# Generating Relations from XML Documents 

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## The Problem

## A Typical Web Page

| Buy our Classic Children's books. |  | One Fish Two Fishy Dr. Seuss Our Discount: $10 \%$ Costs Only: $\$ 7.95$ |
| :---: | :---: | :---: |
| Now at a special discount! | GOODNIGHT MOON | Goodnight Moon by Margaret Brown Costs Only: $\$ 10.55$ |



Brown Bear by Bill Martin Jr.
Our Discount: 15\%
Costs Only: $\$ 6.00$

## An Inside Look

<bookinfo>
\begin{tabular}{|c} 
<book><title>One Fish Two Fish</title> \\
<aname>Dr. Seuss</aname> \\
<discount>10 </discount> \\
<price> 7.95 </price></book> \\
\hline <book><title>Goodnight Moon</title> \\
<aname>Margaret Brown</aname> \\
<price>10.55 </price></book> ....
\end{tabular}
</bookinfo>

## A Query

- Find titles and discounts of books by Dr. Seuss that cost less than $\$ 10$.

How??

## Attempt 1: Search Engine

| SEARCH |
| :--- |
| Books |
| Dr. Suess $<\$ 10$ |

## This won't work!

- No "<" operator defined
- Can't specify that Dr. Seuss is the author and $\$ 10$ is the price
- Can't specify that the price belongs to the book
- Can't specify desired output (i.e., titles, discounts)


## Attempt 2: XQuery

FOR \$b IN document("bixml")//book
WHERE \$price<10 AND \$bname='Dr. Seuss'

## RETURN

<result>
<title> \$b/title </title>
<discount> \$b/discount </discount>
</result>

## This will work, but:

- Difficult for naive users
- Requires knowledge of document structure
- Dependent on document structure


## Attempt 3: Select-Project

Here is what we would like:

## SELECT title, discount FROM "b b.xml" <br> WHERE aname = 'Dr. Seuss' and price < 10

This is possible if the relation
Book(title, aname, price, discount)
can be generated from the document

## Our Goal Extract Relations from XML

- Simple language to define relation generators
- Relation generators should work correctly even if the structure of the document changes
- Missing information should be handled graceful $y$, i.e., create relations with null values


## Syntax of Relation Generators

## The Elements of the Syntax

- Essential ly, a relation generator is a list of tags, e.g., Book(title, aname, price, discount)
- More general $y$, we can use XPath expressions, instead of tags
- Any fragment of XPath can be used, provided that there is a PTime test for checking whether a given node satisfies a given path expression
- We may also want to specify that some of the tags should not get nul lvalues


## The Formal Syntax

- Relation generators are built up from XPath expressions, denoted by $p_{1}, p_{1}, p_{2}$, etc.
- A relation generator is a pair $\Delta=(P, k)$, where
- $P$ is an $m$-tuple of XPath expressions
- $k \leq m$
- $k$ means that the first $k$ tags should not get null values


## The Semantics (Intuitively)

- The result of applying a relation generator ( $\left.\left(p_{1}, \ldots, p_{m}\right), k\right)$ to a document is a set of $m$ tuples ( $n_{1}, \ldots, n_{m}$ ) of nodes and null values, such that
- $n_{i}$ satisfies $p_{i}$ if $n_{i}$ is not the nul lvalue, $i \leq m$
- $n_{i}$ is not the null value, for $i \leq k$
- the nodes in ( $n_{1}, \ldots, n_{m}$ ) are meaningfully related


## Semantics: The Intuition

## An Example Document, as a <br> Tree



Document with information about two books

## Applying a Relation Generator with Human Intervention



## Result:

- Just Lost, \$5.75
- Brown Bear, \$13.95


## A Different Document



Similar document, but the hierarchical structure is different from that of the previous document

## Applying a Relation Generator with Human Intervention (2)



We find the tuples, even with this hierarchy

## Answering a Query without Human Intervention



We need to find pairs of related title and price nodes. How??

## Formal Semantics

## Finding Related Nodes

- The relationship tree of $n_{1}$ and $n_{2}$ is the subtree $T$ of the document $D$, such that
- $T$ is rooted at the lowest common ancestor (Ica) of $n_{1}$ and $n_{2}$, and
- $T$ consists of the two paths from the Ica to $n_{1}$ and $n_{2}$
- We say that $n_{1}$ and $n_{2}$ are interconnected if the relationship tree of $n_{1}$ and $n_{2}$ either
- does not contain two nodes with the same label, or
- the only two distinct nodes with the same label are $n_{1}$ and $n_{2}$


Intuition: The nodes belong to different book entities


Intuition: The nodes belong to the same book entity


Intuition: Although the two nodes represent different author names, they are meaningfully related by virtue of belonging to the same book entity

## Interconnection Graphs

- The interconnection graph of a document $T$, denoted $I G(T)$, consists of
- the same nodes as in $T$, and
- an edge between each pair of interconnected nodes
- We use $\operatorname{IG}(T, N)$ to denote the induced subgraph of $I G(T)$ on the set of nodes $N$


## Graph Properties

- We wil lbe interested in 3 different types of graphs:

Complete Graphs
Connected Graphs


Star Graphs


## Matchings

- $p_{1, \ldots}, p_{m}$ are path expressions
- $S$ is the set of nodes in the document tree
- A function

$$
\mu:\left\{p_{1}, \ldots p_{m}\right\} \rightarrow S \cup\{n u l l\}
$$

is a matching if for all $i$,

- $\mu\left(p_{i}\right)$ satisfies $p_{i}$ or
- $\mu\left(p_{i}\right)=$ null


## Types of Matchings

- Let $\mu$ be a matching
- Let $N$ be the the set of nodes in the image of $\mu$
- $\mu$ is a complete matching if $I G(T, N)$ is a complete graph
- $\mu$ is a reachable matching if $I G(T, N)$ is a connected graph
- $\mu$ is a star matching if $I G(T, N)$ is a star graph


## Maximal Matchings

- A matching $\mu$ subsumes $\mu^{`}$ if $\mu$ and $\mu^{`}$ are equal on all non-null images of $\mu^{\prime}$, i.e., for all $p$, either
- $\mu(p)=\mu^{`}(p)$ or
$-\mu(p)=n u l l$
- A matching is maximal if it is maximal with respect to subsumption


## Evaluating Relation Generators

- The result of applying ( $\left.\left.p_{1}, \ldots, p_{m}\right), k\right)$ to $T$ under complete semantics is the set of images of all maximal complete matchings
- We define similarly the result under reachable semantics and under star semantics


## Example Evaluation (1)



The result remains the same under either the reachable semantics or the star semantics

## Example Evaluation (2)



An additional matching is derived under the reachable semantics and the star semantics

## Complexity of Evaluation

## Complexity Measure

- The time complexity of evaluating a relation generator is measured in terms of the size of the input and the output
- Subsumed matchings should be removed as soon as possible or not be created at all


## Star Semantics

- Theorem: For the star semantics, the result of applying a relation generator ( $\left.\left(p_{1}, \ldots, p_{m}\right), k\right)$ to a tree $T$ can be computed in polynomial time in the size of the input and the output


## Complete Semantics and Reachable Semantics: The General Case

- Theorem: For either the complete semantics or the reachable semantics, it is NP-Complete to check non-emptiness of the result of applying a relation generator $\left(\left(p_{1}, \ldots, p_{m}\right), k\right)$ to a tree $T$


## Complete and Reachable Semantics: All Path Expressions May Have Nulls

- Theorem: For either the complete semantics or the reachable semantics, the result of applying a relation generator $\left(\left(p_{1}, \ldots, p_{m}\right), 0\right)$ to a tree $T$ can be computed in polynomial time in the size of the input and the output


## Complete Semantics: Another Special Case

- Theorem: For the complete semantics, the result of applying $\left(\left(p_{1}, \ldots, p_{m}\right), k\right)$ to $T$ can be computed in polynomial time in the size of the input and the output, provided that
- no path from the root of $T$ to a leaf has repeated tags,
- $p_{1}, \ldots, p_{m}$ are acyclic, and
- for all $p_{i}$ and $p_{j}(i \neq j)$, there is no pair of nodes $n_{1}$ and $n_{2}$ with the same tag, such that $n_{1}$ and $n_{2}$ satisfy $p_{i}$ and $p_{j}$, respectively


## Acyclic Path Expressions

- For a given path expression $p$ and a tree $T$, the relation scheme $R_{p, T}$ consists of al ltags of nodes $n$, such that $n$ either matches $p$ or has a descendent that matches $p$
- $p_{1}, \ldots, p_{m}$ are acyclic if the hypergraph of $R_{p 1, T, \ldots,} \boldsymbol{R}_{p m, T}$ is $\alpha$-acyclic

