

THE SOLUTION OF **LARGE SYSTEMS** OF ALGEBRAIC EQUATIONS

BY

**JOHN M. PAVKOVICH**

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The solution of a system of linear algebraic equations using a computer is not a difficult problem as long as the equations are not ill-conditioned and all of the coefficients can be stored in the computer. However, when the number of coefficients is so large that supplemental means of storage, such as magnetic tape, are required, the problem of solving the system in an efficient manner increases considerably. This paper describes a method of solution whereby such systems of equations can be solved in an efficient manner. The problems associated with ill-conditioned systems of equations are not discussed.

The method described on the following pages was implemented on the IBM 7090 at Stanford for equations with complex coefficients. Although all figures quoted related to tape movement and arithmetic speed are for this computer, the ideas behind the method are applicable to any computer which has the ability to read tape, write tape, and compute simultaneously.

Consider the system of equations

$$\begin{aligned} a_{11}x_1 + a_{12}x_2 + \dots + a_{1N}x_N &= y_1 \\ a_{21}x_1 + a_{22}x_2 + \dots + a_{2N}x_N &= y_2 \\ &\vdots \\ a_{N1}x_1 + a_{N2}x_2 + \dots + a_{NN}x_N &= y_n \end{aligned} \tag{1}$$

The first step in the solution is to normalize the system, i.e., to multiply each equation by a factor which makes the magnitude of the largest coefficient in that equation approximately equal to 1. In the case of a binary machine, this factor should be a power of two so that no significant

figures are lost during this process. The reason for normalizing the system of equations is to increase the effectiveness of pivoting (interchanging equations during the solution process) and thus minimize the difficulties associated with roundoff error.

The method used to solve the system of equations is basically Gauss's method with partial pivoting. Briefly, this method is performed as follows. The first column of the system of equations is scanned to find the largest coefficient of  $x_1$  in absolute value. The equation containing this coefficient is then interchanged with the first equation (or row). A suitable multiple of this new first equation is then subtracted from each of the other equations in order to eliminate  $x_1$  from each of them. This process is then repeated using the coefficients of  $x_2$  and Eqs. 2 through N. Coefficients  $a_{22}$  through  $a_{N2}$  are examined to determine the largest in absolute value. The equation containing this coefficient is interchanged with the second equation and a suitable multiple is subtracted from each of the remaining equations. This same process of eliminating one variable at a time from all succeeding equations is repeated again and again until a system of equations is obtained in which the  $i$ -th equation contains only the unknowns  $x_i$  through  $x_N$ . Such a system of equations is

$$\begin{aligned}
 a_{11}x_1 + a_{12}x_2 + a_{13}x_3 + \dots + a_{1N}x_N &= y_1 \\
 a_{22}x_2 + a_{23}x_3 + \dots + a_{2N}x_N &= y_2 \\
 &\vdots \\
 a_{N-1,N-1}x_{N-1} + a_{N-1,N}x_N &= y_{N-1} \\
 a_{NN}x_N &= y_N
 \end{aligned}
 \tag{2}$$

This so-called reduced system can now be solved by starting at the bottom and solving first for  $x_N$ , then  $x_{N-1}$  using Eq. (N-1) and the now known value of  $x_N$ . This process, known as backsolving, is continued until the entire solution is obtained.

Gauss's method as described above is inefficient when applied to a system of equations too large to fit in core storage. The reason is that

as each variable is eliminated from all subsequent equations, all the coefficients of these equations must be read from tape and the new coefficients written on tape. Moreover, while each coefficient is in core storage, it is used in only one arithmetic operation. What is needed is a method whereby numbers which must be read from tape and written on tape many times, are used in many arithmetic operations while they are in core storage. This can be accomplished by applying Gauss's method in a more subtle fashion in which successive columns of the reduced system are obtained rather than successive rows. This is achieved as follows.

Consider again the system of equations (1). Assume that it has been normalized. As with the ordinary form of Gauss's method, the first column of coefficients is examined to locate the first pivotal element, i.e., the numerically largest coefficient of  $x_1$ . The location of this element is recorded and this coefficient is interchanged with  $a_{11}$ . It is necessary to remember this interchange since this same interchange must be performed in all subsequent columns to accomplish the interchange of the first equation with the equation containing the largest coefficient of  $x_1$ . After the interchange has been performed,  $a_{11}$  is the first column of the reduced system of equations, and will not be involved in any more numerical operations until the backsolving is performed. The remaining elements in column 1, i.e.,  $a_{21}$  through  $a_{N1}$ , are now divided by  $a_{11}$ . The result of this operation will be denoted by  $b_{i1}$  and these numbers will be referred to as multipliers since in terms of Gauss's method,  $b_{i1}$  represents the factor by which the first equation is multiplied when it is used to eliminate  $x_1$  from the  $i$ -th equation.

Thus, we have

$$b_{i1} := \frac{a_{i1}}{a_{11}} \quad (i := 2, 3, \dots, N) \quad . \quad (3)$$

The  $b_{i1}$ 's will be used in processing all of the remaining columns.

The reduction of the second column begins by performing the interchange associated with column 1. The coefficients  $a_{22}$  through  $a_{N2}$  are then processed using the relation

$$a_{i2}^{\text{NEW}} := a_{i2}^{\text{OLD}} - b_{i1} a_{12} \quad (i := 2, \dots, N) \quad . \quad (4)$$





It should be clear from the preceding discussion that the numbers which are used again and again in performing the reduction are the multipliers. Thus these numbers must be repeatedly read from tape if there is insufficient room for all of them in core storage. However, a little thought will show that it is permissible to process more than one column at a time with the same column of multipliers. This means that while a column of multipliers is in core storage, we should process enough columns with it to allow the next column of multipliers to be read from tape. With a judicious choice of the number of columns one chooses to reduce simultaneously, it is possible to overlap almost all tape movement with computing and still keep the amount of core storage required to a minimum.

For the IBM 7090, the number of columns,  $K$ , to be processed simultaneously can be arrived at as follows: The time required to perform arithmetic operations and to read or write tape are as follows:

Floating Multiplication	24 $\mu$ s (microseconds)
Floating Addition or Subtraction	14 $\mu$ s
Read and Write Tape (729-IV Tape Drive 556 Characters/Inch)	100 $\mu$ s/word
Pass a Record Gap	7300 $\mu$ s

From (5) it can be seen that it is necessary to perform one multiplication and one subtraction per multiplier element per column being processed. Here we are assuming the coefficients to be real. If each column of multipliers is written as one record, then the following relation is the criterion we wish to satisfy:

$$\text{Compute Time} \geq \text{Tape Read Time} \quad (7a)$$

$$K(M + 1) (24\mu\text{s} + 14\mu\text{s}) \geq M \cdot 100\mu\text{s} + 7300\mu\text{s} \quad , \quad (7b)$$

where  $K$  = numbers of columns being reduced simultaneously, and  $M$  = length of multiplier column being read. By solving for  $K$ , we find

$$K \geq 2.63 (M/M+1) + 192/(M+1) \quad . \quad (8)$$

From the above relation, we see that  $K$  should certainly be 3 or larger.

A choice of 6 or 8 would probably be the most reasonable since the record gaps would introduce some lost time only when the length of multipliers became less than 30 or 40. In the case of complex coefficients the calculation is quite similar. For the program written at Stanford, 4 columns were used.

If the ideas put forth thus far are implemented in a program, it would proceed as follows. Three tapes are required which will be denoted as below:

IT = Input Tape. This tape contains the matrix describing the system of equations to be solved. It is assumed that the system of equations has been normalized and that the matrix is stored by columns on this tape.

MT = Multiplier Tape. This tape will contain all of the multipliers at the conclusion of the reduction process.

RST = Reduced System Tape. This tape will contain the columns of the reduced system at the conclusion of the reduction process.

It will be seen that the program as described below possesses one major difficulty, namely, that there may be some delay while the MT tape rewinds. A method of overcoming this difficulty will be described subsequently.

The program proceeds as follows:

- 1: Read the first K columns of the system of equations from IT into core storage.
- 2: Reduce these K columns until the first K columns of the reduced system and the first K columns of multipliers are obtained.
- 3: Write the K columns of multipliers on MT and rewind it.
- 4: Write the K columns of the reduced system on RST.
- 5: Read the next K columns of the system of equations from IT into core storage.
- 6: Reduce these K columns using the multipliers stored on MT. During this process, all of the multipliers which have been previously written on MT will be read.
- 7: Further reduce these K columns to obtain K more columns of the reduced system and K more columns of multipliers.

- 8: Write the K new columns of multipliers on MT and rewind it.
- 9: Write the K new columns of the reduced system on RST.
- 10: If more columns remain on IT, go to step 5.

To solve the system of equations for some particular right-hand side, one reduces this right-hand side by processing it with all of the multipliers on MT. The reduced system is then backsolved with this reduced RHS to obtain the solution. During the backsolution process it is necessary to backspace RST before reading each column since they are required in the reverse order from that on the tape. If one has to backsolve the system many times for many different right-hand sides, it is wise to write a tape of the reduced system matrix with the columns in the order in which they are required during backsolving. This can be done the first time the system is backsolved.

As stated previously, the program described above wastes considerable time waiting for the MT to rewind. However, this difficulty can be overcome by using extra multiplier tapes in such a fashion that a tape is always available with the correct column of multipliers ready to be read into core storage. One possible way of doing this using a total of three multiplier tapes will be described here. These three tapes are denoted MT, MT1, MT2. To be effective, this scheme requires two channels.

Tapes MT and MT1 are on Channel A and MT2 is on Channel B. Table I describes how the tapes are used. Here K, the number of columns reduced at one time, is 4. By studying Table I, it will be seen that MT contains approximately one-half of the multiplier columns. The remaining columns of multipliers are on either MT1 or MT2. Consider line 10 in Table I. At this point columns 1-12 have been reduced. Multiplier columns 1-8 are on MT and multiplier columns 9-12 are on MT1. Columns 13-16 are now read from the input tape and processed using multiplier columns 1-8. When this is complete, the rewinding of MT is initiated. Columns 13-16 are then further processed using multiplier columns 9-12. While each of these multiplier columns is in core storage, it is copied onto MT2. Since MT1 and MT2 are on different channels it is possible to read multipliers from MT1, write multipliers on MT2, and compute, all simultaneously. After multiplier columns 9-12 have been used, columns 13-16 are further processed to obtain columns 13-16 of the reduced system and

multiplier columns 13-16. The columns of the reduced system are written on RST and multiplier columns 13-16 are written on MT2. The MT1 and MT2 are now rewound. At this point, the configuration of the tapes is that shown on line 13 of Table I.

The program is now ready to begin processing columns 17-20. These 4 columns are read from IT and processed using multiplier columns 1-8 from MT. Multipliers from MT2 are now used to process the 4 columns in core. While each multiplier column 9, 10, 11, and 12 is in core, it is copied onto MT. Since MT and MT2 are on different channels, there is no delay in the program. As soon as multiplier 12 has been written on MT, it is rewound. While multiplier columns 13-16 are in core, they are written on MT1. Columns 17-20 are then further processed to obtain 4 more columns of the reduced system and 4 more columns of multipliers. The 4 columns of the reduced system are written on RST and the 4 columns of multipliers are written on MT1. Tapes MT1 and MT2 are then rewound and the tapes are in the configurations indicated on line 16 of Table I. The reader should now be able to make his way through Table I.

When all the columns on IT have been processed, it is necessary to copy the multipliers from MT1 or MT2 onto MT if one wants one tape with all of the multiplier columns on it. This will delay the program slightly, but the delay is of little significance when compared to the time required for the entire reduction process.

The program written at Stanford performs the reduction as described above. It also has the capability to compute residues using double precision and iterate the solution to obtain more accurate results. Timing experiments were performed using this program and some representative results are indicated in Table II. A millisecond core clock on the IBM 7090 was used to measure the elapsed time so the measurements are quite accurate. It must be confessed, however, that the results are not exactly reproducible. The reasons for this are related to tape. The start and stop times of various tapes are probably not reproducible from one experiment to another. Also, any tape error further introduces differences since the program is delayed while the tape error is corrected.

TABLE I

	Columns Being Processed	Channel A MT	Channel A MT1		Channel B MT2	
			Reading	Writing	Reading	Writing
1	1-4	---		---	---	
2						
3		1-4		---	---	
4	5-8	1-4	---			---
5						
6		1-4	---			5-8
7	9-12	1-4		---	5-8	
8						
9		1-8		9-12	5-8	
10	13-16	1-8	9-12			---
11						
12		1-8	9-12			9-16
13	17-20	1-8		---	9-16	
14						
15		1-12		13-20	9-16	
16	21-24	1-12	13-16			---
17						
18		1-12	13-16			13-24
ETC.						

Arrangement of Tape Storage During the Reduction Process

TABLE II

N	Reduction and Solution for 1 RHS (no Iterations)	Solution for 2nd RHS (no Iteration)	Iteration
40	11.9 sec	0.44 sec	0.70 sec
80	52.8 sec	2.47 sec	5.32 sec
120	149.6 sec	4.59 sec	10.93 sec
160	327.8 sec	7.33 sec	18.60 sec
320	2398.2 sec	24.57 sec	---

From the results of the timing experiments, it was possible to construct polynomials which give reasonably good estimates of the running time for solving a system of  $N$  equations. These polynomials are as follows:

- (1) Reduction and solution for 1- RHS with no iterations:

$$T = (0.000068)N^3 + (0.0012)N^2 + (0.125)N + (0.425) \quad (9a)$$

- (2) Solution for a second RHS with no iterations:

$$T = (0.000195)N^2 + (0.0144)N + (0.078) \quad (9b)$$

- (3) Each iteration:

$$T = (0.000629)N^2 + (0.015)N + (0.095) \quad (9c)$$

Using polynomial (9a), one estimates that the time required to solve 1000 simultaneous equations with complex coefficients would be about 19 hours. A program to solve equations with real coefficients would require about 30% of this time. Although the numerical operations would require only one-fourth as much time, there is no decrease in the amount of bookkeeping required.

In principle, the program written at Stanford is capable of solving 1000 or more simultaneous equations. However, the use of the present program to solve a system larger than about two or three hundred is rather risky, since the tape routines are not very sophisticated. In their present form, the tape routines make 10 attempts to correct writing errors and 10 attempts to correct reading errors. If the routines are unsuccessful in correcting the tape error, the program halts and the whole computation must be restarted from the beginning. It would be better if the program were able to salvage as much of the computation as possible after encountering bad tape. This could be accomplished by using an extra tape on which a copy of all multipliers and reduced columns was written, so that if any tape failures occurred, the program could continue after new tapes were mounted. This would increase the running time slightly, but it would be well justified by the increased reliability.

SUBROUTINE GAUSS and its associated subroutines are now described briefly and listed in either FORTRAN or FAP.

## SUBROUTINE GAUSS

(NSYS, ISOLVD, KITER, EPS, ANS1, ANS2, RHS1, RHS2,  
KCOEF, KCOPY, KMULT, KT1, KT2, KT3, ISING)

Subroutine Gauss solves a system of up to 500 simultaneous algebraic equations with complex coefficients. The limit of 500 is determined only by the array size in the subroutine and one could increase the maximum allowable size by simply changing the DIMENSION statement and the IF statement which checks to see that the array size is not exceeded.

The arguments of subroutine Gauss are as follows:

**NSYS** = size of the system to be solved. If NSYS exceeds the array size, a message is printed on-line to save the tape containing the system of equations. The subroutine then rewinds the tape containing the system of equations and then pauses before calling EXIT.

**ISOLVD** = an integer variable used to indicate whether the system has been previously solved and that only a new right side is to be considered. If ISOLVD is equal to 1, the reduction process is not performed and the program assumes that the reduced system of equations and the multiplier matrix are available on tapes KT1 and KMULT respectively. If any iterations are required, the program also assumes that a copy of the matrix is available on tape KCOPY. If ISOLVD is not equal to 1, the entire reduction process is performed.

**KITER** = the maximum number of times the program is permitted to iterate and correct the solution. During the iteration process, the error is measured by the maximum change in any unknown divided by the maximum of the unknowns, i.e.,

$$\text{error} = \frac{\text{maximum } |\Delta X_i|}{\text{maximum } |X_i|} .$$

The iteration process stops as soon as either (1) the error is less than EPS, the accuracy criteria, (2) the error for the last iteration is greater than for the previous iteration, or (3) KITER iterations have been performed.

EPS = accuracy criteria for the iteration process. See KITER .

ANS1, ANS2 = one-dimensional arrays which represent the real and imaginary parts of the answer respectively.

RHS1, RHS2 = one-dimensional arrays which represent the real and imaginary part of the right-hand side respectively.

The following 6 arguments of SUBROUTINE GAUSS are logical tape numbers and the purpose of each is described below. In order to perform the reduction efficiently, the program requires that tape KT1 be on a channel different from the channel to which KMULT, KT2, and KT3 are attached. The program also requires that KCOEF and KCOPY be on different channels. If these restrictions are not met, the program prints out a message (off-line) and returns with ISING equal to 4.

KCOEF = the logical tape which contains the matrix describing the system of equations to be solved. The program assumes that the matrix has been previously normalized and that the matrix is stored on this tape by columns. Each column is written as one logical record by a statement of the form

```
WRITE TAPE NCOEF, (A1(K),A2(K),K=1,NSYS,1)
```

where A1 and A2 are the real and imaginary parts respectively of one column of matrix elements.

KCOPY = a logical tape on which SUBROUTINE GAUSS writes a copy of the matrix contained on tape KCOEF. During the iteration process, the entire matrix must be used in computing the residues. In order to overlap the tape reading with computing, it is necessary to have a copy of the matrix written by the I/O routines used by SUBROUTINE GAUSS.



**KMULT =** a logical tape used during the reduction process. At the conclusion of the reduction process, this tape will contain the multiplier matrix. This **lower** triangular matrix will have been written by the I/O routines used by GAUSS and thus this tape cannot be read by **FORTRAN** tape statements.

**KT1 =** a logical tape used during the reduction process. At the conclusion of the reduction process and the initial backsolving, this tape will contain the reduced system matrix. Again, this tape has been written by the I/O routines associated with SUBROUTINE GAUSS.

**KT2, KT3 =** logical tapes used by SUBROUTINE GAUSS. These tapes are used as scratch tapes during the reduction process.

**ISING =** an integer variable used to indicate the result achieved by SUBROUTINE GAUSS. **ISING** will normally be equal to 0. **However, if** during the reduction process a pivotal element is encountered which is less than  $1.0 \times 10^{-15}$  or greater than  $1.0 \times 10^{+15}$ , **ISING is set equal** to 1 or 2 respectively and control is returned to the calling program. Also, as indicated previously, **ISING** is set equal to **4** if the channel requirements for the tapes are not met.

Several subroutines are used by SUBROUTINE GAUSS in solving the system of equations. The function, name, and argument list of each is as follows:

### **SUBROUTINE SAVEIT**

This subroutine has no arguments and is called by GAUSS whenever an uncorrectable tape error occurs. The subroutine should be written by the user and could call EXIT or take any other action deemed appropriate.

## **SUBROUTINE RSTART (NRUN)**

Since SUBROUTINE GAUSS may **run** for a considerable length of time, it should possess the **capability** to be interrupted and restarted. This can be achieved by writing a routine called RSTART. If sense switch 6 is down, RSTART is called periodically by GAUSS. On returning to GAUSS, all tapes are repositioned if **NRUN** is equal to zero. If **NRUN** is positive, tapes are not repositioned before resuming the reduction process.

## **SUBROUTINE MDIVID (N, NA, IMAX, A1, A2)**

This subroutine performs the division necessary to compute a new column of multipliers. A1 and A2 are one-dimensional arrays, N elements in length, representing the real and imaginary parts respectively of one column of the matrix. MDIVID first interchanges element NA with element **IMAX**. Elements NA + 1 through N are then divided by element NA.

## **SUBROUTINE REDUCE (N, NA, IMAX, A1, A2, AM1, AM2)**

This subroutine is used to perform the reduction of one column of the matrix **with** the  $NA^{\text{th}}$  column of multipliers. In the argument list above, N represents the order of the system, NA indicates which column of multipliers is being used, and **IMAX** indicates which element is to be interchanged with element NA before processing. A1 and A2 are **one-**dimensional arrays representing the real and imaginary parts of the matrix column respectively, and **AM1** and **AM2** are one-dimensional arrays representing the real and imaginary parts respectively of the column of multipliers.

## **SUBROUTINE DETER (D1, D2, DET1, DET2, NB2)**

As the system of equations is reduced, the determinant is computed by multiplying together the diagonal elements of the reduced system. This subroutine is used in performing this operation. **DET1** and **DET2** are the real and imaginary parts of the accumulated product and **D1** and **D2** are the real and imaginary parts of the next factor to be used. Because such an extended product may exceed the range of floating point numbers the computer can handle, this subroutine carries the power of 2 separately as **ND2** in order to prevent any overflow or underflow.

## **SUBROUTINE BSOLVE (K, RHS1, RHS2, COL1, COL2, ANS1, ANS2)**

This subroutine is used during the backsolving operation. As with the reduction procedure, the backsolving is carried out by columns. **K** is an integer which indicates the particular element of the answer that is being obtained. **RHS1** and **RHS2** are one-dimensional arrays representing the real and imaginary parts respectively of the right-hand side. **COL1** and **COL2** are one-dimensional arrays representing the real and imaginary parts of column **K** of the reduced system. **ANS1** and **ANS2** are one-dimensional arrays representing the real and imaginary parts of the answer.

## **SUBROUTINE DPSET (NSYS, REMS, IMMS, RELS, IMLS)**

## **SUBROUTINE DPRES (RECOL, IMCOL, ANS1, ANS2)**

These two subroutines are the two entry points to the FAP coded subroutine used in the double precision calculation of the residues. As with the reduction and the backsolving, the residue calculation is performed by columns. The first entry point **DPSET** is used to indicate the size of the system, **NSYS**, and the location for the arrays for the most significant and least significant parts of the real and imaginary parts of the residue. The second entry **DPRES** is used during the calculation of the residues. **RECOL** and **IMCOL** are one-dimensional arrays containing the real and imaginary parts of one column of the matrix. **ANS1** and **ANS2** are the real and imaginary parts of the component of the answer associated with the column being processed.

## **CHAN (NT1, NT2, NOK)**

This FAP coded subroutine is used to check that the channel requirements for the tapes are satisfied. **NT1** and **NW** are two logical tape numbers. If these tapes are on different channels, **NOK** is set equal to 1. If they are on the same channel, **NOK** is set equal to zero.

## **BSET (NTAPE)**

### **BSPACE**

These two subroutines are two entry points to the FAP coded subroutine used to backspace logical tape NTAPE one physical record. **BSET** is used to set up the backspace instruction for logical tape NTAPE, Thereafter, each time **BSPACE** is called, tape NTAPE is backspaced one physical record.

## **RSETA (NTAPE, N, NRET, IQUIT)**

### **READA (NREAD, A1, A2)**

### **RCHKA**

These three subroutines are the three entry points to one of the tape reading routines used by GAUSS. A call to **RSETA** initializes the routine to read records from tape NTAPE. **N** is the size of the system being solved. **NRET** is obtained from an ASSIGN statement and is used to construct a transfer **instruction** which is later executed if an uncorrectable tape error is encountered. **IQUIT** is an integer parameter which is used to indicate the nature of the trouble encountered if a return is made using **NRET**. A call to **READA** then initiates the tape reading. One physical record is read which should contain the last **NREAD** elements of each of the one-dimensional arrays **A1** and **A2**, i.e., elements **N-READ + 1** through **N**. A later call to **RCHKA** checks to see that the reading was completed satisfactorily. If an error has occurred, the tape is backspaced and the record is read again. Up to 5 attempts are made to read the tape correctly. If the routine is unsuccessful, **IQUIT** is set equal to 2 to indicate an uncorrectable reading error and a return is made using the **NRET** transfer instruction.

**WSETA (NTAPE, N, NRET, IQUIT)**

**WRITEA (NWRITE, A1, A2)**

**WCHKA**

These three subroutines are the three entry points to one of the tape writing routines used by GAUSS. The arguments above are analogous to those for **RSETA**, **READA**, and **RCHKA** and the execution of the routine is similar except for the following: Before writing a record, the end of tape indicator is interrogated. If it is on, **IQUIT** is set equal to 3 and a return is made using the **NRET** transfer instruction. If a tape redundancy check occurs, the tape is backspaced and blank tape is written before attempting to write the record again. Up to 10 attempts are ~~made~~ to write the record correctly. If the routine is **unsuccessful**, **IQUIT** is set equal to 1 and a return is made using the **NRET** transfer instruction.

**RSETB (NTAPE, N, NRET, IQUIT)**

**READB (NREAD, A1, A2)**

**RCHKB**

**WSETB (NTAPE, N, NRET, IQUIT)**

**WRITEB (NWRITE, A1, A2)**

**WCHKB**

These subroutines are identical to the above routines ending in A-except for the name.

RSETC (NTAPE, NRET, IQUIT)

READC (NREAD, A1, A2)

RCHKC

WSETC (NTAPE, NRET, IQUIT)

WRITEC (NWRITE, A1, A2)

WCHKC

These subroutines are almost identical to the routines ending in A, the difference being that these mu-tines read or write the first **NREAD** or **NWRITE** elements respectively of the arrays A1 and A2.

```

SUBROUTINE GAUSS(NSYS,ISOLVD,KITER,EPS,ANS1,ANS2,RHS1,RHS2,
1      KCOEF,KCOPY,KMULT,KT1,KT2,KT3,ISING)
C      THIS SUBROUTINE SOLVES A SYSTEM OF UP TO 500 SIMULTANEOUS
C      ALGEBRAIC EQUATIONS WITH COMPLEX COEFFICIENTS USING GAUSS
C      REDUCTION. THE MATRIX ELEMENTS ARE STORED ON TAPE KCOEF
C      BY COLUMNS.
      DIMENSION A1(500),A2(500),B1(500),B2(500),
1      C1(500),C2(500),D1(500),D2(500),
2      AM1(500),AM2(500),BM1(500),BM2(500),
3      RHS1(500),RHS2(500),ANS1(500),ANS2(500),IORDER(500)
      N = NSYS
      NCOEF = KCOEF
      NCOPY = KCOPY
      NMULT = KMULT
      NT1 = KT1
      NT2 = KT2
      NT3 = KT3
      IF (500 - N) 4,8,8
4      WRITE OUTPUT TAPE 6,6,N
60      FORMAT(1H0,10X,29HARRAY SIZE EXCEEDED IN GAUSS./
1      1H0,10X,24HARRAY SIZE = 500 N = I4/
2      1H0,10X,21HEXECUTION TERMINATED.)
      PRINT 7, NCOEF
70      FORMAT(1H0,25HPLEASE SAVE LOGICAL TAPE I2,
1      42H. THIS PROGRAM WILL PAUSE WHEN COMPLETED.)
      REWIND NCOEF
      PAUSE
      CALL EXIT
8      NITER = KITER
      NTERR = 0
      REWIND NCOPY
      REWIND NMULT
      REWIND NT1
10     IF (ISOLVD - 1) 50,10,50
          ITER = 0
          DO 20 K = 1,N,1
              C1(K) = RHS1(K)
              C2(K) = RHS2(K)
              ANS1(K) = 0 . 0
              ANS2(K) = 0 . 0
20     EHold1 = 1 . 0
          GO TO 3400
50     ISING = 0
          EPSA = 1.0E-15
          EPSB = 1.0E+15
          NSAVE = NT1
C      CHECK COMPATABILITY OF TAPE ASSIGNMENTS.
          IQUIT = 0
          CALL LCHAN(NT1,NMULT,NOK)
          IF (NOK) 80,80,90
80      WRITE OUTPUT TAPE 6,160, NT1,NMULT
          IQUIT = 1
90      CALL CHAN(NT1,NT2,NOK)
          IF (NOK) 100,100,110
100     WRITE OUTPUT TAPE 6,165, NT1,NT2
          IQUIT = 1
110     CALL CHAN(NT1,NT3,NOK)
          IF (NOK) 120,120,130
120     WRITE OUTPUT TAPE 6,170, NT1,NT3
          IQUIT = 1
130     CALL CHAN(NCOEF,NCOPY,NOK)
          IF (NOK) 140,140,150
140     WRITE OUTPUT TAPE 6,175, NCOEF,NCOPY

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          IQUIT = 1
150      IF (IQUIT) 100,200,155
155      ISING = 4
          WRITE OUTPUT TAPE 6, 180
          RETURN
1600FORMAT (1H0,25X,14HLOGICAL TAPES I2,5H AND I2,57H HAVE BEEN ASSIGNED
1FD TO KT1 AND KMULT RESPECTFULLY. THESE /1H,35X,43H LOGICAL TAPE UNI
2NITS ARE ON THE SAME CHANNEL.)
1650FORMAT (1H0,25X,14HLOGICAL TAPES I2,5H AND I2,55H HAVE BEEN ASSIGNED
1ED TO KT1 AND KT2 RESPECTFULLY.. THESE /1H,35X,43H LOGICAL TAPE UNI
2TS ARE ON THE SAME CHANNEL.)
1700FORMAT (1H0,25X,14HLOGICAL TAPES I2,5H AND I2,55H HAVE BEEN ASSIGNED
1ED TO KT1 AND KT3 RESPECTFULLY. THESE /1H,35X,43H LOGICAL TAPE UNI
2TS ARE ON THE SAME CHANNEL.)
1750FORMAT (1H0,25X,14HLOGICAL TAPES I2,5H AND I2,59H HAVE BEEN ASSIGNED
1ED TO KCOEF AND KCOPY RESPECTFULLY. THESE /1H,25X,43H LOGICAL TAPE
2 UNITS ARE ON THE SAME CHANNEL.)
1800FORMAT (1H0,25X,79H THIS PROGRAM REQUIRES THAT TAPE KT1 BE ON A CHA
1NNEL DIFFERENT FROM THAT USED BY /1H,35X,68H KMULT, Y T2, OR KT3. A
2LSO TAPES KCOEF AND KCOPY MUST BE ON DIFFERENT /1H,35X,9H CHANNELS.
3)
200      REWIND NCOEF
          REWIND NT2
          REWIND NT3
C      THE FOLLOWING STATEMENTS ARE NECESSARY TO MAKE THE
C      COMPILER HAPPY.
          IQUIT = 4
220      ASSIGN 6000 TO NRET
          GO TO NRET, (6000,6200,6400,6600,6800,7000,7200,7400,
1          7600,7800,8000,8200,8400,8600,8800)
725      ASSIGN 6200 TO NRET
          GO TO NRET, (6000,6200,6400,6600,6800,7000,7200,7400,
1          7600,7800,8000,8200,8400,8600,8800)
330      ASSIGN 6400 TO NRET
          GO TO NRET, (6000,6200,6400,6600,6800,7000,7200,7400,
1          7600,7800,8000,8200,8400,8600,8800)
235      ASSIGN 6600 TO NRET
          GO TO NRET, (6000,6200,6400,6600,6800,7000,7200,7400,
1          7600,7800,8000,8200,8400,8600,8800)
240      ASSIGN 6800 TO NRET
          GO TO NRET, (6000,6200,6400,6600,6800,7000,7200,7400,
1          7600,7800,8000,8200,8400,8600,8800)
245      ASSIGN 7000 TO NRET
          GO TO NRET, (6000,6200,6400,6600,6800,7000,7200,7400,
1          7600,7800,8000,8200,8400,8600,8800)
250      ASSIGN 7200 TO NRET
          GO TO NRET, (6000,6200,6400,6600,6800,7000,7200,7400,
1          7600,7800,8000,8200,8400,8600,8800)
255      ASSIGN 7400 TO NRET
          GO TO NRET, (6000,6200,6400,6600,6800,7000,7200,7400,
1          7600,7800,8000,8200,8400,8600,8800)
260      ASSIGN 7600 TO NRET
          GO TO NRET, (6000,6200,6400,6600,6800,7000,7200,7400,
1          7600,7800,8000,8200,8400,8600,8800)
265      ASSIGN 7800 TO NRET
          GO TO NRET, (6000,6200,6400,6600,6800,7000,7200,7400,
1          7600,7800,8000,8200,8400,8600,8800)
270      ASSIGN 3300 TO NRET
          GO TO NRET, (6000,6200,6400,6600,6800,7000,7200,7400,
1          7600,7800,8000,8200,8400,8600,8800)
275      ASSIGN 8200 TO NRET
          GO TO NRET, (6000,6200,6400,6600,6800,7000,7200,7400,
1          7600,7800,8000,8200,8400,8600,8800)

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280          ASSIGN 8400 TO NRET
          GO TO NRET, (6000,6200,6400,6600,6800,7000,7200,7400,
1              7600,7800,8000,8200,8400,8600,8800)
785          ASSIGN 8600 TO NRET
          GO TO NRET, (6000,6200,6400,6600,6800,7000,7200,7400,
1              7600,7800,8000,8200,8400,8600,8800)
290          ASSIGN 8800 TO NRET
          GO TO NRET, (6000,6200,6400,6600,6800,7000,7200,7400,
1              7600,7800,8000,8200,8400,8600,8800)
295          CONTINUE
C          'THE COMPUTATION AND REDUCTION CAN NOW BEGIN.
          NA = 1
          NB = 2
          NC = 3
          ND = 4
          DFT1 = 1.0
          DET2 = 7.0
          NB2 = 0
          DMAX = 0.0
          DMIN = 1.0
          WRITE TAPE NT3, (RHS1(K),RHS2(K),K = 1,N,1)

C          READ IN AND COPY ON TAPE NCOPIES OF FOUR COLUMNS. IF FEWER
C          THAN FOUR COLUMNS REMAIN, READ IN AND COPY THE REMAINING
C          COLUMNS.
400          ASSIGN 6000 TO NRET
          CALL WSETA(NCOPY,N,NRET,IQUIT)
          NWRITE = N
          IF (NA - N) 420,420,10000
420              READ TAPE NCOEF, (A1(K),A2(K),K=1,N,1)
                  NTEST = 1
                  CALL WRITEA(NWRITE,A1,A2)
          IF (NB - N) 440,440,500
440              READ TAPE NCOEF, (B1(K),B2(K),K=1,N,1)
                  CALL WCHKA
                  NTEST = 2
                  CALL WRITEA(NWRITE,B1,B2)
          IF (NC - N) 460,460,500
460              READ TAPE NCOEF, (C1(K),C2(K),K=1,N,1)
                  CALL WCHKA
                  NTEST = 3
                  CALL WRITEA(NWRITE,C1,C2)
          IF (ND - N) 480,480,500
480              READ TAPE NCOEF, (D1(K),D2(K),K=1,N,1)
                  CALL WCHKA
                  NTEST = 4
                  CALL WRITEA(NWRITE,D1,D2)
500          CALL WCHKA
          IF (NA - 1) 10000,2000,600
C          BEGIN REDUCTION OF COLUMNS USING MULTIPLIERS STORED
C          ON TAPE.
600          ASSIGN 6200 TO NRET
          CALL RSETA(NMULT,N,NRET,IQUIT)
          CALL WSETA(NMULT,N,NRET,IQUIT)
          ASSIGN 6400 TO NRET
          CALL RSETB(NT1,N,NRET,IQUIT)
          CALL WSETB(NT2,N,NRET,IQUIT)
          NREAD = N - 1
          M1 = 4*((NA - 4)/8) + 4
          M2 = 4*(NA/8) + 5
          MLAST = NA - 1
          CALL READA(NREAD,AM1,AM2)
          CALL RCHKA

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      NREAD = NREAD - 1
      CALL READA(NREAD,BM1,BM2)
      IMULT = 1
C     REDUCTION USING MULTIPLIERS IN AM1 AND AM2.
700     IMAX = IORDER(IMULT)
      CALL REDUCE(N,IMULT,IMAX,A1,A2,AM1,AM2)
      IF (NB - N) 720,720,800
720     CALL REDUCE(N,IMULT,IMAX,B1,B2,AM1,AM2)
      IF (NC - N) 740,740,800
740     CALL REDUCE(N,IMULT,IMAX,C1,C2,AM1,AM2)
      IF (ND - N) 760,760,800
760     CALL REDUCE(N,IMULT,IMAX,D1,D2,AM1,AM2)
C     INITIATE TAPE READING AND WRITING OF MULTIPLIER AND
C     REDUCTION TAPES
800     IMULT = IMULT + 1
      NWRITE = NREAD
      NREAD = NREAD - 1
      IF (IMULT - M1) 820,840,880
820     CALL RCHKA
      CALL READA(NREAD,AM1,AM2)
      GO TO 1200
840     IF (IMULT - MLAST1) 845,860,10000
845     CALL RCHKA
      CALL READB(NREAD,AM1,AM2)
      GO TO 1200
860     CALL RCHKA
      IF (ND - N) 870,1200,1200
870     REWIND NYULT
      GO TO 1200
880     IF (IMULT - MLAST) 885,980,1040
885     CALL RCHKB
      IF (IMULT - M2) 900,940,970
900     IF (IMULT - MI - 1) 10000,905,920
905     CALL WRITEA(NWRITE,BM1,BM2)
      CALL READB(NREAD,AM1,AM2)
      GO TO 1200
920     CALL WCHKA
      CALL WRITEA(NWRITE,BM1,BM2)
      CALL READB(NREAD,AM1,AM2)
      GO TO 1200
940     IF (M1 + 1 - M2) 945,950,10000
945     CALL WCHKA
950     IF (ND - N) 955,960,960
955     REWIND NMULT
960     CALL WRITEB(NWRITE,BM1,BM2)
      CALL READB(NREAD,AM1,AM2)
      GO TO 1200
970     CALL WCHKB
      CALL WRITEB(NWRITE,BM1,BM2)
      CALL READB(NREAD,AM1,AM2)
      GO TO 1200
980     CALL RCHKB
      REWIND NT1
1000    IF (MLAST - 8) 10000,1000,1020
      CALL WCHKA
      CALL WRITEA(NWRITE,BM1,BM2)
      GO TO 1200
1020    CALL WCHKB
      CALL WRITEB(NWRITE,BM1,BM2)
      GO TO 1200
1040    IF (MLAST - 4) 10000,2000,1050
1050    IF (MLAST - 8) 10000,1060,1100
1060    CALL WCHKA

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1080             IF (ND - N) 1080,2000,2000
                REWIND NMULT
                GO TO 2000
1100             CALL WCHKB
                GO TO 2000
C             REDUCTION USING MULTIPLIERS- IN BM1 AND BM2.
1200             I MAX = IORDER(IMULT)
                CALL REDUCE(N,IMULT,IMAX,A1,A2,BM1,BM2)
                IF (NB - N) 1220,1220,1400
1720             CALL REDUCE(N,IMULT,IMAX,B1,B2,BM1,BM2)
                IF (NC - N) 1240,1240,1400
1240             CALL REDUCE(N,IMULT,IMAX,C1,C2,BM1,BM2)
                IF (ND - N) 1260,1260,1400
1260             CALL REDUCE(N,IMULT,IMAX,D1,D2,BM1,BM2)
C             INITIATE TAPE READING AND WRITING OF MULTIPLIER AND
C             REDUCTION TAPES.
1400             IMULT = IMULT + 1
                NWRITE = NREAD
                NREAD = NREAD - 1
                IF (IMULT - M1) 1420,1440,1480
1420             CALL RCHKA
                CALL READA(NREAD,BM1,BM2)
                GO TO 700
1444             IF (IMULT - MLAST) 1445,1460,10000
1445             CALL RCHKA
                CALL READB(NREAD,BM1,BM2)
                GO TO 700
1460             CALL RCHKA
                IF (ND - NJ) 1470,700,700
1470             REWIND NMULT
                GO TO 700
1480             IF (IMULT - MLAST) 1485,1580,1640
1485             CALL RCHKB
                IF (IMULT - M2) 1500,1540,1570
1500             IF (IMULT - M1 - 1) 10000,1505,1520
1505             CALL WRITEA(NWRITE,AM1,AM2)
                CALL READB(NREAD,BM1,BM2)
                GO TO 700
1520             CALL WCHKA
                CALL WRITEA(NWRITE,AM1,AM2)
                CALL READB(NREAD,BM1,BM2)
                GO TO 700
1540             IF (M1 + 1 - M2) 1545,1550,10000
1545             CALL WCHKA
1550             IF (ND - N) 1555,1560,1560
1555             REWIND NMULT
1560             CALL WRITEB(NWRITE,AM1,AM2)
                CALL READB(NREAD,BM1,BM2)
                GO TO 700
1570             CALL WCHKB
                CALL WRITEB(NWRITE,AM1,AM2)
                CALL READB(NREAD,BM1,BM2)
                GO TO 700
1580             CALL RCHKB
                REWIND NT1
                IF (MLAST - 8) 10000,1600,1620
1600             CALL WCHKA
                CALL WRITEA(NWRITE,AM1,AM2)
                GO TO 700
1620             CALL WCHKB
                CALL WRITEB(NWRITE,AM1,AM2)
                GO TO 700
1640             IF (MLAST - 4) 10000,2000,1650

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1650          I F (MLAST - 8 1 10000,1660,1700
1660          CALL WCHKA
          IF (ND - N) 1680,2000,2000
1680          REWIND NMULT
          GO TO 2000
1700          CALL WCHKB
C REDUCTION OF COLUMNS AFTER PROCESSING WITH MULTIPLIERS.
2000          IF (ND - N) 2010,2005,2005
2005          REWIND NT2
2010          ASSIGN 7000 TO NRET
          CALL WSETC(NT3,NRET,ICUIT)
          P MAX = 0.0
          I MAX = NA
          DO 2040 K = NA,N,1
              COMP = ABSF(A1(K)) + ABSF(A2(K))
              I F (P MAX - COMP) 2020,2040,2040
2020          P MAX = COMP
          I MAX = K
2040          CONTINUE
          IORDER(NA) = I MAX
          NTEST = NA
          I F (EPSA - P MAX) 2060,2060,4000
          I F (P MAX - EPSB) 2070,2070,4000
2060          CALL DETER(A1(I MAX),A2(I MAX),DET1,DET2,NB2)
2070          DMAX = MAX1F(DMAX,P MAX)
          DMIN = MIN1F(DMIN,P MAX)
          NWRITE = NA
          IF (NA - N) 2080,2400,10000
2080          CALL MDIVID(N,NA,I MAX,A1,A2)
          CALL WRITEC(NWRITE,A1,A2)
          CALL REDUCE(N,NA,I MAX,RHS1,RHS2,A1,A2)
          CALL REDUCE(N,NA,I MAX,B1,B2,A1,A2)
          CALL WCHKC
          P MAX = 0.0
          I MAX = NB
          DO 2140 K = NB,N,1
              COMP = ABSF(B1(K)) + ABSF(B2(K))
              I F (P MAX - COMP) 2120,2140,2140
2120          P MAX = COMP
          I MAX = K
2140          CONTINUE
          IORDER(NB) = I MAX
          NTEST = NB
          I F (EPSA - P MAX) 2160,2160,4000
          I F (P MAX - EPSB) 2170,2170,4000
2160          CALL DETER(B1(I MAX),B2(I MAX),DET1,DET2,NB2)
2170          DMAX = MAX1F(DMAX,P MAX)
          DMIN = MIN1F(DMIN,P MAX)
          NWRITE = NB
          IF (NB - N) 2180,2420,10000
2180          CALL MDIVID(N,NB,I MAX,B1,B2)
          CALL WRITEC(NWRITE,B1,B2)
          CALL REDUCE(N,NB,I MAX,RHS1,RHS2,B1,B2)
          CALL REDUCE(N,NA,IORDER(NA),C1,C2,A1,A2)
          CALL REDUCE(N,NB,IORDER(NB),C1,C2,B1,B2)
          CALL WCHKC
          P MAX = 0.0
          I MAX = NC
          DO 2240 K = NC,N,1
              COMP = ABSF(C1(K)) + ABSF(C2(K))
              I F (P MAX - COMP) 2220,2240,2240
2220          P MAX = COMP
          I MAX = K

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2240          CONTINUE
            IORDER(NC) = IMAX
            NTEST = NC
            IF (FPSA - PMAX) 2260,2260,4000
2260          I F (PMAX - FPSB) 2270,2270,4000
2270          CALL DETER(C1(IMAX),C2(IMAX),DET1,DET2,NB2)
            DMAX = MAX1F(DMAX,PMAX)
            DMIN = MIN1F(DMIN,PMAX)
            NWRITE = NC
            IF (NC - N) 2280,2440,10000
2280          CALL MDIVID(N,NC,IMAX,C1,C2)
            CALL WRITFC(NWRITE,C1,C2)
            CALL REDUCE(N,NC,IMAX,RHS1,RHS2,C1,C2)
            CALL REDUCE(N,NA,IORDER(NA),D1,D2,A1,A2)
            CALL REDUCE(N,NB,IORDER(NB),D1,D2,B1,B2)
            CALL REDUCE(N,NC,IORDER(NC),D1,D2,C1,C2)
            CALL WCHKC
            PMAX = 0.0
            IMAX = ND
            DO 2340 K = ND,1,1
                COMP = ABSF(D1(K)) + ABSF(D2(K))
                I F (PMAX - COMP) 2320,2340,2340
2320                PMAX = COMP
                IMAX = K
2340          CONTINUE
            IORDER(ND) = IMAX
            NTEST = ND
            I F (FPSA - PMAX) 2360,2360,4000
2360          I F (PMAX - EPSB) 2370,2370,4000
2370          CALL DETER(D1(IMAX),D2(IMAX),DET1,DET2,NB2)
            DMAX = MAX1F(DMAX,PMAX)
            DMIN = MIN1F(DMIN,PMAX)
            NWRITE = ND
            IF (ND - N) 2380,2460,10000
2380          CALL MDIVID(N,ND,IMAX,D1,D2)
            CALL WRITFC(NWRITE,D1,D2)
            CALL REDUCE(N,ND,IMAX,RHS1,RHS2,D1,D2)
            CALL WCHKC
            GO TO 2500
2400          CALL WRITFC(NWRITE,A1,A2)
            CALL WCHKC
            GO TO 2700
2420          CALL WRITFC(NWRITE,B1,B2)
            CALL WCHKC
            GO TO 2700
2440          CALL WRITFC(NWRITE,C1,C2)
            CALL WCHKC
            GO TO 2700
2460          CALL WRITFC(NWRITE,D1,D2)
            CALL WCHKC
            GO TO 2700
C          WRITE NEW MULTIPLIERS ON TAPE.
2500          IF (NA - 1) 10000,2505,2520
2505          ASSIGN 6600 TO NRET
            CALL WSETA(NMULT,N,NRET,IQUIT)
            GO TO 2540
2520          ASSIGN 6800 TO NRET
            CALL WSETA(NT2,N,NRET,IQUIT)
2540          NWRITE = N - N A
            CALL WRITEA(NWRITE,A1,A2)
            CALL WCHKA
            NWRITE = N - M B
            CALL WRITEA(NWRITE,B1,B2)

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CALL WCHKA
NWRITE = N - NC
CALL WRITEA(NWRITE,C1,C2)
CALL WCHKA
NWRITE = N - ND
CALL WRITEA(NWRITE,D1,D2)
CALL WCHKA
C CALL RSTART IF RESTART IS DESIRED.
2600 IF (SENSE SWITCH 6) 2610,2670
2610 CALL RSTART(NRUN)
2620 IF (NRUN) 10000,2620,2670
REWIND NCOEF
RE JIND NCOPY
REWIND NMULT
ASSIGN 8600 TO NRET
CALL RSETA(NCOPY,N,NRET,IQUIT)
NREAD = N
DO 2640 J = 1,ND,1
CALL READA(NREAD,A1,A2)
READ TAPE NCOEF,(B1(K),B2(K),K=1,N,1)
2640 CALL RCHKA
READ TAPE NT3,(A1(K),A2(K),K = 1,N,1)

ASSIGN 8800 TO NRET
CALL RSFTC(NT3,NRET,IQUIT)
NREAD = 0
DO 2660 J = 1,ND,1
NREAD = NREAD + 1
CALL RFADC(NREAD,A1,A2)
2660 CALL RCHYC
2670 REWIND NT1
REWIND NT2
REWIND NMULT
NTEMP = NT1
NT1 = NT2
NT2 = NTEMP
NA = NA + 4
NB = NA + 1
NC = NB + 1
ND = NC + 1
GO TO 400
C THE REDUCTION IS COMPLETE. PRINT THE VALUE OF THE DETERMINANT
C AND THE MAXIMUM AND MINIMUM PIVOTAL ELEMENTS.
2700 TEMP = 1.0
DO 2720 K = 1,N,1
IF (IORDER(K) - K) 2715,2720,2715
2715 TEMP = -TEMP
2720 CONTINUE
FNB2 = FLOATF(NB2)
KE1 = FNB2/3.3219281
KE2 = KE1
EXPON = MODF(FNB2,3.3219281)
AMPL = TEMP*(2.0**EXPON)
DET1 = AMPL*DET1
DET2 = AMPL*DET2
IF (DET1) 2745,2740,2745
2740 KE1 = 0
GO TO 2755
2745 IF (ABSF(DET1) - 1.01) 2746,2755,2750
2746 DET1 = 10.0*DET1
KE1 = KE1 - 1
GO TO 2745
2750 IF (10.0 - ABSF(DET1)) 2751,2751,2755

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2751          DET1 = DET1/10.0
              KE1 = KE1 + 1
              GOTO 2750
2755          I F (DET2) 2760,2756,2760
2756          KE2 = 0
              GOTO 2770
2760          I F (ABSF (DET2) - 1.0) 2761,2770,2765
2761          DET2 = 10.0*DET2
              KE2 = KE2 - 1
              GO TO 2760
2765          I F (10.0 - ABSF (DET2)) 2766,2770,2770
2766          DET2 = DET2/10.0
              KE2 = KE2 + 1
              CO TO 2765
2770          WRITE OUTPUT TAPE 6, 2775, DET1,KE1,DET2,KE2,DMAX,DMIN
27750FORMAT (1H0,25X,70HTHE GAUSSIAN REDUCTION IS COMPLETED. THE DETER
MINANT OF THE MATRIX IS/1H,45X,18HREAL PART = F9.5,1HE,14/
21H,45X,18HIMAGINARY PART =F9.5,1HE,14/1H0,25X,62HTHE MAGNITUDE
30F THE LARGEST PIVOTAL ELEMENT IS APPROXIMATELY 1PE9.2,1H./1H0,
425X,63HTHE MAGNITUDE OF THE SMALLEST PIVOTAL ELEMENT IS APPROXIMAT
5ELY 1PE9.2,1H.)
C          COPY ALL MULTIPLIERS ON TO THE MULTIPLIER TAPE.
2800          ASSIGN 7200 TO NRET
              CALL WSETA(NMULT,N,NRET,IQUIT)
              IF (N - 121 2860,2860,2820
2820          ASSIGN 7400 TO NRET
              CALL RSETB(NT2,N,NRET,IQUIT)
              IMULT = M2
2840          NWDS = N - IMULT
              CALL READB(NWDS,AM1,AM2)
              CALL RCHKB
              CALL WRITEA(NWDS,AM1,AM2)
              CALL WCHKA
              IMULT = IMULT + 1
              I F (IMULT - NA) 2840,2860,2860
2860          NWRITE = N - NA
              I F (NWRITE) 10000,2940,2880
2880          CALL WRITEA(NWRITE,A1,A2)
              CALL WCHKA
              NWRITE = N - NB
              IF (NWRITE) 10000,2940,2900
2900          CALL WRITEA(NWRITE,B1,B2)
              CALL WCHKA
              NWRITE = N - NC
              I F (NWRITE) 10000,2940,2920
2920          CALL WRITEA(NWRITE,C1,C2)
              CALL WCHKA
2940          REWIND NT1
              REWIND NT2
              REWIND NMULT
              REWIND NCOEF
              REWIND NCOPY
              NT1 = NSAVE
C          BACKSOLVE THE REDUCED SYSTEM OF EQUATIONS. ALSO WRITE THE
C          REDUCED COLUMNS ON TAPE NT1 IN THE REQUIRED ORDER.
3000          CALL BSET(NT3)
              ASSIGN 7600 TO NRET
              CALL RSETC(NT3,NRET,IQUIT)
              ASSIGN 7800 TO NRET
              CALL WSETC(NT1,NRET,IQUIT)
              NREAD = N
              CALL BSPACE
              CALL READC(NREAD,AM1,AM2)

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CALL RCHKC
CALL BSPACE
3040 NWDS = NREAD
      NREAD = NREAD - 1
      CALL WRITEC(NWDS,AM1,AM2)
      IF (NREAD) 10000,3080,3160
3060         CALL BSPACE
           CALL READC(NREAD,BM1,BM2)
3080 CALL BSOLVE(NWDS,RHS1,RHS2,AM1,AM2,ANS1,ANS2)
CALL WCHKC
IF (NREAD) 10000,3180,3100
3100 CALL RCHKC
CALL BSPACE
NWDS = NREAD
NREAD = NREAD - 1
CALL WRITEC(NWDS,BM1,BM2)
IF (NREAD) 10000,3140,3120
3120         CALL BSPACE
           CALL READC(NREAD,AM1,AM2)
3140 CALL BSOLVE(NWDS,RHS1,RHS2,BM1,BM2,ANS1,ANS2)
CALL WCHKC
IF (NREAD) 10000-3180-3160
3160 CALL RCHKC
CALL BSPACE
GO TO 3040
3180 REWIND NT1
REWIND NT3
ITER = 0
EHOLD1 = 1.0
READ TAPE NT3,(C1(K),C2(K),K = 1,N,1)
REWIND NT3
IF (NITER) 3190,3190,3200
3190         RETURN
C COMPUTE RESIDUES USING DOUBLE PRECISION.
3300 ITER = ITER + 1
      ASSIGN 8000 TO NRET
      CALL RESITA(NCOPY,N,NRET,IQUIT)
      CALL DPSET(N,RHS1,RHS2,D1,D2)
      DO 3220 K=1,N,1
           RHS1(K) = C1(K)
           RHS2(K) = C2(K)
           D1(K) = 0.0
3220           D2(K) = 0.0
      NREAD = N
      CALL READA(NREAD,AM1,AM2)
      ICOL = 1
3240 'IF (ICOL - N) 3260,3250,3320
3250     CALL RCHKA
           GO TO 3370
3260     CALL RCHKA
           CALL READA(NREAD,BM1,BM2)
3270     CALL DPRES(AM1,AM2,ANS1(ICOL),ANS2(ICOL))
           ICOL = ICOL + 1
           IF (ICOL - N) 3290,3280,3320
3280         CALL RCHKA
           GO TO 3300
3290     CALL RCHKA
           CALL READA(NREAD,AM1,AM2)
3300     CALL DPRES(BM1,BM2,ANS1(ICOL),ANS2(ICOL))
           ICOL = ICOL + 1
           GO TO 3240
3320     REWIND NCOPY
C REDUCE THE NEWRIGHT HAND SIDE.

```



```

3400      ASSIGN 8200 TO NRET
        CALL RSETA(NMULT,N,NRET,IQUIT)
        NREAD = N - 1
        CALL READA(NREAD,AM1,AM2)
3420      IMULT = N - NREAD
        NREAC = NREAD - 1
        IF (NREAD) 3520,3440,3450
3440          CALL RCHKA
            GO TO 3460
3450      CALL RCHK
        CALL READA(NREAD,BM1,BM2)
3460      CALL REDUCE(N,IMULT,IORDER(IMULT),RHS1,RHS2,AM1,AM2)
        IMULT = N - NREAD
        NREAD = NREAD - 1
        IF (NREAD) 3520,3480,3490
3480          CALL RCHKA
            GO TO 3500
3490      CALL RCHKA
        CALL READA(NREAD,AM1,AM2)
3500      CALL REDUCE(N,IMULT,IORDER(IMULT),RHS1,RHS2,BM1,BM2)
        GO TO 3420
3520      REWIND NMULT
3600      BACK-SOLVE AND CORRECT SOLUTION.
        ASSIGN 8400 TO NRET
        CALL RSETC(NT1,NRET,IQUIT)
        NREPD = N
        CALL READC(NREAD,AM1,AM2)
3620      NWDS = NREAD
        NREAD = NREAD - 1
        IF (NREAD) 3720,3640,3650
3640          CALL RCHKC
            GO TO 3660
3650      CALL RCHKC
        CALL READC(NREAD,BM1,BM2)
3660      CALL BSOLVE(NWDS,RHS1,RHS2,AM1,AM2,A1,A2)
        NWDS = NREAD
        NREAD = NREAD - 1
        IF (NREAD) 3720,3680,3690
3680          CALL RCHKC
            GO TO 3700
3690      CALL RCHKC
        CALL READC(NREAD,AM1,AM2)
3700      CALL BSOLVE(NWDS,RHS1,RHS2,BM1,BM2,A1,A2)
        GO TO 3620
3720      REWIND NT1
        DO 3740 K = 1,N,1
            B1(K) = ANS1(K)
            B2(K) = ANS2(K)
            ANS1(K) = ANS1(K) + A1(K)
            ANS2(K) = ANS2(K) + A2(K)
3740      IF (NITER) 3760,3760,3780
        RETURN
3760      IF (ITER) 3760,3200,3800
3780      RMAX = 0.0
3800      EMAX = 0.0
        DO 3840 K = 1,N,1
            RMAX = MAX1F(RMAX,ABSF(ANS1(K)),ABSF(ANS2(K)))
            EMAX = MAX1F(EMAX,ABSF(ANS1(K) - B1(K)),
                ABSF(ANS2(K) - B2(K)))
3840      RERR = EMAX/RMAX
        IF (RERR - EPS) 3860,3860,3880
3860      WRITE OUTPUT TAPE 6, 3940, ITER,RERR,EPS
        RETURN

```

```

3880      I F (EHOLD1 - RERR) 3890,3890,3900
3890      WRITE OUTPUT TAPE 6, 3945, ITER,RERR,EHOLD1,EPS
          RETURN
3900      I F (NITER - ITER) 3910,3910,3920
3910      WRITE OUTPUT TAPE 6, 3950, ITER,RERR,EPS,EHOLD1
          RETURN
3920      EHOLD1 = RERR
          GO TO 3200
39400FORMAT (1H0,25X,48HTHE ACCURACY DESIRED HAS BEEN ESTABLISHED AFTER
1 I2,26H ITERATIONS. THE RELATIVE/1H,35X,9H ERROR IS 1PE9.2,
234H. THE RELATIVE ERROR DESIRED WAS 1PE9.2,1H.)
39450FORMAT (1H0,25X,44HTHE ITERATIVE PROCEDURE IS NOT CONVERGING. 12,
131H ITERATIONS HAVE BEEN COMPLETED/1H,35X,38H BUT THE RELATIVE ERR
20R INCREASED FROM 1PE9.2,4H TO 1PE9.2,7H DURING/1H,35X,52H THE LAS
3T ITERATION. THE RELATIVE ERROR DESIRED WAS 1PE9.2,1H.)
39500FORMAT (1H0,25X,48HTHE I2,65H ITERATIONS ALLOWED HAVE BEEN COMPLETE
1D BUT THE RELATIVE ERROR IS/1H,35X,6H STILL 1PE9.2,24H WHILE THAT
2DESIRED WAS 1PE9.2,15H. THE RELATIVE/1H,35X,37H ERROR FOR THE PRE
3VIOUS ITERATION WAS 1PE9.2,1H.)
4000      WRITE OUTPUT TAPE 6, 4040, NTEST,PMAX,EPS1,EPSB
          ISING = 1
          I F (EPS3 - PMAX) 4020,4020,4030
4020      ISING = 2
4030      RETURN
40400FORMAT (1H1,25X,68HTHE BOUNDS FOR PIVOTAL ELEMENTS WERE EXCEEDED I
1N DETERMINING PIVOTAL/1H,35X,8H ELEMENT I3,43H. THE MAGNITUDE OF
2THIS PIVOTAL ELEMENT IS/1H,35X,14H APPROXIMATELY 1PE9.2,33H. THIS
3PROGRAM REQUIRES THAT ALL/1H,35X,29H PIVOTAL ELEMENTS LIE BETWEEN
4 1PE9.2,5H AND 1PE9.2,1H.)
C          PROCEDURES FOR CORRECTING TAPE ERRORS. IQUIT ASSUMES THE
C          VALUES 1,2, OR 3 ACCORDING TO THE DIFFICULTY ENCOUNTERED.
C          IQUIT = 1      UNCORRECTABLE WRITING ERROR
C          IQUIT = 2      UNCORRECTABLE READING ERROR
C          IQUIT = 3      SHORT TAPE
C          WRITING ERROR ON TAPE NCOPY DURING COPYING OF INPUT COLUMNS.
6000      NGO = IQUIT
          MTERR = NCOPY
          GO TO (9500,10000,9700,225), NGO
C          READING OR WRITING ERROR ON TAPE NMULT DURING REDUCTION.
6700      NGO = IQUIT
          MTERP = NMULT
          GO TO (9500,9600,9700,230), NGO
C          READING OR WRITING ERROR ON TAPE NT1 OR NT2 DURING REDUCTION.
6400      NGO = IQUIT
          MTERR = NT1
          NTERR = NT2
          GO TO (9500,9600,9700,235), NGO
C          WRITING ERROR ON TAPE NMULT DURING MULTIPLIER WRITING.
6600      NGO = IQUIT
          YTERR = NMULT
          GO TO (9500,10000,9700,240), NGO
C          WRITING ERROR ON TAPE NT2 DURING MULTIPLIER WRITING.
6800      NGO = IQUIT
          MTERR = NT2
          GO TO (9500,10000,9700,245), NGO
C          WRITING ERROR ON TAPE NT3 DURING REDUCEC COLUMN WRITING.
7000      NGO = IQUIT
          MTERR = NT3
          GO TO (9500,10000,9700,250), NGO
C          WRITING ERROR ON TAPE NMULT DURING MULTIPLIER COPYING.
7200      NGO = IQUIT
          MTERR = NMULT
          GO TO (9500,10000,9700,255), NGO

```

```

C      7400      READING ERROR ON TAPE NT2 DURING MULTIPLIER COPYING.
                NGO = IQUIT
                MTERR = NT2
                GO TO (10000,9600,10000,260),NGO
C      7600      READING ERROR ON TAPE NT3 DURING INITIAL BACKSOLVING.
                NGO = IQUIT
                MTERR = NT3
                GO TO (10000,9600,10000,265),NGO
C      7800      WRITING ERROR ON TAPE NT1 DURING INITIAL BACKSOLVING.
                NGO = IQUIT
                MTERR = NT1
                GO TO (9500,10000,9700,270),NGO
C      8000      READING ERROR ON TAPE NCOPY DURING ITERATION.
                NGO = IQUIT
                MTERR = NCOPY
                GO TO (10000,9600,10000,275),NGO
C      8300      READING ERROR ON TAPE NMUL' DURING RHS REDUCTION.
                NGO = IQUIT
                MTERR = NMULT
                GO TO (10000,9600,10000,280),NGO
C      8400      READING ERROR ON TAPE NT1 DURING BACKSOLVING.
                NGO = IQUIT
                MTERR = NT1
                GO TO (10000,9600,10000,285),NGO
C      8600      READING ERROR ON TAPE NCOPY DURING RESTARTING.
                NGO = IQUIT
                MTERR = NCOPY
                GO TO (10000,9600,10000,290),NGO
C      8800      READING ERROR ON TAPE NT3 DURING RESTARTING.
                NGO = IQUIT
                MTERR = NT3
                GO TO (10000,9600,10000,295),NGO
9500      IF (NTERR) 9530,9505,9530
9505      WRITE OUTPUT TAPE 6, 9515, MTERR
          PRINT 5515, MTERR
95150     FORMAT (1H0,40HREPEATED REDUNDANCIES IN WRITING LOGICAL,
1         6H TAPE,I2,1H.)
          GO TO 9660
9530      WRITE OUTPUT TAPE 6, 9545, MTERR,NTERR
          PRINT 9545, MTERR,NTERR
95450     FORMAT (1H0,40HREPEATED REDUNDANCIES IN WRITING LOGICAL,
1         6H TAPF,I2,21HAND/OR LOGICAL TAPF,I2,1H.)
          GO TO 9660
9600      IF (NTERR) 9630,9605,9630
9605      WRITE OUTPUT TAPE 6, 9615, MTERR
          PRINT 9615, MTERR
96150     FORMAT (1H0,40HREPEATED REDUNDANCIES IN READING LOGICAL,
1         6H TAPE,I2,1H.)
          GO TO 9660
9630      WRITE OUTPUT TAPF 6, 9645, MTERR,NTERR
          PRINT 9645, MTERR,NTERR
96450     FORMAT (1H0,40HREPEATED REDUNDANCIES IN READING LOGICAL,
1         6H TAPE,I2,21HAND/OR LOGICAL TAPE,I2,1H.)
          PRINT 9675
9660      PRINT 9675
9675      FORMAT (1H0,28HINSPECT TAPE AND TAPF DRIVE.)
          GO TO 9800
9700      IF (NTERR) 9730,9705,9730
9705      WRITE OUTPUT TAPE 6, 9715, MTERR
          PRINT 9715, MTERR
97150     FORMAT (1H0,40HEND OF TAPF ENCOUNTERED WHILE WRITING ON,
1         14H LOGICAL TAPE,I2,1H.)
          GO TO 9760
9730      WRITE OUTPUT TAPE 6, 9745, MTERR,NTERR

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```

          PRINT 9745, MTERR, NTERR
97450    FORMAT (1H0,40HEND OF TAPE FNCONTAINED WHILE WRITING ON,
           1      14H LOGICAL TAPE ,I2,17H OR LOGICAL TAPE ,I2,1H.)
9760    PRINT 9775
9775    FORMAT (1H0,34HMOUNT A LONGER TAPE ON THIS DRIVE.)
9800    PRINT 9815
9815    FORMAT (1H0,41HPRESSSTART TO RESUME PROCESSING THIS JOB)
        PAUSE
        REWIND NCOEF
        REWIND NMULT
        REWIND NCOPY
        REWIND NT1
        REWIND NT2
        REWIND NT3
        CALL SAVEIT
10000    WRITE OUTPUT TAPE 6, 10020
        REWIND NMULT
        REWIND NCOEF
        REWIND NCOPY
        REWIND NT1
        REWIND NT2
        REWIND NT3
        CALL DUMP
100200   FORMAT(1H1,123HEITHER A MACHINE ERROR HAS OCCURRED OR THERE IS AN
          1 ERROR IN SUBROUTINE GAUSS OR ITS ASSOCIATED SUBROUTINES. DUMP HAS
          2S BEEN /1H,29HCALLED TO TERMINATE THIS JOB.)
          END

```

```

SUBROUTINE SAVEIT
  CALL CHAIN(3,B3)
  END

```

```

SUBROUTINE RSTART(NRUN)
  NRUN = 1
  RETURN
  END

```

```

C
C
SUBROUTINE MDIVID(N,NA,IMAX,A1,A2)
  THIS SUBROUTINE PERFORMS THE DIVISION NECESSARY IN
  COMPUTING A NEW COLUMN OF MULTIPLIERS.
  DIMENSION A1(500),A2(500)
    T1 = A1(IMAX)
    T2 = A2(IMAX)
    A1(IMAX) = A1(NA)
    A2(IMAX) = A2(NA)
    A1(NA) = T1
    A2(NA) = T2
    IF (ABS(T1) - ABS(T2)) 100,120,120
100   TEMP = T1/T2
      R2 = -1.0/(T2*(1.0 + TEMP**2))
      R1 = -TEMP*R2
      GO TO 140
120   TEMP = T2/T1
      R1 = 1.0/(T1*(1.0 + TEMP**2))
      R2 = -TEMP*R1
140   KS = NA + 1
      DO 160 K = KS,N,1
        TEMP = A1(K)
        A1(K) = R1*TEMP - R2*A2(K)
160   A2(K) = R1*A2(K) + R2*TEMP
      RETURN
  END

```

```

C
C
SUBROUTINE REDUCE(N,NA,IMAX,A1,A2,AM1,AM2)
  THIS SUBROUTINE PERFORMS THE REDUCTION OF ONE COLUMN WITH
  ONE COLUMN OF MULTIPLIERS. THE NECESSARY INTERCHANGE IS
  PERFORMED.
  DIMENSION A1(500),A2(500),AM1(500),AM2(500)
    KA = NA
    KMAX = IMAX
    T1 = A1(KMAX)
    T2 = A2(KMAX)
    A1(KMAX) = A1(KA)
    A2(KMAX) = A2(KA)
    A1(KA) = T1
    A2(KA) = T2
    KS = KA + 1
    DO 100 K = KS,N,1
      A1(K) = A1(K) - AM1(K)*T1 + AM2(K)*T2
100   A2(K) = A2(K) - AM1(K)*T2 + AM2(K)*T1
    RETURN
  END

```

```

SUBROUTINE DETER(D1,D2,DET1,DET2,NB2)
C      THIS SUBROUTINE IS USED IN COMPUTING THE DETERMINANT OF
C      THE MATRIX.
      T1 = DET1
      T2 = DET2
      DET1 = T1*D1 - T2*D2
      DET2 = T1*D2 + T2*D1
      COMP = MAX1F(ABSF(DET1),ABSF(DET2))
      NADD = LOGF(COMP)/0.69314718
      AYPL = 2.0**NADD
      DFT1 = DET1/AMPL
      DET2 = DET2/AMPL
      NB2 = NB2 + NADD
      RETURN
END

```

```

SUBROUTINE BSOLVE(K,RHS1,RHS2,COL1,COL2,ANS1,ANS2)
C      THIS SUBROUTINE IS USED TO OBTAIN THE SOLUTION OF THE
C      REDUCED SYSTEM OF EQUATIONS.
      DIMENSION RHS1(500),RHS2(500),COL1(500),COL2(500),
1          ANS1(500),ANS2(500)
      N = K
      T1 = COL1(N)
      T2 = COL2(N)
      I F (ABSF(T1) - ABSF(T2)) 10,20,20
10          TEMP = T1/T2
              R2 = -1.0/(T2*(1.0 + TEMP**2))
              R1 = -TEMP*R2
              GO TO 30
20          TEMP = T2/T1
              R1 = 1.0/(T1*(1.0 + TEMP**2))
              R2 = -TEMP*R1
30          T1 = R1*RHS1(N) - R2*RHS2(N)
              T2 = R1*RHS2(N) + R2*RHS1(N)
              ANS1(N) = T1
              ANS2(N) = T2
              KS = N - 1
              I F (KS) 50,50,60
50          RETURN
60          DO 80 K = 1,KS,1
              RHS1(K) = RHS1(K) - T1*COL1(K) + T2*COL2(K)
              RHS2(K) = RHS2(K) - T1*COL2(K) - T2*COL1(K)
80          RETURN
END

```

```

*      DOUBLE PRECISION SUBROUTINE
      LBL      DPRES
      COUNT   100
      ENTRY   DPSET      (NSYS,REMS,IMMS,RELS,IMLS)
      ENTRY   DPRFS      (RECOL,IMCOL,ANS1,ANS2)
DPSET  CLA*    1,4
      STD     NSYS
      CCA     2,4
      ADD     =1
      STA     REMS1
      STA     REMS2
      STA     REMS3
      STA     REMS4
      CLA     3,4
      ADD     =1
      STA     IMMS1
      STA     IMMS2
      STA     IMMS3
      STA     IMMS4
      CLA     4,4
      ADD     =1
      STA     RELS1
      STA     RELS2
      STA     RELS3
      STA     RELS4
      CLA     5,4
      ADD     =1
      STA     IMLS1
      STA     IMLS2
      STA     IMLS3
      STA     IMLS4
      TRA     6,4
DPRES  SXA     X4,4
      CLA     1,4
      ADD     =1
      STA     RECOL1
      STA     RECOL2
      CLA     2,4
      ADD     =1
      STA     IMCOL1
      STA     IMCOL2
      CLA*    ?,4
      STO     ANS1
      CLA*    4,4
      STO     ANS2
      LXD     =000000100000,4
RFPFAT LDQ     ANS1
RECOL1 FMP     **,4
      STQ     PROD?
      CHS
REMS1  FAD     **,4
      STO     TEMP
      XCA
RELS1  UFA     **,4
      UFS     PROD2
      FAD     TEMP
REMS2  STO     **,4
RELS2  STQ     **,4
      LDQ     ANS2
IMCOL1 FMP     **,4
      STQ     PROD2
REMS3  FAD     **,4
      STO     TEMP

```

	XCA	
RELS3	UFA	** ,4
	IJFA	PROD?
	FAD	TEMP
REMS4	STO	** ,4
RELS4	STO	** ,4
	LDQ	ANS1
IMCOL2	FMP	** ,4
	STQ	PROD?
	CHS	
IMMS1	FAD	** ,4
	STO	TEMP
	XCA	
IMLS1	UFA	** ,4
	UFS	PROD2
	FAD	TEMP
IMMS2	STO	** ,4
IMLS2	STO	** ,4
	LDQ	ANS2
RECOL2	FMP	** ,4
	STQ	PROD2
	CHS	
IMMS3	FAD	** ,4
	STO	TEMP
	XCA	
IMLS3	UFA	** ,4
	UFS	PROD?
	FAD	TEMP
IMMS4	STO	** ,4
IMLS4	STQ	** ,4
	TXI	**+1,4,1
NSYS	TXL	REPEAT,4,**
x4	AXT	,4
	TRA	5,4
ANS1	PZE	
ANS2	PZE	
PROD1	PZE	
PROD2	PZE	
TEMP	PZE	
	END	



```

* CHANNEL COMPATABILITY SUBROUTINE
  LBL      CHAN
  COUNT   20
  ENTRY   CHAN          (NT1,NT2,NOK)
CHAN      SXA      X4,4
          CLA*    1,4
          CALL    (IOS)
          CLA*    $(ETT)
          STO     TEMP
          LXA     X4,4
          CLA*    2,4
          CALL    (IOS)
          CLA*    $(ETT)
          SUB     TEMP
x 4       AXT     ,4
          TZE     OUT
          CLA     =00000C1000000
          STO*    394
          TRA     4,4
OUT       STZ*    3,4
          TRA     4,4
TEMP     PZE
          END

```

```

* TAPE BACKSPACE SUBROUTINE
  LBL      BSPACE
  COUNT   13
  ENTRY   BSET          (NTAPE)
  ENTRY   BSPACE
BSET      SXA      X4,4
          CLA*    1,4
          ADM     =020
          CALL    (IOS)
          CAL*    $(BSR)
          STO     BSPACE
x 4       AXT     ,4
          TRA     2,4
BSPACE   PZE
          TRA     1,4
          END

```

```

*      SUBROUTINE READA
      LBL      READA
      COUNT   63
      ENTRY   QSETA      (NTAPE,N,NRET,IQUIT)
      ENTRY   READA      (NREAD,A1,A2)
      ENTRY   RCHKA
RSETA  SXA     X4,4
      CAL*    1,4
      ACL     =020
      CALL    (IOS)
      LDQ*    $(TRC)
      SLQ     TRC
      LDQ*    $(TCO)
      SLQ     TCO
      LDQ*    $(RCH)
      SLQ     RCH
      CAL*    $(RDS)
      SLW     RDS
      STA     BSR
x 4    AXT     ,4
      CLA*    2,4
      ARS     18
      SUB     =1
      STO     TEMP
      CLA*    3,4
      STA     NRET
      CLA     4,4
      STA     IQUIT
READA  TRA     5,4
      CLA*    194
      STD     RIO
      STD     RIO+1
      CLA     2,4
      SUB     TEMP
      STA     RIO
      CLA     394
      SUR     TEMP
      STA     RIO+1
RDS    PZF
RCH    PZE     RIO
      TRA     4,4
RIO    IOCP    **,**
      IOCD    **,**
RCHKA  STZ     NBAD
TCO    PZE     *
TRC    PZF     ERROR
      TRA     1,4
ERROR  SXA     54,4
      LXD     NREAD,4
      TXI     **+1,4,1
      TXH     QUIT,4,5
      SXD     NBAD,4
BSR    BSR     **
      XEC     RDS
      XEC     RCH
S4     AXT     **,4
      TRA     TCO
QUIT   CLA     =0000002000000
IQUIT  STO     **
      CAL     RDS
      STA     **+1
      REW     **
NRET   TRA     **
NBAD   PZE
TEMP   PZE
      END

```

```

*      SUBROUTINE WRITEA
      LBL      WRITCA
      COUNT   80
      ENTRY   WSETA      (NTAPE,N,NRET,IQUIT)
      ENTRY   WPITFA    (WRITE,A1,A2)
      ENTRY   WCHKA
WSFTA  SXA     X4,4
      CAL*    1,4
      ACL     =020
      CALL    (ICS)
      LDQ*    $(TRC)
      SLQ     TRC
      LDQ*    $(TCO)
      SLQ     TCO
      LDG*    $(RCH)
      SLQ     RCH
      CAL*    $(ETT)
      SLW     ETT
      SLW     ETTOFF
      CAL*    $(WRS)
      SLW     WRS
      STA     BSR
X4     AXT     ,4
      CLA*    2,4
      ARS     18
      SUR     =1
      STO     TEMP
      CLA*    3,4
      STA     NRET1
      STA     NRET2
      CLA     4,4
      STA     IQUIT1
      STA     IQUIT2
ETTOFF PZF
      NOP
      TRA     5,4
WRITEA CLA*    1,4
      STD     WIO
      STD     WIO+1
      CLA     2,4
      SUB     TEMP
      STA     WIO
      CLA     3,4
      SUB     TEMP
      STA     WIO+1
ETT    PZE
      TRA     SHORT
WRS    PZE
RCH    PZF     WIC
      TRA     4,4
WIO    IOCP    **,**
      IOCD    **,**
SHORT  CLA     =0000003000000
IQUIT1 STG     **
      CAL     WRS
      STA     *+1
      REW     **
NRET1  TRA     **
WCHKA  STZ     NBAD
TCO    PZE     *
TRC    PZE     FRROR
      TRA     1,4
ERROR  SXA     S4,4

```

```

LXD      NBAD,4
TXI      **+1,4,1
TXH      QUIT,4,10
SXD      NBAD,4
BSR      BSR      **
          XFC      WRS
          XFC      WRS
          XEC      WRS
          XEC      RCH
5 4      AXT      **,4
          TRA      TCO
QUIT     CLA      =0000001000000
IQUI T2  STO      **
          CAL      WRS
          STA      **+1
          REW      **
NRFT2   TRA      **
NBAD    PZE
TEMP    PZE
          END

```

```

*      SUBROUTINE READB
      LBL      READB
      COUNT    63
      ENTRY    RSETB      (NTAPE,N,NRET,IQUIT)
      ENTRY    READB      (NREAD,A1,A2)
      ENTRY    RCHKB
RSETB  SXA     X4,4
      CAL*    1,4
      ACL     =020
      CALL    (IOS)
      LDQ*    $(TRC)
      SLO     TRC
      LDQ*    $(TCO)
      SLO     TCO
      LDQ*    $(RCH)
      SLO     RCH
      CAL*    $(RDS)
      SLW     RDS
      STA     BSR
x 4    AXT     ,4
      CLA*    2,4
      ARS     18
      SUB     =1
      STO     TEMP
      CLA*    3,4
      STA     NRET
      CLA     4,4
      STA     IQUIT
      TRA     5,4
READB  CLA*    1,4
      STD     RIO
      STD     RIO+1
      CLA     2,4
      SUB     TEMP
      STA     RIO
      CLA     3,4
      SUB     TEMP
      STA     RIO+1
RDS    PZE
RCH    PZF     RIO
      TRA     4,4
RIO    IOCP    **,,**
      IOCD    **,,**
RCHKB  STZ     NBAD
TCO    PZE     *
TRC    PZF     ERROR
      TRA     1,4
ERROR  SXA     54,4
      LXD     NBAD,4
      TXT     **1,4,1
      TXH     QUIT,4,5
      SXD     NBAD,4
BSR    BSR     **
      XEC     RDS
      XEC     RCH
S4     AXT     **,4
      TRA     TCO
QUIT   CLA     =00000C z 0 0 0 0 0 0 .
IQUIT  STO     **
      CAL     RDS
      STA     **+1
      REW     **
NRFT   TRA     **

NBAD'  PZE
TEMP   PZE
      END

```

*	SUBROUTINE	WRITER	
	LBL	WRITFB	
	COUNT	80	
	ENTRY	WSETB	(NTAPE,N,NRET,IQUIT)
	ENTRY	WRITFB	(NWRITE,A1,A2)
	ENTRY	WCHKR	
WSETB	SXA	X4,4	
	CAL*	1,4	
	ACL	=020	
	CALL	(IOS)	
	LDQ*	\$(TRC)	
	SLQ	TRC	
	LDQ*	\$(TCO)	
	SLQ	TCO	
	LDQ*	\$(RCH)	
	SLQ	RCH	
	CAL*	\$(ETT)	
	SLW	FTT	
	SLW	ETTOFF	
	CAL*	\$(WRS)	
	SLW	WRS	
	STA	RSR	
x 4	AXT	,4	
	CLA*	2,4	
	ARS	18 --	
	SUR	=1	
	STO	TEMP	
	CLA*	3,4	
	STA	NRET 1	
	STA	NRET 2	
	CLA	4,4	
	STA	IQUIT 1	
	STA	IQUIT 2	
FTTOFF	PZF		
	NOP		
	TRA	5,4	
WRITEB	CLA*	1,4	
	STD	WIO	
	STD	WIO+1	
	CLA	2,4	
	SUB	TEMP	
	STA	WIO	
	CLA	3,4	
	SUB	TEMP	
	STA	WIO+1	
ETT	PZF		
	TRP	SHORT	
WRS	PZE		
RCH	PZF	wIO	
	TRA	4,4	
WIO	IOCP	**,**,**	
	IOCD	**,**,**	
SHORT	CLA	=0000003000000	
IQUI T1	STO	**	
	CAL	WRS	
	STA	**+1	
	REW	**	
NRET 1	TRA	**	
WCHKB	ST7	NRAD	
TCO	PZE	*	
TRC	PZF	FRROR	
	TRA	1,4	
ERROR	SXA	S4,4	

	LXD	NBAD,4
	TXI	**+1,4,1
	TXH	QUIT,4,10
	SXD	NEAD,4
BSR	BSR	**
	XEC	WRS
	XEC	WRS
	XEC	WRS
	XEC	RCH
54	AXT	** ,4
	TRA	TCO
QUIT	CLA	=0000001000000
IQUIT2	STO	**
	CAL	WRS
	STA	**+1
	REW	**
NRFT2	TRA	**
NBAD	PZF	
TEMP	PZE	
	END	

```

*      SURROUTINE READC
      LBL      READC
      COUNT   62
      ENTRY   RSETC      (NTAPE,NRET,IQUIT)
      ENTRY   READC     (NREAD,A1,A2)
      ENTRY   RCHKC
RSETC  SXA     X4,4
      CAL*    1,4
      ACL     =O20
      CALL    (IOS)
      LDQ*    $(TRC)
      SLQ     TRC
      LDQ*    $(TCO)
      SLQ     TCO
      LDQ*    $(RCH)
      SLQ     RCH
      CAL*    $(RDS)
      SLW     RDS
      STA     RSR
x 4    AXT     ,4
      CLA*    2,4
      STA     NRET
      CLA     3,4
      STA     IQUIT
READC  TPA     4,4
      CLA*    1,4
      STD     RIO-
      STD     RIO+1
      ARS     18
      SUB     =1
      STO     TEMP
      CLA     2,4
      SUB     TEMP
      STA     RIO
      CLA     3,4
      SUB     TEYP
      STA     RIO+1
RDS    PZE
RCH    PZE     RIO
      TRA     4,4
RIO    IOCP    **,,**
      IOCD    **,,**
RCHKC  STZ     NRAD
TCO    PZF     *
TRC    PZE     FRROR
      TRA     1,4
ERROR  SXA     S4,4
      LXD     NBAD,4
      TXI     *+1,4,1
      TXH     QUIT,4,5
      SXD     NBAD,4
BSR'   BSR     **
      XEC     RDS
      XEC     RCH
s 4    AXT     **,4
      TRA     TCO
QUIT   CLA     =0000002000000
IQUIT  STO     **
      CAL     RDS
      STA     *+1
      REW     **
NRET   TRA     **
NBAD   PZE
TEMP   PZE
      END

```



```

*      SUBROUTINE WRITEC
      LBI      WRITFC
      COUNT   79
      ENTRY   WSETC      (NTAPE,NRET,IQUIT)
      ENTRY   WRITEC    (NWRITE,A1,A2)
      ENTRY   WCHKC
WSETC  SXA     X4,4
      CAL"    1,4
      ACL     =020
      CALL    (IOS)
      LDQ*    $(TRC)
      SLQ     TRC
      LDQ*    $(TCO)
      SLQ     TCO
      LDQ*    $(RCH)
      SLQ     RCH
      CAL*    $(ETT)
      SLW     ETT
      SLW     ET TOFF
      CAL*    $(WRS)
      SLW     WRS
      STA     BSR
x 4 -  AXT     ,4
      CLA*    2,4
      STA     NPET1
      STA     NRET2
      CLA     3,4
      STA     IQUIT1
      STA     IQUIT2
ETTOFF PZE
      NOP
      TRA     4,4
WRITEC CLA*    1,4
      STD     WIO
      STD     WIO+1
      ARS     18
      SUB     =1
      STO     TEMP
      CLA     2,4
      SUB     TEMP
      STA     WIO
      CLA     3,4
      SUB     TEMP
      STA     WIO+1
ETT    PZE
      TRA     SHORT
WRS    PZE
RCH    PZE     WIO
      TRA     4,4
WIO    IOCP    **,,**
      IOCD    **,,**
SHORT  CLA     =0000003000000
IQUIT1 STO     **
      CAL     WRS
      STA     **+1
      REW     **
NRET1  TRA     **
WCHKC  STZ     NBAD
TCO    PZE     *
TRC    PZF     ERROR
      TRA     1,4
ERROR  SXA     $4,4
      LXD     NBAD,4

```

	TXI	**+1,4,1
	TXH	QUIT,4,10
	SXD	NBAD,4
RSR	BSR	**
	XEC	WFS
	XEC	WRS
	XEC	WFS
	XEC	RCH
S4	AXT	** ,4
	TRA	TCC
QUIT	CLA	=0000001000000
IQUI T2	STO	**
	CAL	WRS
	STA	**+1
	REW	**
NRFT2	TRA	**
NBPD	PZE	
TEMP	PZE	
	END	