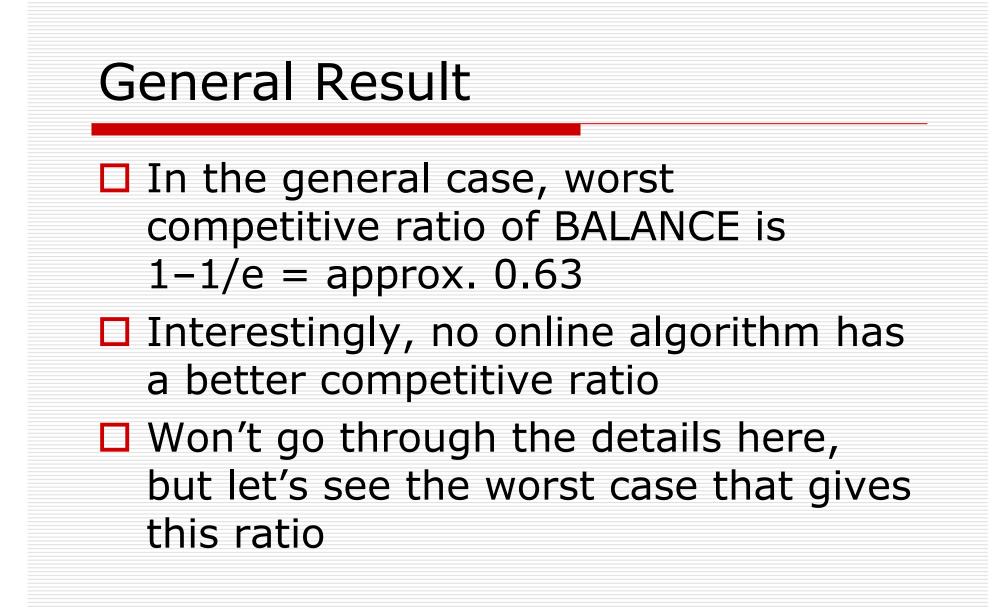
Analyzing Balance





Opt revenue = 2BBalance revenue = 2B-x = B+y

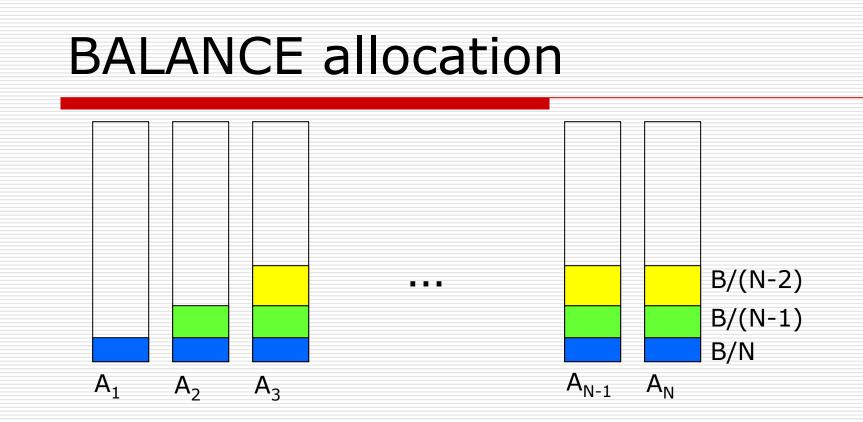
We have y , x Balance revenue is minimum for x=y=B/2Minimum Balance revenue = 3B/2Competitive Ratio = 3/4



Worst case for BALANCE

- N advertisers, each with budget B À N À 1
- NB queries appear in N rounds of B queries each
- **\Box** Round 1 queries: bidders $A_1, A_2, ..., A_N$
- **\Box** Round 2 queries: bidders A_2 , A_3 , ..., A_N
- \square Round i queries: bidders A_i, ..., A_N
- Optimum allocation: allocate round i queries to A_i

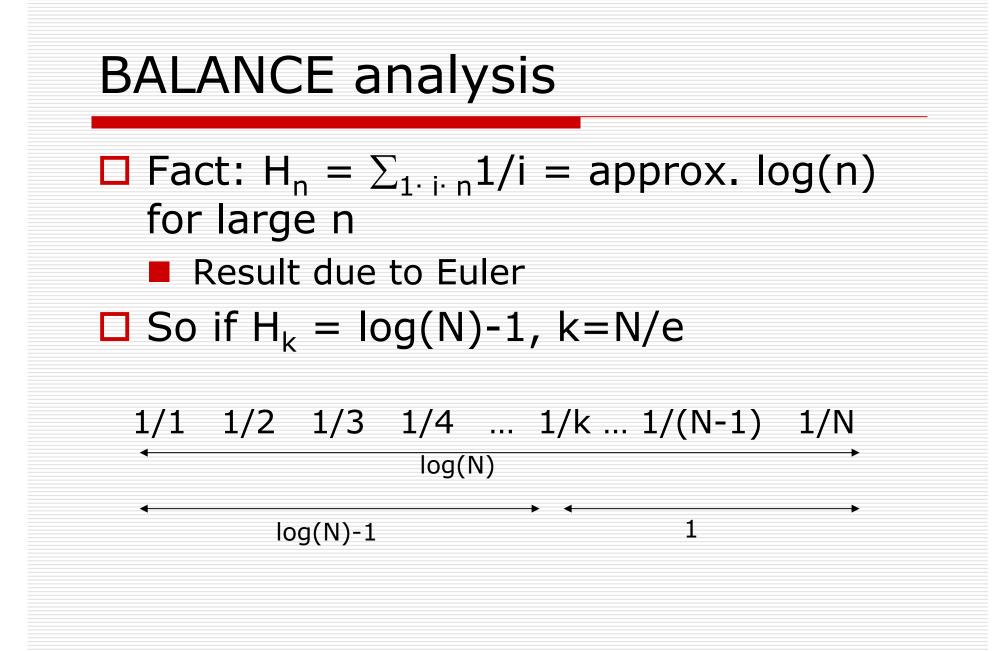
Optimum revenue NB

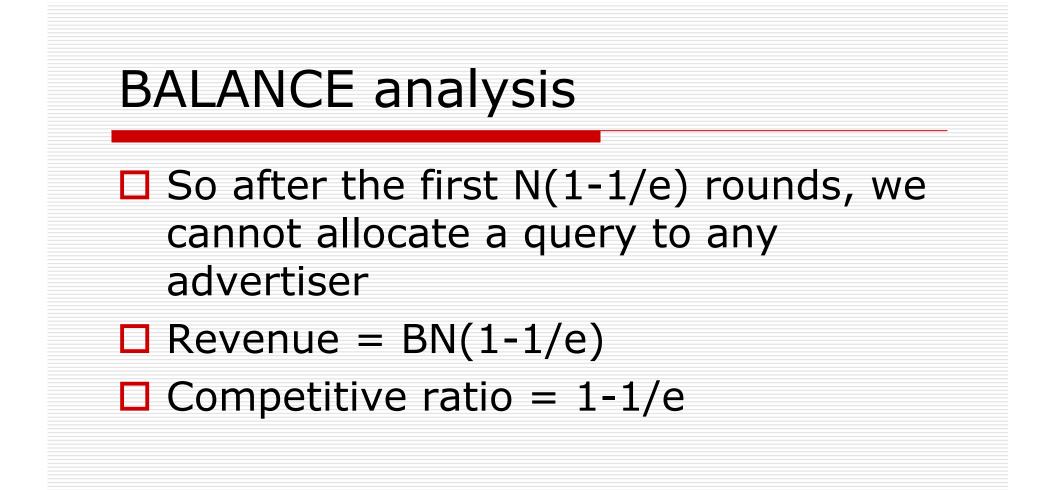


The sum of the allocations to a bin k is given by: $S_k = min(B, \sum_{1 \le i \le k} B/(N-i+1))$

BALANCE analysis

B/1 B/2 B/3 B/4 ... B/k ... B/(N-1) B/N A_1 A_2 A_{n-k+1}





General version of problem

- MSVV also provides an algorithm for the general case with arbitrary bids
 - Same competitive ratio

