# ANALYSIS IN TRANSFORMATIONAL GRAMMAR

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# JOYCE FRIEDMAN AND THEODORE S. MARTNER

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#### **ABSTRACT**

In generating sentences by means of a transformational grammar, it is necessary to analyze trees, testing for the presence or absence of various structures. This analysis occurs at two stages in the generation process -- during insertion of lexical items (more precisely, in testing contextual features), and during the transformation process, when individual transformations are being tested for applicability.

In this paper we describe a formal system for the definition of tree structure of sentences. The system consists of a formal language for partial or complete definition of the tree structure of a sentence, plus an algorithm for comparison of such a definition with a tree. It represents a significant generalization of Chomsky's notion of "proper analysis", and is flexible enough to be used within any transformational grammar which we have seen.

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# Introduction

The notion of analysis described here is an outgrowth of a project which had as its primary goal the writing of a computer system to aid transformational grammarians [3]. Early in this project we realized that certain aspects of transformational grammar theory had never received the sort of formalization necessary for computer applications; this paper is essentially a description of our attempt to correct this situation in one such area. It should be noted that rigorous formalization is not simply an ad hog matter in order to be able to use the computer; questions of the relative simplicity of grammars are realistically answerable only when the grammars have been placed in a precise system of notation, and, more important, a transformational generative grammar cannot be said to have succeeded in defining a language unless it is possible to generate sentences by using the grammar without any appeal to intuition.

In the first part of this paper we define our notion of a <u>structural</u> <u>description</u> of a sentence, and define the conditions under which a sentence may be said to be <u>analyzable as</u> such a structural description; later we discuss our implementation of these concepts, in particular the algorithm which determines in what order the various possible analyses of a sentence are produced.

# Underlying concepts

We begin the discussion of <u>structural description</u> by explaining some underlying concepts and giving definitions of certain key terms. This is in line with one of the major goals of our project, namely uniformity, clarity, and precision of expression.

A <u>transformational- generative</u> grammar is a device for generating

sentences in a language. Note that this is a characterization rather than a definition; the only definition of transformational grammar given in this paper will be in terms of its three components: <a href="mailto:phrase structure">phrase structure</a>, transformations, and lexicon.

The phrase structure component is a phrase structure grammar. may commence with a sentence symbol (the letter S) and expand it by means of the grammar into a base tree which has the node labeled S as its top (root) node. In this tree, each nonterminal node (node with branches below it) corresponds to some phrase-structure rule in the sense that its label is the lefthand side of the rule and the labels of the nodes immediately below it are the symbols of the righthand side of the rule in the same left-to-right order. The labels of terminal nodes of the tree are terminal symbols of the grammar; the list of labels of terminal nodes, taken from left to right, is the terminal string of the tree. Nonterminal nodes of the tree are labeled with nonterminal symbols of the grammar. The nodes immediately beneath a given node are its daughters, and the given node immediately dominates them; a node dominates its daughters, the daughters of its daughters, etc. A tree node may have an associated complex symbol (see below); this complex symbol is not a daughter of the node, but is rather an adjunct to the label of the node. This tree is ; also known as the constituent structure of the sentence.

The transformational component contains <u>transformations</u> and a statement of the order in which these transformations are to be applied. A transformation consists primarily of a <u>structural description</u> and a <u>structural change</u>; it essentially makes the statement: "If the tree currently has this (given) structure, then change its structure in this manner."

The lexical component contains a list of vocabulary words, each of which has an associated <u>complex symbol</u>. A complex symbol is a collection of <u>feature specifications</u> which describe both the inherent characteristics of the word (e.g., Noun or Verb, +HUMAN or -HUMAN (or neither), etc.) (<u>inherent features</u>), and the sort of sentence environment into which it can be inserted (<u>contextual features</u>). Lexical insertion attaches vocabulary words to the terminal nodes of a tree in positions where all of their feature specifications are met. It inserts their complex symbols into the tree at the same time.

Since both the contextual feature and the structural description of a transformation ask the question "Does the tree we are working with have this structure?", they can be treated in the same manner for most purposes. We will say in both cases that the sentence tree is <a href="mailto:analyzable">analyzable</a> as the structural description if the answer to the above question is affirmative. The process of answering the question is <a href="mailto:analysis">analysis</a>; a matching of nodes in the sentence tree with their counterparts in the structural description will be <a href="mailto:analysis">analysis</a> of the sentence tree as the structural description.

### Structural description

We have defined the formats for writing transformational grammars in our system in a modification of the Backus-Naur form (BNF) used to define computer programming languages [5]. In BNF, the definition of a structural description and a contextual feature description are:

structural description ::= structural analysis opt[,WHERE restriction].
contextual feature description ::= ( structure opt[,WHERE restriction])
structural analysis ::= list[ term ]

term = opt[ integer ] structure or opt[ integer ] choice or skip

This definition can be thought of as a procedure for checking whether a string of characters is one of the underlined items. The :=may be read "is a". The operator opt[] means that whatever is between the brackets may or may not be present. The notation A or B is obvious. The operator list[] means that one or more of whatever is between the brackets should be present; for example, list[A or B] could be A or B or A A or A B or A B B A A etc. The operator clist  $\begin{bmatrix} 1 \end{bmatrix}^1$ resembles list[], but separate occurrences of whatever is between the brackets are separated by commas; for example, clist[ A or B ] could be A or B or A,A or A,B or A,A,B,A,B etc. All other symbols which are not underlined mean themselves. There are four items left undefined by the above; these are <u>restriction</u>, which will be discussed later, complex symbol, which is defined in [4], integer, which is any positive integer, and node, which may be any string of letters and digits starting with a letter or may be a boundary symbol ( # ). For example, \$1(EN,ING) 2(HAVE,BE) \$ . is a structural description which is the structural analysis \$ 1(EN,ING) 2(HAVE,BE) \$ followed by a .; this structural analysis is a list of the terms \$ , 1(EN, ING) , 2(HAVE, BE), %; the first and last of these terms are skips, each of which is the symbol %, while the second and third are the choices (EN,ING)

<sup>1 &</sup>quot;clist" is pronounced see-list, and is a noun of the same type as "herd".

and (HAVE, BE) preceded by the <u>integers</u> 1 and 2; each <u>choice</u> consists of a (followed by a clist of <u>structural analyses</u> EN, ING and `HAVE, BE followed by a ); each <u>structural analysis</u> here is a list of exactly one <u>term</u>, which is a <u>structure</u> without any preceding <u>integer</u>; each of these <u>structures</u> is an <u>element</u> without any of the optional items, and each element is a node.

The above description has not in any way explained the meaning of these items; it has simply defined how to write them., The meaning of structural description and contextual feature description can be best explained in terms of analyzability and analysis, since their purpose is precisely-to test trees for analyzability and to provide analyses of trees. Although a structural description contains a structural analysis and a contextual feature description contains a structure, the recursiveness of their definitions makes them very similar. The difference stems from the fact that when transformations are being applied the position of the top node of the current tree is known, while during lexical insertion only the terminal node at which insertion is being attempted is known. For this reason, the contextual feature must specify the label of a node somewhere above the insertion node which can serve as tree top. In the following discussion, whenever a structural description is referred to, we will mean either a structural description or a contextual feature description.

# Analyzability

We will define analyzability in two phases; first we will consider a <u>structural analysis</u> or <u>structure</u> without any associated <u>restriction</u>, and then we will consider how the presence of a restriction modifies the

definition.

If a structural description is simply a list of <u>elements</u>, analyzability is similar to Chomsky's notion of "proper analysis" [1]. A tree is analyzable as a structural description of this form if a one-to-one match of certain tree nodes with all of the structural description elements can be found such that:

- 1. Each terminal node in the tree is, or is dominated by, exactly one node in the match.
- Left-to-right order of <u>elements</u> corresponds to left-to-right order of matching tree nodes.
- 3a. For each <u>element</u> which is a <u>node</u>, the label of the matching tree node is the same as the node.
- 3b. For each element which is a \_\_\_, the matching tree node is the
   node at which lexicon insertion is currently being attempted.

  (Note that a \* will thus match any one tree node, regardless of its label.)

A <u>complex symbol</u> following an <u>element</u> requires that a corresponding <u>complex symbol</u> be attached to the matching tree node. "Corresponding" has a different meaning for lexicon insertion than for transformations; in the case of lexicon insertion the test is compatibility (roughly, no conflicting feature specifications; see [4] for a precise definition), while for transformations the test is inclusion (that is, the <u>complex symbol</u> in the tree contains every feature specification of the one in the structural description).

A <u>skip</u> (the **%** symbol) matches not a single node, but any string of adjacent terminal nodes. It may match a string of zero nodes, in which case it is said to be null. The "range" of a <u>skip</u> is defined in

terms of the <u>elements</u> on either side; it is the set of tree nodes which dominate (or equal) the nodes matching the <u>skip</u> and do not dominate the nodes matched by these <u>elements</u>. In other words, the range of a <u>skip</u> is precisely those tree nodes which would have to be deleted if the <u>skip</u> were not present in order to have the analysis of the tree as the structural description be the same as before.

The matching of a <a href="choice">choice</a> is somewhat more complex. The procedure depends on whether the clist within the choice has only one <a href="structural">structural</a> analysis, or more than one. If there is only one <a href="structural">structural</a> analysis, it is regarded as optional; that is, the tree is analyzable either if it is analyzable as a similar structural description without the parentheses of the choice, or if it is analyzable as a similar structural description without any of the choice being present. If there is more than one <a href="structural">structural</a> analyzable if it is analyzable as a similar structural description with some one of the <a href="structural">structural</a> analyzable as a similar structural description with some one of the <a href="structural">structural</a> analyzable in place of the <a href="choice">choice</a>. (Note that the only requirement here is that at least one <a href="structural">structural</a> analyzis will work; if several different ones could be analyzably substituted; it merely means that the tree is analyzable as this structural description in several ways.)

A <u>structural analysis</u> within angle brackets following an element represents a "subanalysis". The analysis of the whole tree as the structural description is unchanged, but in order that the tree be analyzable, there is a further requirement on analyzability of the subtree headed by the node matched to the head <u>element</u> of the angle-bracketed <u>structural analysis</u>. The exact requirement depends on the presence of the optional modifiers ¬ and / . If only a / is

present, this sub-tree must be analyzable in the usual sense, with the minor exception that the top node of the subtree is not allowed to match any element in the structural analysis. If neither modifier is present, the subtree must be analyzable in the above sense, with the further restriction that any element in the structural analysis must match a tree node which is immediately dominated by the top node of the subtree. In the case of contextual features, this corresponds to Chomsky's notion of strict local subcategorization [2]. If a ¬ modifier is present, it means that the sub-tree must not be analyzable in the sense defined above.

Integers do not directly enter into the analysis process. They are used to permit reference to tree nodes in a restriction or a structural change. An <a href="integer">integer</a> preceding a <a href="structure">structure</a> refers to the tree node which matches the <a href="element">element</a> heading that <a href="structure">structure</a>. An <a href="integer">integer</a> preceding a <a href="choice">choice</a> is handled exactly as if it had been written at the beginning of every <a href="structural analysis">structural analysis</a> in the clist of the <a href="choice">choice</a>. Note that complex symbols are not numbered directly; the <a href="integer">integer</a> attaches to the tree node and will refer to the complex symbol associated with that node in any context which requires a complex symbol.

# Restrictions

If a structural description or contextual feature description has an associated <u>restriction</u>, analysis proceeds exactly as above, except that the analysis of the tree must also meet the <u>restriction</u> in order for the tree to be analyzable. The BNF format for restriction is:

restriction ::= booleancombination[ condition ]

condition ::= unary condition or binary condition

unary condition ::= unary relation integer

<u>binary condition</u> ::= <u>integer</u> <u>binary tree relation node designator</u> or integer binary complex relation complex symbol designator

node designator ::= integer or node

complex symbol designator ::= complex symbol or integer
where booleancombination[ condition ] means any Boolean combination of
conditions which can be expressed using the connectives .&.
(not, and, or) and parentheses.

The conditions now in the system are:

(unary conditions) the match must be to a terminal/tree node; or null (in the case of an option); also a special condition useful where more than one analysis is to be found, e.g. that the match in the current analysis be to a different tree node than in any of the previous successful analyses.

(binary tree conditions) equality of trees (including identity of corresponding complex symbol); dominance without searching below a sentence symbol; unrestricted dominance; domination by a specified node.

(binary complex conditions) inclusion of complex symbols; nondistinctness of complex symbols; and compatibility of complex symbols (see [4]).

The restriction on a structural description is tested whenever a new match is found for a structure with a corresponding <u>integer</u>. If the <u>restriction</u> fails, the structure does not match. In a conditional <u>structural change</u>, a <u>restriction</u> may be used to select one of two possible structural changes (see below).

# Analysis Algorithm

In this section we discuss the algorithm used to find a particular analysis of a tree as a structural description. This algorithm has nothing to do with the question of analyzability; it merely decides the order in which several possible analyses are taken if a sentence tree can be analyzed in more than one way as a particular structural description. This is particularly important if the transformation specifies that only one analysis is to be found.

Analysis commences with a tree marker pointing to the top node of the tree and a structural description marker pointing to the first item in the structural description. The procedure depends on the nature of this item.

Integers and skips are skipped but remembered. For an element (i.e., the beginning of a structure), a match is attempted. A \* will match any tree node, a node will match a node with the same label, and a \_\_\_\_ will match the current lexical insertion node. If there is not a match, the tree marker is moved to point to the leftmost daughter of the current node, and matching is attempted again. If no match is found of a terminal node and no skip preceded the current element, the backup procedure is entered (see below). If a skip preceded, the tree marker is moved to the top of the tree branch just right of the current branch, and matching is attempted again; in this case, the backup procedure is entered only if no match can be found for the rightmost terminal node of the tree.

If a match is found and a <u>complex symbol</u> follows the <u>element</u>, it will be compared to the complex symbol attached to the matching tree node for compatibility (in a contextual feature description) or inclusion

(in a structural description). If an <u>integer</u> precedes the <u>element</u>, any conditions involving this <u>integer</u> are checked. In the case of a binary condition, no checking is performed until both <u>integers</u> have been matched. Failure of any of these 'tests causes analysis to proceed as if the node had not matched the element.

If the structural description marker is pointing to a choice instead of an element, the procedure to be followed depends on whether the clist of the choice contains only one structural analysis (an option), or more than one (a true choice). For an option, the ( of the choice is ignored; options affect only the backup procedure. For a true choice, a more complicated procedure is necessary. First, a list is made of all elements which could possibly be first in the choice, in left-toright order. For example, if the choice were (A, (B)(C,D), % E, % (F,G)), this list would be A - B - C - D - E - F - G  $\cdot$  The element-matching procedure is then followed as above, but at each tree node all of the possible elements are tested for matches and for satisfactory complex Msymbolstanduin regears. l l y , only those <u>elements</u> which are preceded by skips are tested after a terminal-node failure. When a satisfactory match has been found between a tree node and some element, analysis proceeds along the associated structural analysis of the choice, at the end of which it continues following the choice.

If a <u>structural analysis</u> within angle brackets follows an <u>element</u> that has been satisfactorily matched, a record is made of relevant information about the current status of things, and analysis commences again, using the angle-bracketed <u>structural analysis</u> and the subtree headed by the node matched to the <u>element</u>. If no / preceded, the tree

marker is only allowed to point to immediate daughters of the top node during this analysis, instead of looking all the way down to terminal nodes. If a ¬ preceded and the subtree is not analyzable, or if no ¬ preceded and the subtree is analyzable, analysis continues following the angle-bracketed <u>structural analysis</u>; otherwise, analysis proceeds as if the head element had not matched its tree node.

When a <u>structure</u> has been successfully matched, the tree marker is moved to point to the top node of the tree branch immediately to the right of the tree node matching the head <u>element</u>, and analysis proceeds. The tree is analyzable as the structural description if the rightmost <u>element</u> not within angle brackets successfully matches a tree node on the rightmost branch of the tree, or if the rightmost such <u>element</u> has been successfully matched in any way and a <u>skip</u> follows it.

The backup procedure is entered when no tree node can be found which successfully matches the current <u>element</u> or <u>choice</u>. It moves the structural description marker backward to the left until it encounters a previously-matched <u>element</u> (in which case it pretends that this <u>element</u> did not match its tree node and starts forward again), or the ( of a one-<u>structural analysis choice</u> (in which case it hops to the ) of the choice and starts forward), or the lefthand end of the structural description (in which case the tree is not analyzable as the structural description).

For certain transformations, all possible analyses of the tree are required instead of just one. In this case, after each analysis is found, the backup procedure is entered to find the next one, until it

finally claims unanalyzability.

# Structural Change

Because of the close relationship between the structural description and structural change of a transformation, any comparison of our system with others requires that the whole concept of transformation be considered at once. For that reason, we now give a description of the structural change process. The BNF description of the form of a structural change is:

```
structural change ::= clist[ change instruction ]
change instruction ::= change or conditional change
conditional change ::= IF \( \) restriction \( \) THEN
\( \) structural change \( \) opt[ ELSE \( \) structural change \( \)]
change ::= unary operator integer

or tree designator binary tree operator integer

or complex symbol designator binary complex operator
integer
```

or <u>complex symbol designator</u> <u>ternary complex operator</u>

<u>integer</u> e <u>g e r</u>

tree designator ::= ( tree ) or integer or node
 complex symbol designator ::= complex symbol or integer
The operators are given by a list in the BNF form and are discussed below.

If the current sentence tree is analyzable as a structural description and the transformation is to be performed, each <u>change</u>

<u>instruction</u> in the clist is performed in the order of occurrence
in the clist. Tree nodes have been matched to <u>integers</u> by the analysis

process; a  $\underline{\text{change}}$  modifies the tree structure at the nodes matched to its integer (s).

The change operators currently in the system are:

(unary operators) erasure of the node, all nodes dominated by it, and all non-branching nodes dominating it,

(binary tree operators) left and right sister, daughter, and aunt adjunction, and substitution, with or without erasure of the original occurrence of the copied node, and optionally with special treatment of the non-branching nodes which dominate (as in [9]).

(binary complex operators) erasure of, merging of, or erasure of all but, specified feature specifications in the complex symbol associated with the node,

(ternary complex operators) merging of specified features from one node's complex symbol to another's

A <u>conditional change</u> causes the <u>structural change</u> following THEN to be performed if the <u>restriction</u> is met; otherwise the <u>structural</u> <u>change</u> following ELSE is performed, if there is one.

The change operators discussed above may be broken down into four types: erasure, copying, moving and complex symbol manipulation.

Permutations are not given directly, since only one move can be made at a time. The only transformation of this type that we have seen is PASSIVE, for which we require three changes (copy, move, erase) to interchange the subject and object.

The structural change operators include all of those of the MITRE grammar [11] as well as those of the IBM core grammar [9]. The addition of "Chomsky-adjunction" is planned.

# Comparisons with other notations

In a transformation, our structural analysis plays essentially the same role as the "structural description" and "structural analysis" which were first used by Chomsky. As an example, here is a transformation from Rosenbaum and Lochak [9]:

60. WHPD2 WH pronoun Deletion 2 OB

X WH + INDEF + (ever) 
$$\begin{bmatrix} <+PRO \\ <+Sg > \end{bmatrix}$$
N Y

1 2 3 4 ----->
1 2  $\phi$  4

In our system this would be written

TRANS 60 WHPD2 "WH PRONOUN DELETION 2" OB II AACC .

SD 
$$\%$$
 WH INDEF (EVER) 1 N |+PRO +SG|  $\%$  .

SC ERASE1 1 .

The first line gives the transformation identification and the conditions of applicability. In this case the transformation number and name are followed by a comment and by parameters specifying that the transformation is obligatory (OB), is in group II, and that it is to be applied by first finding all possible analyses and then performing the changes for each of them (AACC). A full discussion of the possible parameters is given in [6]. The second line is our structural description. As can be seen, the details of the representation are different, the major features are the same. We chose the \$\%\$ symbol rather than X, Y, Z to represent variables because these letters are possible labels for nodes. This decision reinforces the idea that a variable need not be a constituent. The standard use of parentheses for options is carried over into our notation; in addition, we reflect the use of curly brackets for a choice

by allowing a clist of structural analyses within parentheses. Our notation for complex symbols resembles standard notation except for the use of vertical bars in place of square brackets; see [4] for a complete discussion of complex symbols in the system. The most significant change is in our use of numbers, since we allow only constituents to be numbered, and do not require numbering of items which are not referred to in either the structural change or the restriction. This is a result of our treatment of transformations as changes of position of single constituents rather than rearrangements of the whole tree. In this we follow the approach taken in the MITRE grammars [11]; we have extended the approach to complex symbol operations.

Gross [7] and Londe and Schoene [8] have also developed notations for transformations, in both cases for use with grammar testers. Both notations differ from ours in form and have less power in the structural description. For example, Gross does not include complex symbols; neither allows any equivalent of a Londe and Schoene require that immediate dominance be expressed as a restriction. However, both systems contain more powerful notations than ours for structural change.

# Future directions

The analysis algorithm was designed to correspond to the linguistic theory based on Aspects [2]. Since that time there have been radical changes in the theory; the change of particular importance for analysis is the strong notion of general constraints on transformations, following from the work of Ross [10]. Thus, if the system is to be extended and kept current with the theory, the first changes will need to be in devising notations and algorithms for the implementation of

general conditions on the applicability of transformations.

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