CS 89

ALGOL W (REVISED)

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ALGOL W

DECK SET-UP

by

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Algol W Deck Set-Up

```
< Job Card >

//JOBLIB DD DSNAME=SYS2. PROGLIB,DISP=(OLD,PASS)

//   EXEC  ALGOLW

//ALGOLW.SYSIN DD *

        %ALGOL

             < program>

        %EOF

             < data >

        %EOF

        /*
```

** (brace grouping)
* (brace grouping)

    * Optional

Note : The maximum execution time or number of printed lines for the

job may optionally be specified on the %ALGOL card. Columns 10-29

of that card are scanned for such specification according to the

following syntax:

```
<limit specification>     ::=  <time limit, | <time limit>, <line limit>
<time limit>              ::=  <minutes specification2 |
                              <minutes specification> : <seconds specification2
<minutes specification>   ::= <unsigned integer> | (empty}
<seconds specification)   ::= <unsigned integer? | (empty)
<line limit>              ::=  <unsigned integer> | (empty)
```

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An empty field is given the value zero. If the time limit specified is
zero, termination for excess time is controlled by the ∅S jcb card. Other-
wise, the program is automatically terminated if necessary at the end
of the indicated time. Similarly, if the line limit specified is zero,
termination for excess lines is controlled by the ∅S job card; otherwise,
the program is automatically terminated if necessary after the indicated
number of lines have been printed.

ALGOL W

LANGUAGE DESCRIPTION

by

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"A Contribution to the Development
of ALGOL" by Niklaus Wirth and C. A. R.
Hoare[1] was the basis for a compiler de-
veloped for the IBM 360 at Stanford Univer-
sity.   This report is a description of the
implemented language, ALGOL W.   Historical
background and the goals of the language
may be found in the Wirth and Hoare paper.

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[1] Wirth, Niklaus and Hoare, C. A. R., "A
Contribution to the Development of ALGOL",
Comm. ACM 9, 6(June 1966), pp. 413-431.

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1. TERMINOLOGY, NOTATION AND BASIC DEFINITIONS

The Reference Language is a phrase structure language, defined by
a formal metalanguage. This metalanguage makes use of the notation and
definitions explained below. The structure of the language ALGOL W
is determined by:

    (1) V, the set of basic constituents of the language,

    (2) U, the set of syntactic entities, and

    (3) P, the set of syntactic rules, or productions.

1.1. Notation

A syntactic entity is denoted by its name (a sequence of letters)
enclosed in the brackets < and >. A syntactic rule has the form

        <A> ::= x

where <A> is a member of U, x is any possible sequence of basic con-
stituents and syntactic entities, simply to be called a "sequence".
The form

        <A> ::= x | y | ... | z

is used as an abbreviation for the set of syntactic rules

        <A> ::= x

        <A> ::= y

        ....

        <A> ::= z

1.2, Definitions

    1.   A sequence x is said to directly produce a sequence y if and

only if there exist (possibly empty) sequences u and w, so that
either (i) for some <A> in U, x = u<A>w, y = uvw, and <A> ::=
v is a rule in P; or (ii) x = uw, y = uvw and v is a "comment"
(see below).

2.   A sequence x is said to <u>produce</u> a sequence y if and only if
there exists an ordered set of sequences s[0], s[1], . . . , s[n],
so that x = s[0], s[n] = y, and s[i-1] directly produces s[i] for
all i = 1, . . . , n.

3.   A sequence x is said to be an ALGOL W program if and only if
its constituents are members of the set V, and x can be produced
from the syntactic entity <program>.

The sets V and U are defined through enumeration of their members
in Section 2 of this Report (cf. also 4.4.). The syntactic rules are
given throughout the sequel of the Report. To provide explanations
for the meaning of ALGOL W programs, the letter sequences denoting
syntactic entities have been chosen to be English words describing
approximately the nature of that syntactic entity or construct, Where
words which have appeared-in this manner are used elsewhere in the
text, they refer to the corresponding syntactic definition. Along
with these letter sequences the symbol J may occur. It is understood
that this symbol must be replaced by any one of a finite set of English
words (or word pairs). Unless otherwise specified in the particular
section, all occurrences of the symbol J within one syntactic rule
must be replaced consistently, and the replacing words are

```
     integer                logical
     real                   bit
     long real              string
     complex                reference
     long complex
```

For example, the production

$$\langle \mathcal{J}\ term\rangle ::= \langle \mathcal{J}\ factor\rangle \qquad (cf.\ 6.3.1.)$$

corresponds to

```
<integer term>        ::=  <integer factor>
<real term>           ::=  <real factor>
<long real term>      ::=  <long real factor>
<complex term>        ::=  <complex factor>
<long complex term>   ::=  <long complex factor>
```

The production

$$\langle \mathcal{J}_0\ primary\rangle ::= \underline{long}\ \langle \mathcal{J}_1\ primary\rangle \qquad (cf.\ 6.3.1.\ and$$

corresponds to

table for $\underline{long}$
6.3.2.7.)

```
<long real primary>    ::= long <real primary2
<long real primary>    ::= long <integer primary>
<long complex primary> ::= long <complex primary>
```

It is recognized that typographical entities exist of lower order than basic symbols, called characters. The accepted characters are those of the IBM System 360 EBCDIC code.

The symbol comment followed by any sequence of characters not containing semicolons, followed by a semicolon, is called a comment. A comment has no effect on the meaning of a program, and is ignored during execution of the program. An identifier (cf. 3.1.) immediately

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following the basic symbol end is also regarded as a comment.

The execution of a program can be considered as a sequence of units of action. The sequence of these units of action is defined as the evaluation of expressions and the execution of statements as denoted by the program. In the definition of the implemented language the evaluation or execution of certain constructs is either (1) defined by System 360 operations, e.g., real arithmetic or (2) left undefined, e.g., the order of evaluation of arithmetic primaries in expressions, or (3) said to be not valid or not defined.

2. SETS OF BASIC SYMBOLS AND SYNTACTIC ENTITIES

2.1. Basic Symbols

A | B | C | D | E | F | G | H | I | J | K | L | M | N | O | P |
Q | R | S | T | U | V | W | X | Y | Z |
0 | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 |
true | false | " | null | # | ' |
integer | real | complex | logical | bits | string |
reference | long real | long complex | array |
procedure | record |
_ | ; | : | . | (|) | begin | end | if | then | else |
case | of | + | - | * | / | ** | div | rem | shr | shl | is |
abs | long | short | and | or | ¬ | | | = | ¬ = | < |
< = | > | > = | :: |
:= | goto | go to | for | step | until | do | while |
comment | value | result

All underlined words, which we call "reserved words", are represented by the same words in capital letters in an actual program, with no intervening blanks

Adjacent reserved words, identifiers (cf. 3.1.) and numbers must have
no blanks and must be separated by at least one blank space. Otherwise
blanks have no meaning and can be used freely to improve the read-
ability of the program.

2.2. Syntactic Entities

(with corresponding section numbers)

\<actual parameter list\>	7.3	\<formal type\>	5.3
\<actual parameter\>	7.3	\<go to statement\>	7.4
\<bit factor\>	6.5	-\<hex digit\>	4.3
\<bit primary\>	6.5	\<identifier list\>	3.1
\<bit secondary\>	6.5	\<identifier\>	3.1
\<bit sequence\>	4.3	\<if clause\>	6
\<bit term\>	6.5	\<if statement-=	7.5
		-\<imaginary number\>	4.1
\<block body\>	7.1	\<increment\>	7.7
\<block head\>	7.1	\<initial value\>	7.7
\<bloc&	7.1	\<iterative statement\>	7.7
\<bound pair list\>	5.2	\<label definition\>	7.1
\<bound pair\>	5.2	\<label identifier\>	3.1
\<case clause\>	6	\<letter\>	3.1
\<case statement\>	7.6	\<limit\>	7.7
\<control identifier\>	3.1	\<logical element\>	6.4
\<declaration\>	5	\<logical factor\>	6.4
\<digit\>	3.1	\<logical primary\>	6.4
\<dimension specification\>	5.3		
\<empty\> see page 34		\<logical term\>	6.4
\<equality operator\>	6.4	\<logical value\>	4.2
\<expression list\>	6.7	\<lower bound\>	5.2
\<field list\>	5.2	\<null reference\>	4.5
\<for clause\>	7.7	\<procedure declaration\>	5.3
\<for list\>	7.7	\<procedure heading\>	5.3
\<formal array parameter3	5.3	\<procedure identif ier\>	3.1
\<formal parameter list\>	5.3	\<procedure statement\>	7.3
\<formal parameter segment\>	5.3	\<program\>	7

3. IDENTIFIERS

3.1. Syntax

<identifier> ::= <letter> | <identifier> <letter> | <identifier> <digit>
<ℑ variable identifier> ::= <identifier>

```
<𝔍 array identifier>  ::=  <identifier>
<procedure  identifier>  ::=  <identifier>
<𝔍 function identifier>  ::=  <identifier>
<record class identifier> ::= <identifier>
<𝔍 field identifier> ::= <identifier>
<label  identifier>  ::=  <identifier>
<control  identifier>  ::=  <identifier>
<letter>  ::=  A | B | C | D | E | F | G | H | I | J | K | L | M |
               N | O | P | Q | R | S | T | U | V | W | X | Y | Z
<digit> ::= 0 | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9
<identifier list>  ::=  <identifier> | <identifier list> , <identifier>
```

3.2. Semantics

Variables, arrays, procedures, record classes and record fields
are said to be quantities. Identifiers serve to identify quantities,
or they stand as labels, formal parameters or control identifiers.
Identifiers have no inherent meaning, and can be chosen freely in the
reference language. In an actual program a reserved word cannot be
used as an identifier.

Every identifier used in a program must be defined. This is
achieved through

(a) a declaration (cf. Section 5), if the identifier identifies a
     quantity. It is then said to denote that quantity and to be a
     𝔍 variable identifier, 𝔍 array identifier, 𝔍 procedure identifier,
     𝔍 function identifier, record class identifier or 𝔍 field iden-
     tifier, where the symbol 𝔍 stands for the appropriate word re-
     flecting the type of the declared quantity;

(b) a label definition (cf. 7.1.), if the identifier stands as a

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label. It is then said to be a label identifier;

(c) its occurrence in a formal parameter list (cf. 5.3.). It is then said to be a formal parameter;

(d) its occurrence following the symbol <u>for</u> in a for clause (cf. 7.7.). It is then said to be a control identifier;

(e) its implicit declaration in the language. Standard procedures, standard functions, and predefined variables (cf. 8.3) may be considered to be declared in a block containing the program.

The recognition of the definition of a given identifier is determined by the following rules:

Step 1. If the identifier is defined by a declaration of a quantity or by its standing as a label within the smallest block (cf. 7.1.) embracing a given occurrence of that identifier, then it denotes that quantity or label. A statement following a procedure heading (cf. 5.3.) or a for clause (cf. 7.7.) is considered to be a block.

Step 2. Otherwise, if that block is a procedure body and if the given identifier is identical with a formal parameter in the associated procedure heading, then it stands as that formal parameter.

Step 3. Otherwise, if that block is preceded by a for clause and the identifier is identical to the control identifier of that for clause, then it stands as that control identifier.

Otherwise, these rules are applied considering the smallest block embracing the block which has previously been considered.

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If either step 1 or step 2 could lead to more than one definition, then the identification is undefined.

The scope cf a quantity, a label, a formal parameter, or a control identifier is the set of statements in which occurrences of an identifier may refer by the above rules to the definition of that quantity, label, formal parameter or control identifier.

3.3. Examples,

    I
    PERSON
    ELDERSIBLING
    x15, X20, x25

4.   VALUES AND TYPES

Constants and variables (cf. 6.1.) are said to possess a value. The value of a constant is determined by the denotation of the constant . In the language, all constants (except references) have a reference denotation (cf. 4.1.-4.4.). The value of a variable is the one most recently assigned to that variable. A value is (recursively) defined as either a simple value or a structured value (an. ordered set of one or more values). Every value is said to be of a certain type. The following types of simple values are distinguished:

    <u>integer</u>: the value is a 32 bit integer,
    <u>real</u>: the value is a 32 bit floating point number,
    <u>Long</u> <u>real</u>:   the value is a 64 bit floating point number,
    <u>complex</u>:   the value is a complex number composed of two
            numbers of type <u>real</u>,

<u>complex</u>: the value is a complex number composed of two
<u>long</u> <u>real</u> numbers,

<u>logical</u>: the value is a logical value,

<u>bits</u>: the value is a linear sequence of 32 bits,

<u>string</u>: the value is a linear sequence of at most 256 char-
acters,

<u>reference</u>: the value is a reference to a record.

The following types of structured values are distinguished:

<u>array</u>: the value is an ordered set of values, all of identi-
cal simple type, ·

<u>record</u>: the value is an ordered set of simple values.

A procedure may yield a value, in which case it is said to be a
function procedure, or it may not yield a value, in which case it is
called a proper procedure. The value of a function procedure is de-
fined as the value which results from the execution of the procedure
body (cf. 6.2.2.).

Subsequently, the reference denotation of constants is defined.
The reference denotation of any constant consists of a sequence of
characters. This, however, does not imply that the value of the de-
noted constant is a sequence of characters, nor that it has the pro-
perties of a sequence of characters, except, of course, in the case
of strings.

4.1. <u>Numbers</u>

4.1.1. Syntax

```
<long complex number>  ::=  <complex number>L
<complex number>   ::=  <imaginary number>
<imaginary number> ::=  <real number>I | <integer number>I
```

```
<long real number> ::= <real number>L | <integer number>L
<real number> : := <unscaled real> | <unscaled real> <scale factor> |
                <integer number> <scale factor> | <scale factor>
<unscaled real> ::= <integer number> .<integer number> |
                *<integer number> | <integer number> .
<scale factor> : := '<integer number> |'<sign> <integer number>
<integer number> ::= <digit> | <integer number> <digit>
<sign> ::= + | -
```

4.1.2. Semantics

Numbers are interpreted according to the conventional decimal notation. A scale factor denotes an integral power of 10 which is multiplied by the unscaled real or integer number preceding it. Each number has a uniquely defined type. (Note that all <number>s are unsigned.)

4.1.3. Examples

```
    1          .5            11
     0100        1'3           0.67I
    3.1416       6.02486'+23    1IL
    2.718281828459045235360287L    2.3'-6
```

4.2. Logical Values

4.2.1. Syntax

```
<logical value> ::= true | false
```

4.3. Bit Sequences

4.3.1. Syntax

```
<bit sequence> ::= # <hex digit> | <bit sequence> <hex digit>
<hex digit> ::= 0 | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | A | B |
               C | D | E | F
```

Note that $2 \mid ... \mid F$ corresponds to $2_{10} \mid . . . \mid 15_{10}$.

4.3.2. Semantics

The number of bits in a bit sequence is 32 or 8 hex digits. The bit sequence is always represented by a 32 bit word with the specified bit sequence right justified in the word and zeros filled in on the left.

4.3.3. Examples

$\#4F$ = 0000 0000 0000 0000 0000 0000 0100 1111
$\#9$ = 0000 0000 0000 0000 0000 0000 0000 1001

4.4. Strings

4.4.1. Syntax

<string> ::= "<sequence of characters>"

4.4.2. Semantics

Strings consist of any sequence of (at mast 256) characters accepted by the System 360 enclosed by ", the string quote, If the string quote appears in the sequence of characters it must be immediately followed by a second string quote which is then ignored. The number of characters in a string is said to Be the length of the string.

4.4.3. Examples

"JOHN"
"""" is the string of length 1 consisting of the string
        quote.

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4.5. References

4.5.1. Syntax

`<null reference3 ::= null`

4.5.2. Semantics

The reference value null fails to designate a record; if a reference expression occurring in a field designator (cf. 6.1.) has this value, then the field designator is undefined.

5. DECLARATIONS

Declarations serve to associate identifiers with the quantities used in the program, to attribute certain permanent properties to these quantities (e.g. type, structure), and to determine their scope. The quantities declared by declarations are simple variables, arrays, procedures and record classes.

Upon exit from a block, all quantities declared or defined within that block lose their value and significance (cf. 7.1.2. and 7.4.2.).

Syntax:

```
<declaration> ::= '<simple variable declaration> | <J array
                  declaration> | <procedure declaration> |
                  <record class declaration>
```

5.1. Simple Variable Declarations

5.1.1. Syntax

```
<simple variable declaration> ::= <simple type> <identifier list=>
<simple type> ::= integer | real | long real | complex | long
                  complex | logical | bits | bits (32) |
```

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$$\text{string} \mid \text{string} (\text{<integer>}) \mid \underline{\text{reference}}$$
$$(\text{<record class identifier list>})$$

<record class identifier list> ::= <record class identifier> |

                                      <record class identifier list> ,

                                      <record class identifier>

5.1.2. Semantics

Each identifier of the identifier list is associated with a
variable which is declared to be of the indicated type. A variable is
called a simple variable, if its value is simple (cf. Section 4). If
a variable is declared to be of a certain type, then this implies that
only values which are assignment compatible with this type (cf. 7.2.2.)
can be assigned to it. It is understood that the value of a variable
is equal to the value of the expression most recently assigned to it.

A variable of type $\underline{\text{bits}}$ is always of length 32 whether or not
the declaration specification is included.

A variable of type $\underline{\text{string}}$ has a length equal to the unsigned
integer in the declaration specification. If the simple type is
given only as $\underline{\text{string}}$, the length of the variable is 16 characters.

A variable of type $\underline{\text{reference}}$ may refer only to records of the
record classes whose identifiers-appear in the record class identi-
fier list of the reference declaration specification.

5.1.3. Examples

```
integer I, J, K, M, N
real X, Y, Z
long complex C
Logical
bits G, H
```

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string (10) S, T

        reference (PERSON) JACK, JILL

5.2. Array Declarations

5.2.1. Syntax

<J array declaration> ::= <simple type> array <identifier list>
                         (<bound pair list>)
<bound pair lists ::= <bound pair> |<bound pair list>,<bound
                         pair>
<bound pair> ::= <lower bound> :: <upper bound>
<lower bound> ::= <integer expression>
<upper bound> ::= <integer expression>

5.2.2. Semantics

Each identifier of the identifier list of an array declaration is
associated with a variable which is declared to be of type array,
variable of type array is an ordered set of variables whose type is the
simple type preceding the symbol array, The dimension of the array is
the number of entries in the bound pair list,

Every element of an array is identified by a list of indices.
The indices are the integers between and including the values of the
lower bound and the upper bound, Every expression in the bound pair
list is evaluated exactly once upon entry to the block in which the
declaration occurs. The bound pain expressions can depend only on
variables and procedures global to the block in which the declaration
occurs . In order to be valid, for every bound pair, the value of' the
upper bound must not be less than the value of the lower bound.

5.2.3. Examples

        integer array H(1::100)

                              15

real array A, B(1::M, 1::N)

string (12) array STREET, TOWN, CITY (J::K + 1)

5.3. <u>Procedure Declarations</u>

5.3.1. Syntax

<procedure declaration> ::= <proper procedure declaration> |
             <J function procedure declaration>

<proper procedure declaration> ::= <u>procedure</u> <procedure heading>;
           <proper procedure body>

<J function procedure declaration> ::= <simple type> <u>procedure</u>
           <procedure heading>;
           <J function procedure body>

<proper procedure body> ::= <statement>

<J function procedure body> ::= <J expression> | <block body>
           <J expression> <u>end</u>

<procedure heading> ::= <ident if ier> | <ident if ier> (<formal
         parameter list;>)

<formal parameter list> ::= <formal parameter segment> |
         <formal parameter list> ; <formal
         parameter segment>

<formal parameter segment> ::= <formal type> <identifier list> |
         <formal array parameter>

<formal type> ::= <simple type> | <simple type> <u>value</u> | <simple
        type> <u>result</u> | <simple type> <u>value</u> <u>result</u> |
        <simple type> <u>procedure</u> | <u>procedure</u>

<formal array parameter> ::= <simple type> <u>array</u> <identifier
        list> (<dimension specification>)

<dimension specif icat ion> ::= * | <dimension specification> , *

5.3.2. Semantics

A procedure declaration associates the procedure body with the
identifier immediately following the symbol <u>procedure</u>. The principal

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part of the procedure declaration is the procedure body. Other parts
of the block in whose heading the procedure is declared can then cause
this procedure body to be executed or evaluated. A proper procedure
is activated by a procedure statement (cf. 7.3.), a function procedure
by a function designator (cf. 6.2.). Associated with the procedure
body is a heading containing the procedure identifier and possibly a
list of formal parameters.

5.3.2.1. Type specification of formal parameters. All formal para-
meters of a formal parameter segment are of the same indicated type.
The type must be such that the replacement of the formal parameter by
the actual parameter of this specified type leads to correct ALGOL W
expressions and statements (cf. 7.3.2.).

5.3.2.2. The effect of the symbols value and result appearing in a
formal type is explained by the following rule, which is applied to
the procedure body before the procedure is invoked:

(1)   The procedure body is enclosed by the symbols begin and end
      if it is not already enclosed by these symbols;

(2) For every formal parameter whose formal type contains the
    symbol value or result (or both),

(a)   a declaration followed by a semicolon is inserted after
      the first begin of the procedure body, with a simple
      type as indicated in the formal type, and with an iden-
      tifier different from any identifier valid at the place
      of the declaration.

(b) throughout the procedure body, every occurrence of the

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formal parameter identifier is replaced by the identifier
defined in step 2a;

(3) If the formal type contains the symbol <u>value,</u> an assignment
statement (cf. 7.2.) followed by a semicolon is inserted
after the declarations of the procedure body. Its left part
contains the identifier defined in step 2a, and its expres-
sion consists of the formal parameter identifier. The sym-
bol <u>value</u> is then deleted;-

(4) If the formal type contains the symbol <u>result,</u> an assignment
statement preceded by a semicolon is inserted before the
symbol <u>end</u> which terminates a proper procedure body. In
the case of a function procedure, an assignment statement
is inserted after the final expres-
sion of the function procedure body. Its left part contains
the formal parameter identifier, and its expression consists
of the identifier defined in step 2a. The symbol <u>result</u> is
then deleted.

5.3.2.3. Specification of array dimensions. The number of "*"'s
appearing in the formal array specification is the dimension of the
array parameter.

5 ● 3.3. Examples

<u>procedure</u> INCREMENT; X := X+1

<u>real procedure</u> MAX (<u>real value</u> X, Y);
    <u>if</u> X < Y <u>then</u> Y <u>else</u> X

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```
procedure COPY (real array U, V (*,*); integer value A, B);
    for I := 1 until A do
    for J := 1 until B do U(I,J) := V(I,J)

real procedure  HORNER (real array A (*); integer value N;
    real value X);
    begin real S; S := 0;
        for I := 0 until N do S := S * X + A(1);
        S
    end

long real procedure SUM (integer K, N; long real X);
    begin long real Y; Y := 0; K := N;
        while K > = 1 dc
        begin Y := Y + X; K := K - 1
        end;
        Y
    end

reference (PERSON) procedure YOUNGESTUNCLE (reference (PERSON) R);
    begin reference  (PERSON) P, M;
        P := YOUNGESTOFFSPRING (FATHER (FATHER (R)));
        while  (P ¬ = null)  and (¬ MALE (P)) or
            (P = FATHER (R))'
            P := ELDERSIBLING (P);
        M := YOUNGESTOFFSPRING (MOTHER (MOTHER (R)));
        while (M ¬ = null)  and (¬ MALE (M)) do
            M := ELDERSIBLING (M);
        if P = null then M else
        if M = null then P else
        if AGE(P) < AGE(M) then P else M
    end
```

5.4. Record Class Declarations

5.4.1. Syntax

```
<record class declaration>  ::=  record <identifier> (<field list>) '
<field list>  ::=  <simple variable declaration> | <field list> ;
                   <simple variable declaration>
```

5.4.2. Semantics

A record class declaration serves to define the structural pro-
perties of records belonging to the class. The principal constituent
of a record class declaration is a sequence of simple variable declara-
tions which define the fields and their simple types for the records
of this class and associate identifiers with the individual fields.
A record class identifier can be used in a record designator (cf. 6.7.)
to construct a new record of the given class.

5.4.3. Examples

```
record NODE (reference (NODE) LEFT, RIGHT)
record PERSON (string NAME; integer AGE; logical MALE;
        reference (PERSON) FATHER, MOTHER,, YOUNGESTOFFFSPRING,
        ELDERSIBLING)
```

6. EXPRESSIONS

Expressions are rules which specify how new values are computed
from existing ones. These new values are obtained by performing the
operations indicated by the operators on the values of the operands.
Several simple types of expressions are distinguished. Their struc-
.ture is defined by the following rules, in which the symbol $\mathcal{T}$ has to

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be replaced consistently as described in Section 1, and where the triplets J_0, J_1, J_2 have to be either all three replaced by the same one of the words

> logical
> bit
> string
> reference

or by any combination of words as indicated by the following table, which yields J_0 given J_1 and J_2:

J_1 \ J_2	integer	real	complex
integer	integer	real	complex
real	real	real	complex
complex	complex	complex	complex

J_0 has the quality "long" if either both J_1 and J_2 have that quality, or if one has the quality and the other is "integer"".

Syntax:

<J expression> ::= <simple J expression> | <case clause
      (<J expression list>)
<J_0 expression> ::= <if clause> <simple J_1 expression> else
      <J_2 expression>
<J expression list> ::= <J expression>
<J_0 expression list> ::= <J_1 expression list> , <J_2 expression>
<if clau ::= if <logical expression> then .
<case clause> ::= case <integer expression> of

The operands are either constants, variables or function designators or other expressions between parentheses, The evaluation of operands other than constants may involve smaller units of action such as the evaluation of other expressions or the execution of statements,,

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The value of an expression between parentheses is obtained by evaluating
that expression. If an operator has two operands, then these operands
may be evaluated in any order with the exception of the logical operators
discussed in 6.4.2.2. The construction

<if clause> <simple $\mathcal{T}_1$ expression> else $\mathcal{T}_2$ expression>

causes the selection and evaluation of an expression on the basis of
the current value of the logical expression contained in the if clause.
If this value is true, the simple expression following the if clause
is selected, if the value is false, the expression following else is
selected. If $\mathcal{T}_1$ and $\mathcal{T}_2$ are simple type string, both string expressions
must have the same length. The construction

<case clause> ($\mathcal{T}$ expression list>)

causes the selection of the expression whose ordinal number in the
expression list is equal to the current value of the integer expression
contained in the case clause. In order that the case expression be
defined, the current value of this expression must be the ordinal number
of some expression in the expression list. If $\mathcal{T}$ is simple type string,
all the string expressions must have the same length.

6.1. Variables

6.1.1. Syntax

<simple $\mathcal{T}$ variable> ::= $\mathcal{T}$ variable identifier> | $\mathcal{T}$ field designator> |
                     $\mathcal{T}$ array designator>
$\mathcal{T}$ variable> ::= <simple $\mathcal{T}$ variable>
<string variable> ::= <substring designator>
$\mathcal{T}$ field designator> ::= $\mathcal{T}$ field identifier> (<reference expression>)
$\mathcal{T}$ array designator> ::= $\mathcal{T}$ array identifier> (<subscript list;>)
<subscript list> ::= <subscript> | <subscript list>, <subscript>
<subscript> ::= <integer expression>

6.1.2. Semantics

An array designator denotes the variable whose indices are the current values of the expressions in the subscript list. The value of each subscript must lie within the declared bounds for that subscript position.

A field designator designates a field in the record referred to by its reference expression. The simple type of the field designator is defined by the declaration of that field identifier in the record class designated by the reference expression of the field designator (cf. 5.4.).

6.1.3. Examples

```
X          A(I)        M(I+J, I-J)
FATHER (JACK)          MOTHER(FATHER(JILL))
```

6.2. Function Designators

6.2.1. Syntax

<J function designator> ::= <J function identifier> | <J function identifier> (<actual parameter list>)

6.2.2. Semantics .

A function designator defines a value which can be obtained by a process performed in the following steps:

Step 1. A copy is made of the body of the function procedure whose procedure identifier is given by the function designator and of the actual parameters of the latter.

Steps 2, 3, 4, As specified in 7.3.2.

Step 5. The copy of the function procedure body, modified as in-
dicated in steps 2-4, is executed, The value of the function
designator is the value of the expression which constitutes or is
part of the modified function procedure body. The simple **type**
of the function designator **is** the simple type in the corresponding
function procedure declaration.

6.2.3. Examples

MAX (X ** 2, Y ** 2)
SUM (I, 100, H(1))
SUM (I, M, SUM (**J, N, A(I,J)**))
YOUNGESTUNCLE (**JILL**)
SUM ((I, 10, x(1) * Y(**I**))
HORNER (X, 10, 2.7)

6.3. Arithmetic Expressions

6.3.1. Syntax

In any of the following rules, every occurrence of the symbol $\mathcal{J}$
must be systematically replaced by one of the following words (or
word **pairs**):

> integer .
> real
> long real
> complex
> long complex

The rules governing the replacement **of** the symbols $\mathcal{J}_0$, $\mathcal{J}_1$ and $\mathcal{J}_2$ are
given in 6.3.2.

<simple $\mathcal{J}$ expression> ::= <$\mathcal{J}$ term> | + <$\mathcal{J}$ term> | - <$\mathcal{J}$ term>

<simple J_0 expression> ::= <simple J_1 expression> + <J_2 term> |

                            <simple J_1 expression> -- <J_2 term>

<J term> ::= <J factor>

<J_0 term> ::= <J_1 term> * <J_2 factor;,"

<J_0 term> ::= <J_1 term> / <J_2 factor>

<integer term> ::= <integer term> div <integer factor> |

                    <integer term> rem <integer factor>

<J_0 factor> ::= <J_0 primary> | <J_1 factor> ** <integer primary>

<J_0 primary> ::= abs <J_1 primary> | abs <J_1 number>

<J_0 primary> ::= long <J_1 primary>

<J_0 primary> ::= short <J_1 primary>

<J primary> ::= <J variable> | <J function designator> |

              (<J expression>) | <J number>

<integer primary> ::= <control identifier>

6.3.2. Semantics

An arithmetic expression is a rule for computing a number.

According to its simple type it is called an integer expression, real expression, long real expression, complex expression, or long complex expression.

6.3.2.1. The operators +, -, *, and / have the conventional meanings of addition, subtraction, multiplication and division. In the relevant syntactic rules of 6.3.1. the symbols J_0, J_1 and J_2 have to be replaced by any combination of words according to the following table which indicates J_0 for any combination of J_1 and J_2.

Operators + | -

J_1 \ J_2	integer	real	complex
integer	integer	real	complex
real	real	real	complex
complex	complex	complex	*complex*

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$\mathcal{T}_0$ has the quality "long" if both $\mathcal{T}_1$ and $\mathcal{T}_2$ have the quality "long", or if one has the quality "long" and the other is "integer".

Operator *

$\mathcal{T}_1$ \ $\mathcal{T}_2$	integer	real	complex
integer	integer	long real	long complex
real	long real	long real	long complex
complex	long complex	long complex	long complex

$\mathcal{T}_1$ or $\mathcal{T}_2$ having the quality "long" does not affect the type of the result.

Operator /

$\mathcal{T}_1$ \ $\mathcal{T}_2$	integer	real	complex
integer	real	real	complex
real	real	real	complex
complex	complex	complex	complex

$\mathcal{T}_0$ has the quality "long" if both $\mathcal{T}_1$ and $\mathcal{T}_2$ have the quality "long", or if one has the quality "long" and the other is "integer".

6.3.2.2. The operator "-" standing as the first symbol of a simple expression denotes the monadic operation of sign inversion. The type of the result is the type of the operand. The operator "+" standing as the first symbol of a simple expression denotes the monadic operation of identity.

6.3.2.3. The operator div is mathematically defined (for $B \neq 0$) as

A div B = SGN (A X B) X D (abs A, abs B)   (cf. 6.3.2.6.)

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where the function procedures SGN and D are **declared** as

> <u>integer procedure</u> SGN (<u>integer value</u> A);
>   <u>if</u> A < 0 <u>then</u> -1 <u>else</u> 1;

> **integer** <u>procedure</u> D (<u>integer</u> <u>value</u> A, B);
>   if A < B <u>then</u> 0 else D(A-B, B) + 1

6.3.2.4. The operator <u>rem</u> (remainder) is mathematically defined as

> A <u>rem</u> B = A - (A <u>div</u> B) X B

6.3a2.5 . The operator ** denotes exponentiation of the first operand
to the power of the second operand. In the relevant syntactic rule of
6.3.1. the symbols T_0 and T_1 are to be replaced by any of the follow-
ing combinations of words:

T_0	T_1
real	integer
real	real
complex	complex

T_0 has the quality "long" if and only if T_1 does,

6.3.2.6. The monadic operator <u>abs</u> yields the absolute value or modulus
of the operand. In the relevant syntactic rule of 6.3.1. the symbols T_0
and T_1 have to be replaced by any of the **following** combinations of words:

T_0	T_1
integer	integer
real	real
real	complex

If T_1 has the quality "long", then so does T_0.

6.3.2.7. Precision of arithmetic. If the **result** of an arithmetic operation is of simple type <u>real</u>, <u>complex_</u>, <u>long real</u>, or <u>long</u> <u>complex</u> then it is the mathematically understood result of the operation performed on operands which may deviate from actual operands.

In the relevant syntactic rules of 6.3.1. the symbols $\mathcal{T}_0$ and $\mathcal{T}_1$ must be replaced by any of the following combinations of words (or word pairs):

Operator <u>long</u>

$\mathcal{T}_0$	$\mathcal{T}_1$
long real	real
long real	integer
long complex	complex

Operator <u>short</u>

$\mathcal{T}_0$	$\mathcal{T}_1$
real	long real
complex	long complex

6.3.3. Examples

C + A(1) * $(I)
EXP(-X/(2 * SIGMA)) / SQRT (2 * SIGMA)

6.4. <u>Logical</u> <u>Expressions</u>

6X.1. Syntax

In the following rules for <relation> the symbols $\mathcal{T}_0$ and $\mathcal{T}_1$ must either be identically replaced by any one of the following words:

bit

string

reference

or by any of the words from:

complex

long complex

real

long real

integer

and the symbols J_2 or J_3 must be identically replaced by string or must be replaced by any of real, long real, integer.

<simple logical expression> ::= <logical element> | <relation>

<logical element> ::= <logical term> | <logical element> or
                      <logical term>

<logical term> ::= <logical factor> | <logical term> and
                   <logical factor>

<logical factor> ::= <logical primary=> | ¬ <logical primary>

<logical primary> ::= <logical value | <logical variable |
                      <logical function designator> |
                      (<logical expression>)

<relation> ::= <simple J_0 expression> <equality operator>
               <simple J_1 expression> | <logical element>
               <equality operator> <logical element> |
               <simple reference expression> is
               <record class identifier> |
               <simple J_2 expression> <relational operator>
               <simple J_3 expression>

<relational operator> ::= < | < = | > = | >

<equality operator> ::= = | ¬ =

6.4.2. Semantics

A logical expression is a rule for computing a logical value.

6.4.2.1. The relational operators represent algebraic ordering for arithmetic arguments and EBCDIC ordering for string arguments. If two strings of unequal length are compared, the shorter string is extended to the right by characters less than any possible string character, The relational operators yield the logical value true if the relation is satisfied for the values of the two operands; false otherwise. Two references are equal if and only if they are both null or both refer to the same record. Two strings are equal if and only if they have the same length and the same ordered-sequence of characters.

6.4.2.2. The operators ¬ (not), and, and or, operating on logical values, are defined by the following equivalences:

          ¬ X   if X then false else true
          X and Y   if X then Y else false
          X or Y if X then true else Y

  6.4.3. Examples

  P or Q
  (X C Y) and (Y C Z)
  YOUNGESTOFFSPRING (JACK) ¬ = null
  FATHER (JILL) is PERSON

6.5. Bit Expressions .

  6.5.1. Syntax

  <simple bit expression> ::= <bit term> | <simple bit expression>
                              or <bit term>
  <bit term> ::= <bit factor> | <bit term> and <bit factor>
  <bit factor> ::= Cbit secondary> | ¬ <bit secondary>
  Cbit secondary> ::= <bit primary> | <bit secondary> shl
                      <integer primary> | <bit secondary> shr
                      <integer primary>
  <bit primary> ::= <bit sequence> | Cbit variable> | <bit
                    function designator> | (<bit expression>)

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6.5.2. Semantics

A bit expression is a rule for computing a bit sequence.

The operators <u>and</u>, or, and ¬ produce a result of type <u>bits</u>, every bit being dependent on the corresponding bits in the operand(s) as follows:

X	Y	¬ X	X <u>and</u> Y	X <u>or</u> Y
0	0	1	0	0 ·
0	1	1	– 0	1
1	0	0	0	1
1	1	0	1	1

The operators <u>shl</u> and <u>shr</u> denote the shifting operation to the left and to the right respectively by the number of bit positions indicated by the absolute value of the integer primary. Vacated bit, positions to the right or left respectively are assigned the bit value O.

6.5.3. Examples

G <u>and</u> H <u>or</u> #38
G <u>and</u> ¬ (H <u>or</u> G) <u>shr</u> 8.

6.6. String Expressions

6.6.1. Syntax

<simple string expression> ::= <string primary>
<string primary> ::= <string> | <string variable> | <string
                    function designator> | (<string expression>)
<substring designator> ::= <simple string variable>
                          (<integer expression ▮ <integer number>)

6.6.2. Semantics

A string expression is a rule for computing a string (sequence of characters).

6.6.2.1. A substring designator denotes a sequence of characters of the string designated by the string variable. The integer expression preceding the █ selects the starting character of the sequence. The value of the expression indicates the position in the string variable. 'The value must be greater than or equal to 0 and less than the declared length of the string variable. The first character of the string has position 0. The integer number following the █ indicates the length of the selected sequence and is the length of the string expression. The sum of the integer expression and the integer number must be less than or equal to the declared length of the string variable.

6.6.3. Example

<u>string</u> (10) S;
S (4█3)
S (I+J█1)

<u>string</u> (10) array T (1::m,2::n);
    T (4,6)(3█ 5)

6.7. <u>Reference Expressions</u>

6.7.1. Syntax

<simple reference expression> ::= <null reference', | <reference variable> | <reference function designator> | <record designator> | (<reference expression>)

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```
<record designator>  ::=  <record class identifier> ¦ <record
                           class identifier> (<expression list>]
<expression list> ::=  <J expression> | <expression list>,
                           <J expression>
```

6.7.2. Semantics

A reference expression is a rule for computing a reference to a record. All simple reference expressions in a reference expression must be of the same record class.

The value of a record designator is the reference to a newly created record belonging to the designated record class. If the record designator contains an expression list, then the values of the expressions are assigned to the fields of the new record. The entries in the expression list are taken in the same order as the fields in the record class declaration, and the simple types of the fields must be assignment compatible with the simple types of the expressions (cf. 7.2.2.).

6.7.3. Example

```
PERSON ("CAROL", 0, false, JACK, JILL, null, YOUNGESTOFFSPRING
       ( Ja cK))    .
```

6.8. Precedence of Operators

The syntax of 6.3.1., 6.4.1., and 6.5.1. implies the following hierarchy of operator precedences:

```
            long , short, abs
            shl, shr, **
                 ¬
            *, /, div, rem, and
```

$$+, -, \text{ or}$$
$$<, \leq, =, \neg =, \geq, >, \text{ is}$$

Example

A = B and C   is equivalent to   A = (B and C)

7. STATEMENTS

A statement denotes a unit of action. By the execution of a statement is meant the performance of this unit of action, which may consist of smaller units of action such as the evaluation of expressions or the execution of other statements.

Syntax:

```
<program>  ::=  <block> .
<statement> ::=  <simple statement> | <iterative statement> |
                <if statement> | <case statement>
<simple statement>  ::=  <block> | <assignment statement> |
                <empty> | <procedure statement> |
                <goto statement>
```

7.1. Blocks

7.1.1. Syntax

```
<block>  ::=  <block body> <statement> end
<block-body> ::= <block head> | <block body> <statement>; |
                <block body> <label definition>
<block head> ::=  begin | <block head> <declaration> ;
<label definition>  ::=  <identifier> :
```

7.1.2. Semantics

Every block introduces a new level of nomenclature. This is realized by execution of the block in the following steps:

Step 1. If an identifier, say A, defined in the block head or in
a label definition of the block body is already defined at the
place from which the block is entered, then every occurrence of
that identifier, **A,** within the block except **for** occurrence in
array bound expressions is systematically replaced by another
identifier, say **APRIME,** which is defined neither within the
block nor at the place from which the block is entered.

Step 2. If the declarations of the block contain array bound
expressions, then these expressions are evaluated,

Step 3. Execution of the statements contained in the block body
begins with the execution of the first statement following the
block head.

After execution of the last statement of the block body (unless
it is a goto statement) a block exit occurs, and the statement follow-
ing the entire block is executed.

7.1.3. Example

begin real U;
      u := X; X := Y; Y := Z; Z := u
end

7.2. Assignment Statements

7.2.1. Syntax

In the following rules the symbols J_0 and J_1 must be replaced by
words as indicated in Section 1, subject to the restriction that the
type J_0 is assignment compatible with the type J_1 as defined in 7.2.2.

$\langle T_0$ assignment statement$\rangle$ ::= $\langle T_0$ left part$\rangle$ $\langle T_1$ expression$\rangle$ |
                              $\langle T_0$ left par-D $\langle T_1$ assignment
                              statement$\rangle$

$\langle T$ left part$\rangle$ ::= $\langle T$ variable$\rangle$:=

7.2.2.   Semantics

The execution of a simple assignment statement

$\langle T_0$ assignment statement$\rangle$ ::= $\langle T_0$ left part$\rangle$ $\langle T_1$ expression$\rangle$

causes the assignment of the value of the expression to the variable.
If a shorter string is to be assigned to a longer one, the shorter
string is first extended to the right with blanks until the lengths are
equal. In a multiple assignment statement

$(\langle T_0$ assignment statement$\rangle$:= $\langle T_0$ left part$\rangle$ $\langle T_1$ assignment
                                        statement$\rangle)$

the assignments are performed from right to left. The simple type of
each left part variable must be assignment compatible with the simple
type of the expression or assignment variable immediately to the right.

A simple type T_0 is said to be assignment compatible with a simple
type T_1 if either

   (1) the two types are identical (except that if T_0 and T_1 are
       <u>string</u>, the length of the T_0 variable must be greater than
       or equal to the length of the T_1 expression or assignment), or
   (2) T_0 is real or <u>long</u> <u>real</u>, and T_1 is <u>integer</u>, real or <u>long</u>
       <u>real</u> r
   (3) T_0 is <u>complex</u> or long complex, and T_1 is <u>integer</u>, <u>real</u>,
       <u>long real</u>, <u>complex</u> or <u>long</u> <u>complex</u>.

In the case of a reference, the reference to be assigned must refer
to a record of the class specified by the record class identifier asso-
ciated with the reference variable in its declaration.

7.2.3. Examples

```
Z := AGE(JACK) :=28
X := Y + abs Z
C := I + X + C
P := X ¬ = Y
```

7.3. Procedure Statements

7.3.1. Syntax

<procedure statement> ::= <procedure identifier> | <procedure
identifier> (<actual parameter list>)

<actual parameter list> ::= <actual parameter> | <actual para-
meter list> , <actual parameter>

<actual parameter> ::= <J expression> | <statement> | <J subarray
designator> | <procedure identifier> |
<J function identifier9

<J subarray designator:> ::= <J array identifier> | <J array
identifier> (<subarray designator
list>)

<subarray designator list> ::= <subscript> | * | Csubarray
designator list>,<subscript> |
<subarray designator list>,*

7.3.2. Semantics

The execution of a procedure statement is equivaient to a process
performed in the following steps:

Step 1. A copy is made of the body of the proper procedure whose
procedure identifier is given by the procedure statement, and of
the actual parameters of the latter.

Step 2. If the procedure body is a block, then a systematic
change of identifiers in its copy is performed as specified by

step 1 of 7.1.2.

Step 3. The copies of the actual parameters are treated in an undefined order as follows: If the copy is an expression different from a variable, then it is enclosed by a pair of parentheses, or if it is a statement it is enclosed by the symbols begin and end.

Step 4. In the copy of the procedure body every occurrence of an identifier identifying a formal parameter is replaced by the copy of the corresponding actual parameter (cf. 7.3.2.1.). In order for the process to be defined, these replacements must lead to correct ALGOL W expressions and statements.

Step 5. The copy of the procedure body, modified as indicated in steps 2-4, is executed.

7.3.2.1. Actual·formal correspondence. The correspondence between the actual parameters and the formal parameters is established as follows: The actual parameter list of the procedure statement (or of the function designator) must have the same number of entries as the formal parameter list of the procedure declaration heading. The correspondence is obtained by taking the entries of these two lists in the same order.

7.3.2.2. Formal specifications. If a'formal parameter is specified by value, then the formal type must be assignment compatible with the type of the actual parameter. If it is specified as result, then the type of the actual parameter must be assignment compatible with the

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formal type. In all other cases, the types must be identical. If an
actual parameter is a statement, then the specification of its corre-
sponding formal parameter must be procedure.

7.3.2.3. Subarray designators. A complete array may be passed to a
procedure by specifying the name of the array if the number of sub-
scripts of the actual parameter equals the number of subscripts of
the corresponding formal parameter. If the actual array parameter has
more subscripts than the corresponding formal parameter, enough sub-
scripts must be specified by integer -expressions so that the number of
*'s appearing in the subarray designator equals the number of sub-
scripts of the corresponding formal parameter. The subscript positions
of the formal array designator are matched with the positions with *'s
in the subarray designator in the order they appear.

7.3.3. Examples

```
INCREMENT
COPY (A, B, M, N)
INNERPRODUCT (I, N, A(I,*), B(*,J))
```

7.4. Goto Statements

7.4.1. Syntax

<goto statement> ::= goto <label identifier> | go to <label
                      identifier>

7.4.2. Semantics

An identifier is called a label identifier if it stands as a
label.

A goto statement determines that execution of the text be continued after the label definition of the label identifier. The identification of that label definition is accomplished in the following steps:

Step 1. If some label definition within the most recently activated but not yet terminated block contains the label identifier, then this is the designated label definition. Otherwise,

Step 2. The execution of that block is considered as terminated and Step 1 is taken as specified above.

7.5. If Statements

7.5.1. Syntax

<if statement)- : := <if clause> <statement> | <if clause>
                    <simple statement> else <statement>
<if clause> ::= if <logical expression> then

7.5.2. Semantics

The execution of if statements causes certain statements to be . executed or skipped depending on the values of specified logical expressions. An if statement. of the form

    <if clause> <statement)

is executed in the following steps:

-Step 1. The logical expression in the if clause is evaluated.

Step 2. If the result of Step 1 is true, then the statement following the if clause is executed. Otherwise step 2 causes no action to be taken at all.

An if statement of the form

<if clause> <simple statement> else <statement>

is executed in the following steps:

Step 1. The logical expression in the if clause is evaluated.

Step 2. If the result of step 1 is _true_, then the **simple** statement following the if clause is executed. Otherwise the statement following else is executed.

7.5.3. Examples

if X = Y then goto L
ifX< Y then U :=X else if Y < Z then U := Y else V := Z

7.6. Case Statements

7.6.1. Syntax

<case statement> ::= <case clause> begin <statement list> end
<statement list> ::= <statement> | <statement list> ; <statement>
<case clause> ::= case <integer expression> of

7.6.2. Semantics

The execution of a case statement proceeds in the following steps:

Step 1. The expression of the case clause is evaluated.

Step 2. The statement whose ordinal number in the statement list is equal to the value obtained in Step 1 is executed. In order that the case statement be defined, the current value of the expression in the case clause must be the ordinal number of some

statement of the statement list.

7.6.3. Examples

<u>case</u> I <u>of</u>
<u>begin</u> X := X + Y;
     Y := Y + Z;
     Z := Z + X
<u>end</u>

<u>case</u> j <u>of</u>
<u>begin</u> H(1) := -H(I);
    <u>begin</u> H(I-1) := H(I-1) + H(I); I := I-1 end;
    <u>begin</u> H(I-1) := K(I-1) x H(I); I := I-1 <u>end</u>;
    <u>begin</u> H(H(I-1)) := H(I); I := I-2 <u>end</u>
<u>end</u>

7.7. <u>Iterative Statements</u>

7.7.1. Syntax

<iterative statement> ::= <for clause> <statement> | <while
                     clause> <statement>
<for clause> ::= <u>for</u> <identifier> := <initial value>
         <u>step</u> <increment> <u>until</u> <limit> <u>do</u> | <u>for</u>
         <identifier> := <initial value> <u>until</u> <limit>
         <u>do</u> | <u>for</u> <identifier> := <for list> <u>do</u>
<for list> ::= <integer expression> | <for list> , <integer
       expression>
<initial value> ::= <integer expression>
<increment> ::= <integer expression>
<limit> ::= <integer expression>
<while clause> ::= <u>while</u> <logical expression> <u>do</u>

7.7.2. Semantics

The iterative statement serves to express that a statement be

executed repeatedly depending on certain conditions specified by a
for clause or a while clause.   The statement following the for clause
or the while clause always acts as a block, whether it has the form of
a block or not.   The value of the control identifier (the identifier
following _for_) cannot be changed by assignment within the controlled
statement.

(a) An iterative statement of the form

> _for_ <identifier> :=El_step_ E2 un_til_ E3 _do_ <statement>

is exactly equivalent to the block

> _begin_ <statement-O>; <statement-P ... ; <statement-L>;
>   . . .; <statement-N> _end_

in the Ith statement every occurrence of the control identifier
is replaced by the value of the expression (El + I X E2).

The index N of the last statement is determined by
$N < (E3-El) / E2 < N+1$.   If N < 0, then it is understood that
the sequence is empty. The expressions El, E2, and E3 are
evaluated exactly once , namely before execution of <statement-O).
Therefore they can not depend on the control identifier.

(b) An iterative statement of the form

> _for_ <identifier> := El _until_ E3 _do_ <statement>

is exactly equivalent to the iterative statement

> _for_ <identifier> := El _step_ 1 _until_ E3 _do_ <statement>

(c) An iterative statement of the form

> _for_ <identifier> := El, E2, ... , EN _do_ <statement>

is exactly equivalent to the block

```
          begin <statement-D; <statement-a ... <statement-I> ; ...
          <statement-N> end
```

when in the Ith statement every occurrence of the control identifier

is replaced by the value of the expression EI.

(d) An iterative statement of the form

```
     while E do <statement>
```

is exactly equivalent to

```
     begin
L:        if E then
          begin <statement> ; goto L end
     end
```

7 • 7.3. **Examples**

```
for V := 1 step 1 until N-1 do S := S + A(U,V)
while (J > 0) and (CIT₁(J) ¬ = S)do J := J-1
for I := x, x + 1, x + 3, X + 7 do P(I)
```

7.8. Standard Procedures

The standard procedures differ from explicitly declared procedures
in that they may have one or more parameters of mixed simple type.
In the following descriptions $\mathcal{J}$ is to be replaced by any one of

integer	bit
real	string
long real	
complex	
long complex	

7.8.1. Read Statements

Implicit declaration heading:

> procedure   read ($\mathcal{T}$ result X_1, $\mathcal{T}$ result X_2 . . . , $\mathcal{T}$ result X_n);
>
> procedure read on ($\mathcal{T}$ result X_1, $\mathcal{T}$ result X_2 . . . , $\mathcal{T}$ result X_n);
>
> (where $n \geq 1$)

Both read and readon designate free field read statements. The quantities on the data cards must be separated by one or more blank columns . All 80 card columns can be used and quantities extending to column 80 on one card can be continued beginning in column 1 of the next card. In addition to the numbers of 4.1., numbers of the following syntactic forms are acceptable quantities on the data cards:

1)   <sign> <$\mathcal{T}$ number>

> where $\mathcal{T}$ is one of integer, real, long real, complex, long complex.

2)   <sign> <$\mathcal{T}_0$ number> <sign> <$\mathcal{T}_1$ number>

> where $\mathcal{T}_0$ is one of integer, real, long real, and $\mathcal{T}_1$ is one of complex, long complex.

The quantities on the data cards are matched with the variables of the variable list in order of appearance. The simple type of each quantity read must be assignment compatible with the simple type of the variable designated. The read statement begins scanning for the data on the next card. The readon statement begins scanning for the data where the last read or readon statement finished.

7.8.1.2. Examples

    read (X,A(I))
    for I := 1 until N do readon (A(I))

7.8.2. Write Statements

Implicit declaration heading:

$$\underline{procedure}\ write\ (\mathcal{T}\ \underline{value}\ X_1,\ \mathcal{T}\ \underline{value}\ X_2, \ldots ,\ \mathcal{T}\ \underline{value}\ X_n);$$

$$(where\ n \geq 1);$$

The values of the variables are output in the order they appear

in the variable list in a free field form described below. The first
field of each WRITE statement begins on a new line. If there is insuffi-
cicnt space remaining on the 132 character print line for a new field,
that line is printed and the new-field starts at the beginning of a new
print line.

<u>integer</u>: right justified in field of 14 characters followed by 2
          blanks. Field size can be changed by assignment to Intfieldsize.

<u>real</u>: same as <u>integer</u> except the field size cannot be changed.

<u>long real</u>: right justified in field of 22 characters followed
            by 2 blanks.

<u>complex</u>: two adjacent <u>real</u> fields always on the same line.

<u>long complex</u>: two <u>long real</u> fields adjacent always on the same
              line.

<u>logical</u>: TRUE or FALSE right justified in a field of 6 characters
            followed by 2 blanks.

<u>string</u>: placed in a field large enough to contain the string
          and may extend to a new line if the string is larger
          than 132 characters.

<u>bits</u>: same as <u>real</u>.

<u>reference</u>: same as <u>real</u>.

8. STANDARD FUNCTIONS AND PREDECLARED IDENTIFIERS .

8.1. Standard Transfer Functions

Implicit declaration headings:

```
integer procedure round (real value X);

integer procedure truncate (real value X);

integer procedure entier (real value X);

real procedure realpart (complex value X);

long real procedure.longrealpart (long complex value X);

real procedure imagpart (complex value X);

long real procedure longimagpart (long complex value X);

complex procedure imag (real value X);

     comment complex number XI;

long complex procedure longimag (long real value X);

logical procedure odd (integer-value X);

bits procedure bitstring (integer value X);

     comment binary representation of number X;

integer procedure number (bits value X);

     comment integer with binary representation X;

integer procedure decode (string (1) value S);

     comment numeric code of the character S;

string (1) procedure code (integer value X);

     comment character whose numeric code is X REM 256;
```

8.2. Standard Functions of Analysis

```
real procedure sin (real value X);

long real procedure longsin (long real value X);

real procedure cos (real value X);

long real procedure' longcos (long real value X);

real procedure arctan (real value X);

     comment -π/2 < arctan (X) < π/2;

long real procedure longarctan (long real value X);

     comment -π/2 < longarctan (X) < π/2;

real procedure ln (real value X);

     comment logarithm base e;

long real procedure longln (long real value X);

     comment logarithm base e;
```

<u>real</u> <u>procedure</u> log (real value X);

    <u>comment</u> logarithm base 10;

<u>long</u> <u>real procedure</u> longlog (<u>long real</u> value X);

    <u>comment</u> logarithm base 10;

<u>real</u> <u>procedure</u> exp (real value X);

<u>long</u> <u>real procedure</u> longexp (<u>long</u> real value X);

<u>real</u> <u>procedure</u> sqrt (real value X);

<u>long</u> <u>real</u> <u>procedure</u> longsqrt (<u>long</u> real value X);

<u>complex procedure</u> complexsqrt (<u>complex value</u> X);

    <u>comment</u> principal square root;

<u>long complex procedure</u> longcomplexsqrt (<u>long complex value</u> X);

    <u>comment</u> principal square root;

8.3. <u>Overflow and Underflow</u>

8.3.1. Predeclared Variables

<u>logical</u> underflow;

    <u>comment</u> initialized to <u>false</u>. Set to <u>true</u> at occurrence

    of a floating-point,-underflow interrupt;

<u>logical</u> overflow;

    <u>comment</u> initialized to <u>false</u>. Set to <u>true</u> at occurrence

    of a floating-point or fixed-point overflow or divide-by?
zero interrupt;

8.3.2. Standard Message Function

<u>integer procedure</u> msglevel (<u>integer value</u> X);

    <u>comment</u> The value of a system integer variable MSG controls

    the number of underflow/overflow messages printed during

    program execution. MSG is initialized to zero.

        <u>MSG = 0</u>
        No messages are printed.

MSG > 0

Underflow and overflow messages are printed.
After each message is printed, MSG is decreased by 1.

MSG < 0

Overflow messages are printed. After each message
is printed, MSG is increased by 1.

Each message gives the type of interrupt and a source card number
near which the interrupt occurred.

Examples

OVERFLOW NEAR CARD 0023
UNDERFLOW NEAR CARD 0071
DIV BY ZERO NEAR CARD 0372

The predeclared integer procedure msglevel is used to interro-
gate and to set the value of MSG. The old value of MSG is the value
of the procedure msglevel, and the new value given to MSG is the
value of the argument of msglevel.

8.4. Output Field Sizes

integer intfieldsize;

comment indicates number of digits including minus sign if

any. Initialized to 14; can be changed by assignment state-

ment;

8.5. Time Function

integer procedure time (integer value X);

comment if X = 1, time is returned in 60^{th}s of a second,

If X = 2, time is printed in minutes, seconds and 60^{th}s of

a second and returned in 60^{th}s of a second.

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ALGOL W

ERROR MESSAGES

by

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ALGOL W ERROR MESSAGES

I.   PASS ONE MESSAGES

All Pass One messages appear on the first page following the program listing.   The message format is

CARD NO.   (number) -- (message)

The (number) corresponds to the card number on which the error was found.   The (message) is one of-those listed below:

INCORRECT SPECIFTN	syntactic entity of a declaration is incorrect, e.g. variable string length.
INCORRECT CONSTANT	syntax error in number or bitstring.
MISSING END	an END needed to close block.
MISSING BEGIN	an attempt to close outer block before end of code.
MISSING)	) is needed.
ILLEGAL CHARACTER	a character, not in a string, is unrecognizable.
MISSING END .	program must conclude with the sequence END .
STRING LENGTH ERROR	string is of 0 length or length greater than 256.
BITS LENGTH ERROR	bits constant denotes no bits or more than 32 bits.
MISSING (	(is needed.
COMPILER TABLE OVERFLOW	terminating error — a compile time table has exceeded its bounds.

1

TOO MANY ERRORS   the maximum number of errors for Pass
                                         One records has been reached. Com-
                                         pilation continues but messages for
                                         succeeding errors detected by Pass
                                         One are suppressed.

ID LENGTH >256   more than 256 characters in' identifier.
See also discussion of PROGRAM CHECK in IV.

II.   PASS TWO MESSAGES

      The format of Pass Two error messages is

      (message), CARD NUMBER IS (number). CURRENT SYMBOL IS (incoming
            symbol)

      If a $STACK card is included anywhere in the source deck, the
SYNTAX ERROR message is followed by

      STACK CONTAINS:
            .   (beginning of file)
            <symbol-1>
            :
            <symbol-m (top of stack)

  - The symbol names may differ-somewhat from the metasymbols of
the syntax.

      If any Pass One or Pass Two errors occur, compilation is termi-
nated at the end of Pass Two.

INCORRECT SIMPLE TYPE <number>   <simple type> of entity is improper
                                  as used. Number indicates explana-
                                  tion on list of simple type errors.

2

ARRAY USED INCORRECTLY	a variable must be used here.
IDENTIFIER MUST BE RECORD CLASS ID	reference declaration is incorrect,
MISMATCHED PARAMETER	formal parameter does not correspond to actual parameter.
MULTIPLY-DEFINED SYMBOL <identifier>	symbol defined more than , once in a block.
UNDEFINED SYMBOL <identifier9	symbol is not declared or defined,
INCORRECT NUMBER OF ACTUAL PARAMETERS	the number of actual parameters to a procedure does, not equal the number of formal parameters declared for the procedure.
INCORRECT DIMENSION	the array has appeared previously with a different/number of dimensions..
DATA AREA EXCEEDED	too many declarations in the block.
INCORRECT NUMBER OF FIELDS	the number of fields specified in a record designator doe's not equal the number of fields the declaration of the record indicates.
INCOMPATIBLE STRING LENGTH	length of assigned string is greater than length of string assigned to.
INCOMPATIBLE REFERENCES	record class bindings are inconsistent.
BLOCKS NESTED TOO DEEP	blocks are nested more than 8 levels.
-REFERENCE MUST REFER TO RECORD CLASS	reference must be bound to a record class.
EXPRESSION MISSING IN PROCEDURE BODY	body of typed procedure must end with. an expression.

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RESULT PARAMETER MUST BE <T VAR> the actual parameter corresponding
to a result formal parameter must
be a <J VARIABLE>.

PROCEDURE HEW LACKS SIMPLE TYPE proper procedure ends with an ex-
pression.

<SYMBOL-1> UNRELATED TO <SYMBOL-a the symbol at the top of the stack
(<SYMBOL-I>) should not be followed
by the incoming symbol (<SYMBOL-&).

SYNTAX ERROR   construction violates the rules of
the grammar. The input string is
skipped until the next END, ";",
BEGIN, or the end of the program.
More than one error message may be
generated for a single syntax error.

Simple Type Errors

25. Upper and lower bounds must be integer.
29. Upper and lower bounds must be integer.
32. Simple type of procedure and simple type of expression in pro-
cedure body do not agree.
71. Substring index must be integer.
73. Variable before '(' must be string, procedure identifier, or array
identifier.   .
74. Substring length must be integer.
76. Field index must be reference or record class identifier.
77. Array subscript must be integer.
81. Array subscript must be integer.
84. Actual parameters and formal parameters do not agree.
88. Actual parameters and formal parameters do not agree.
93. Expressions in if expression do not agree.
94. Expressions in case expression do not agree.
95. Expression in if clause must be logical.

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98. Expressions in case expression do not agree,

99. Expression in case clause must be integer.

101. Arguments of = or ¬= do not agree.

102. Arguments of relational operators must be integer, real, or
     long real.

103. Argument before is must be reference.

106. Argument of unary + must be arithmetic.

107. Argument of unary - must be arithmetic.

108. Arguments of + must be arithmetic.

109. Arguments of - must be arithmetic.

110. Arguments of or must be both logical or both bits.

112. Record field must be assignment compatible with declaration.

117. Arguments of * must be arithmetic.

118. Arguments of / must be arithmetic.

119. Arguments of div must be integer.

120. Arguments of rem must be integer.

121. Arguments of and must be both logical or both bits.

123. Argument of ¬ must be logical or bits.

125. Exponent or shift quantity must be integer: expression to be
     shifted must be bits.

126. Shift quantity must be integer; expression to be shifted must be
     bits.

130. Actual parameter of standard function has incorrect simple type.

134. Argument of long must be integer, real, or complex.

135. Argument of short must be long real or long complex.

136. Argument of abs must be arithmetic.

148. Record field must be assignment compatible with declaration.

181. Expression cannot be assigned to variable.

182. Result of assignment cannot be assigned to variable.

188. Limit expression in for clause must be integer.

190. Expression in for list must be integer.

191. Assignment to for variable must be integer.

193. Expression in for list must be integer.

195. Step element must be integer.

197. Expression in while clause must be logical.

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III. PASS THREE ERROR MESSAGES

The form of Pass Three error messages is

***** (message)
***** NEAR CARD (number)

The number indicates the number of the card near which the error occurred. The message may be

PROGRAM SEGMENT OVERFLOW   the amount of code-generated for a procedure exceeds 4096 bytes.

COMPILER STACK OVERFLOW   constructs nested too deeply,

CONSTANT POINTER TABLE TOO LARGE too many literals appear in a pro-cedure.

BLOCKS NESTED TOO DEEP   parameters in procedure call are nested, too deeply; procedure calls in 'block nested too deeply.

DATA SEGMENT OVERFLOW   too many variables declared in the block.

IV. RUN TIME ERROR MESSAGES

The form of run error messages is

RUN ERROR NEAR CARD (number) - (message)

SUBSTRING INDEXING   sub&ring selected not within named string.

CASE SELECTION INDEXING   index of case statement or case ex-pression is less than 1 or greater than number of cases.

ARRAY SUBSCRIPTING   array subscript not within de&red bounds.

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LOWER BOUND > UPPER BOUND

lower bound is greater than upper bound in array declaration.

ARRAY TOO LARGE

The (n-l) dimensional array obtained by deleting the right-most bound-pair of the array being declared has too many elements The maximum number of elements allowed in this (n-l) dimensional array is given below, according to the declared type of the array.

type	maximum # of elements in first (n-l) dimensions
logical, string	32767
integer, real	8191
bits, reference	8191
long real, complex	4095
long complex	2047

ASSIGNMENT TO NAME PARAMETER

assignment to a formal name parameter whose corresponding actual parameter is an expression, a literal, control identifier,? or procedure name.

DATA AREA OVERFLOW

storage available for program execution has been exceeded.

ACTUAL-FORMAL PARAMETER MISMATCH IN FORMAL PROCEDURE CALL

the number of actual parameters in a formal procedure call is different from the number of formal parameters in the called procedure, or the parameters are not assignment compatible.

RECORD STORAGE AREA OVERFLOW

no more storage exists for records.

LENGTH OF STRING INPUT	string read is not assignment compatible with corresponding declared string.
LOGICAL INPUT	quantity corresponding to logical quantity is not true or false.
NUMERICAL INPUT	numerical input not assignment compatible with specified quantity.
REFERENCE INPUT	reference quantities cannot be read.
READER EOF	a system control card has been encountered during a read request.
REFERENCE	the null reference has been used to address a record, or a reference bound to two or more record classes was used to address a record class to which it was not currently pointing.
I/O ERROR	see consultant
LINE ESTIMATE EXCEEDED	line estimate on %ALGOL card is exceeded.
TIME: ESTIMATE EXCEEDED	time estimate on %ALGOL card is exceeded.

Counts of certain exceptional conditions detected during program compilation *or* execution are maintained. If any of these are non-zero, they are listed after the post-compilation or post-execution elapsed time message in the following format:

nnnn PROGRAM CHECK NO xx

The number of times the condition was detected (module 10000) is given by nnnn; the nature of the condition is indicated by xx according to the following table:

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08	integer overflow
09	integer division by zero
12	real exponent overflow
13	real exponent underflow
15	real division by zero

This counting is not affected by the value of MSG.

V.   OTHER

PRG PSW (16 hexidecimal digits) compiler error, see consultant

ALGOL W NOTES

FOR INTRODUCTORY

COMPUTER SCIENCE COURSES

by

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Introduction

The textbook _Introduction to ALGOL_ by Baumann, Feliciano, Bauer, and Samelson describes the internationally recognized language ALGOL 60 for algorithm communication. ALGOL W can be viewed as an extension of ALGOL.

Part I of these notes describes the differences between similar constructs of the two languages.

For clarity, Part I is numbered according to the sections of the textbook. In general only differences are mentioned; items which are the same in both languages are usually not discussed.

Part II presents some of the details concerning the new features of ALGOL W. A complete syntactic and semantic description of these constructs as well as of all others in the language is available in "ALGOL W Language Description".

CONTENTS

PART I: Differencea between ALGOL 60 and ALGOL W

1 .   Basic Symbols of the Language

1.1.   The basic symbols

1.1.1.   Letters

Only tipper case letters are used.

1.1.3.   Other   symbols

The following are the same in ALGOL 60 and ALGOL W.

+ - / . ,

:= ;

( ) ¬

= < >

The following are different in the two languages. The correspondence between the symbols is shown in the following table:

ALGOL 60	ALGOL W
10	'
X	*
↑	**
[	(
]	)
' '	"
÷	DIV
≡	=
⊃	no equivalent
V	OR

ALGOL 60	ALGOL W
$\wedge$	AND
$\sqcup$	one blank space
$\neq$	$\neg =$
$<$	$< =$
$>$	$> =$
:	: or :: (cf. section 6.1 and 4.2.1)
no equivalent	I #

All characters indicated for ALGOL W are on the IBM 029 key-punch,

The significance of spaces in ALGOLW will be discussed in subsequent sections.

1.2, Numbers

A number is represented in its most general form with'a scale factor to the base 10 as in c nventional scientific notation.

EXAMPLE $3.164981'-4$ means 3.164981×10^{-4}

This is often called the floating point form,   Certain abbreviations omitting unessential parts are permissible.

EXAMPLES

77	317.092	126'04
551	.5384	04.719'2
'30	0.710	9.123'+1
'-7	0	2'-6
'-3	009.123'+01	2.0'-06

To represent a long floating point (cf. Section 2.3.1) number an

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EXAMPLES   77L   317.092L   126'04L

In ALGOL W, complex numbers (short and long forms) may be used. The imaginary part of a complex number is written as an unsigned real number followed by an I.

EXAMPLES   4I   4.8I   4'-5I

Long imaginary numbers are followed by an L.

EXAMPLE   4.8IL

Numbers may be written in a variety of equivalent forms.

EXAMPLE   12'04   ≡   .12'6   ≡   1.2'05   ≡   120000.0

No spaces may appear within an unsigned number. The magnitude of an integer or the integer part before the decimal point in a floating point number must be less than or equal to 2147483647. The magnitude of a non-zero floating point r-umber must be between approximately 5.4×10^{-79} and 7×10^{75} ($1/16 \times 16^{-64}$ and $(1-16^{-6}) \times 16^{63}$).

1.3. Identifiers

A -letter followed by a sequence of letters and/or digits constitutes an identifier, Identifiers may be as short, as one letter or as long as 256 letters and digits.

Identifiers may be chosen freely and have no inherent meaning. However, ALGOL W recognizes a set of reserved words which must not be used as identifiers.

RESERVED WORDS

ABS	GOTO	REM
AND	GO TO	RESULT
ARRAY	IF	SHL
BEGIN	INTEGER	SHORT
BITS	IS	SHR
CASE	LOGICAL	STEP
COMMENT	LONG	STRING
COMPLEX	NULL	THEN
DIV	OF	TRUE
DO	OR	UNTIL
ELSE	PROCEDURE	VALUE
END	REAL	WHILE
FALSE	RECORD	
FOR	REFERENCE	

The reserved word BOOLEAN can be used in place of LOGICAL. Spaces are used to separate reserved words and identifiers from each other and from numbers.

Certain identifiers are predefined for use by the programmer but are not reserved words. Their meaning will be discussed later. Among these are three input and output identifiera: READ, READON, WRITE, (See Sections 2.2.2. and 2.5.)

1.4 Nonarithmetic symbols

The symbols which are printed in bold type in the text are usually underlined in typewritten copy. They are contained in the list of reserved words (cf. Section 1.3) for ALGOL W. They are not distinguished

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in any other way but they must not be used for any purpose other than
that for which they are specifically intended. The symbol **END,** for
example, must not be used **as an** identifier.

2. <u>Arithmetic Expressions</u>

2.1. <u>Numerical Expressions</u>

The basic arithmetic **operators** of AIGOL W are

> + - * / ** DIV REM

EXAMPLES

3.1459.   7 DIV 3

(3.47'-4 + 9.01'+1) / 4   17 REM 12

9 * 8 * 7 / (1 * 2 * 3)   -1.2

(9 + 2.7) / (-3)

(((1.5 * 3 - 4) * 3 + 0.19'1) * 3 - 2.6'3) * 3

10 + 1.4 / (1 + 0.9 / (7 - 0.4 / 3))

The symbol * denotes multiplication while ** denotes exponentiation.
For instance, 4.5 ** 3 means 4.5^3. The exponent must **always** be **an**
integer in **AIGOL** W. An integer to any exponent gives a real result.

EXAMPLES

> AIGOL W form   Conventional form
>
> 4.1 - 3 ** 2 $4.1 - 3^2$
>
> (4.1 - 3) ** 2 $(4.1 - 3)^2$
>
> 3.2 ** 2 + 5.2 $3.2^2 + 5.2$
>
> -4 ** 2 -4^2

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ALGOL W form	Conventional form

$$(-4) ** 2 \qquad\qquad (-4)^2$$

$$4 * 5 / 2 ** 3 \qquad\qquad \frac{4 \times 5}{2^3}$$

$$5 ** 2 * 3 \qquad\qquad 5^2 \cdot 3$$

Also notice

$$2**3**4 \quad \equiv \quad (2^3)^4$$

In ALGOL W the following two constructs are not allowed because the exponent is a real number:

$$3.2**(2 +5.2) \quad \text{and} \quad 2**(3**4).$$

2.2.2. <u>Assignment of numerical values through input</u>

If the value of an identifier is to be provided by input it is assumed that this value appears on a data card which is in the card reader waiting to be read.   The statement

READØN   (V)

where **V** stands for variable identifier, reads the next number on the current input card,   If there are no more numbers on the current input card, s-ubsequent cards are read until a number is found.   This statement assigns the value of the number to the variable whose name is specified.

$$READØN(V_1, V_2, \ldots, V_n)$$

is equivalent to

$$READØN (V_1); \ READØN (V_2); \ldots; \ READØN (V_n)$$

The constants on the data cards are assigned in the same order as

the **variable** names in the READ∅N statement, One or **several** numbers **may appear** on a single **card separated** by one or more blank spaces with column 80 of one card immediately followed by column 1 of the succeeding card,

The statement

READ (V)

is similar to READ∅N (V) except that scanning for the number begins on a new input card.

The statement

$$\text{READ } (V_1, V_2, V_3, \ldots, V_n)$$

is equivalent to

$$\text{READ } (V_1); \text{READ∅N } (V_2, V_3, \ldots, V_n)$$

Numbers are punched into data cards in the forms described in Section 1.2, and may be prefixed by "-". Numbers corresponding to variables of type integer must *not* contain decimal fractions or scale parts.

EXAMPLES   READ∅N (A2)

- In this case the data card must contain **at least** one number, say 1.279'-7 if A2 is not an integer variable,,

READ (B10,B11,B12,B15);

The data cards must contain four numbers, say

3.4'-1   7. 149   825'1   9 if **B10, B11, B12** are not integer variables, B15 may be an integer variable or a real variable. One could spread these constants over **several** cards if desired.

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In general input read into the machine must be assignment compatible with the corresponding variable (cf. Section 2.3.2).

2.3. Assignment of numerical values through expressions

Exponentiation a^b (a**b) is defined by repeated multiplication if b is a positive integer and by $1/a^{|b|}$ when b is negative. b must have type integer. If one desires the result of A^R where R is real, use EXP (R * LN (A)).

2.3.1. Evaluation of expressions

The discussion in this paragraph of Baumann et. al. is correct. However, in ALGOL W the type of a resulting expression is defined for each type and each operator. The type complex and the discussion of the long forms is provided for completeness and may be ignored by beginning programmers (cf. ALGOL W Language Description, Section 6.3).

I: A + B , A - B

A \ B	integer	real	complex
integer	integer	real	complex
real	real	real	complex
complex	complex	complex	complex

The result has the quality "long" if both A and B have the quality "long", or if one has the quality "long" and the other is integer.

II: A * B

A \ B	integer	real	complex
integer	integer	long real	long complex
real	long real	long real	long complex
complex	long complex	long complex	long complex

A or B having the quality "long" does not affect the resultant type of the expression.

III: A / B

A \ B	integer	real	complex
integer	real	real	complex
real	real	real	complex
complex	complex	complex	complex

The specifications for the quality "long" are those given for + and - .

IV: A ** B

A \ B	integer
integer	real
real	real
complex	complex

The result has the quality "long" if and only if A does.

V: ABS A means the "absolute value of A".

A	ABSA
integer	integer
real	real
complex	real

2.3.2. Type of the variable to which a value is assigned,

The assignment V := E is correct only if the type of E is
assignment compatible with V. That is, the type of V must be lower or
on the same level in the list below as the type of E.

integer

real, long real

complex, long complex

Several transfer functions are provided as standard functions
(cf. Section 2.4). For example, to change the type of expression E from
real to integer either ROUND(E), TRUNCATE(E) or ENTIER(E) may be used.,

2.3.4. Multiple assignments

The assignment of the value of an expression can be extended to
several variables. As in ALGOL 60, the form in ALGOL W is

$$V_1 := V_2 := \ldots := V_{u} := E;$$

The multiple assignment statement is possible only if all the
variables occurring to the left of $V_i :=$ are assignment compatible with
the type of the variable or expression to the immediate right of the :=.

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2.4 Standard Functions

All the standard functions listed in this section are provided in ALGOL W except sign and abs. ABS is a unary operator in ALGOL W. In addition the following standard functions are provided.

truncate(E)   if $E \geq 0$, then entier(E)

                         if $E < 0$, then -entier(-E)

round(E)   if $E \geq 0$, then truncate $(E + 0.5)$

                         if $E < 0$, then truncate $(E - 0.5)$

log(E)   the logarithm of E to the base 10

                         (not defined for $E < 0$)

time(E)   if $E = 1$, elapsed time returned in 60th's of a second

                        if $E = 2$, elapsed time returned in 60th's of a second and printed in minutes, seconds, and 60th's of a second

2.5. output

The identifier "print" should be replaced by "write". A print line-consists of 132 characters.

- EXAMPLES   WRITE(E);   WRITE($E_1, E_2, \ldots, E_n$);

The format of the values of each type of variable is listed below:

integer   right justified in field of 14 characters and followed by two blanks, Field width can be changed by assignment to INTFIELDSIZE.

real   same as integer except that field width is invariant.

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long real	right justified in field of 22 characters followed by 2 blanks.
complex	two adjacent real fields.
long complex	two adjacent long real fields.
logical	TRUE or FALSE right justified, in a field of 6 characters followed by 2 blanks.
string	field large enough to contain the string and continuing onto the next line if the string is longer than 132 characters.
bits	same as real.

In order to provide headings or labels for printed results, a sequence of characters may be printed by replacing any expression in the write statement by the sequence of characters surrounded by ". If the " mark is desired in a string it must be followed by a ".

EXAMPLES

WRITE ("N = ", N)

This statement will cause the following line to be printed if N is integer and has the value 3.

N =   3

WRITE ("SHAKESPEARE WRØTE ""HAMLET""")

This statement will cause the following line to be printed.

SHAKESPEARE WRØTE "HAMLET"

In the statement

WRITE $(E_1, E_2, \ldots, E_n)$

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the type of each E_i determines the field in which its value will be placed. The field for E_{i+1} follows the field for E_i on the current print line. If there is not enough space remaining on the current print line, the line is printed and the field for E_{i+1} begins at the beginning of a new print line. The first field of each write statement begins on a new print line.

3. Construction of the program

3.1 Simple Statements

Note that the simple assignment statement takes the form V := E and that the input-output statements are

READ (V), READON(V), and WRITE(E)

where V is a variable or a variable list and E is an expression or expression list.

3.2 Compound Statements

In later descriptions in these notes "compound statements" will be synonomous with "blocks without declarations".

3.4 Comments

The construction

comment text;

may appear anywhere in an ALGOL W program. However, in ALGOL W the comment following an end is limited to one identifier which is not a reserved word.

3.5. Example.

To clarify the change necessary to form an ALGOL W program from the program enclosed in the box, the example is shown as it would be punched. Note that an ALGOL W program must end with a . (period).

```
BEGIN COMMENT EVALUATION OF A POLYNOMIAL;
      REAL AO, Al, A2, A3, Xl, P;
      READ (AO, Al, A2, A3, Xl);
      P := ( (A3 * Xl + A2) * Xl + Al) * Xl + AO;
      WRITE (P)
END.
```

Note that the indentation, although not required, allows the begin and end to be matched easily. In complicated programs indentation will improve readability and therefore reduce the number of careless errors.

4. Loops

4.1. Repetition

The variable V of the for statements described is always of the type integer and cannot be declared in ALGOL W; its declaration is implicit (cf. Section 7), and its value cannot be changed by explicit assignment within the controlled statement. Each expression E of the for clause must be of type integer.

The statement of the form

$$\text{for } V := H_1, H_2, \ldots, H_n \text{ do } S;$$

is correct for $n \geq 1$ in ALGOL W only if $H_1, H_2, \ldots, H_n$ are all integer expressions,

The form

$$\underline{for}\ V := E_1\ \underline{step}\ 1\ \underline{until}\ E_2\ \underline{do}\ S;$$

may be abbreviated as

$$\underline{for}\ V := E_1\ \underline{until}\ E_2\ \underline{do}\ S;$$

4.2. Subscripted Variables

In **ALGOL** W the subscript expression must be of type **integer.** Any other type will result in an error detected during compilation.

4.2.1. Array declarations

. In the text, the : in array declarations must be replaced by :: for ALGOL W.   The word array must always be preceded by its type.

ARRAY A[1:10,1:20]; is incorrect and should be written

REAL ARRAY A (1::10, 1::20);

Only one set of subscript bounds may be given in an array declaration. Hence, the examples should be corrected for ALGOL W to read

EXAMPLES

real array A, B, C(1::10);

real array D, EG(1::10, 1::20);

integer array N, M(1::4);

4.4.2. Example

In ALGOL W the example in the box would be written as listed below.

```
BEGIN COMMENT DERIVATIVE OF A POLYNOMIAL;

    INTEGER N;      REAL P, C;

  REAL ARRAY A(1::20);

  READ (N, C);

  FOR I ..= 1 UNTIL N DO READON(A(I));

  P := 0;

  FOR I := N STEP -1 UNTIL 1 DO

      P := P*C + I*A(I);

  WRITE (P)

END.
```

5.   The Conditional Statement

Conditional statements are very useful and are used in ALGOL W as discussed in this chapter for ALGOL 60. Note that the symbols $<$, $\geq$, and $\neq$ must be replaced by $< =$, $> =$, and $\neg =$, respectively.

6.   Jumps

6.1. Labels

All labels in ALGOL W must be identifiers which are not reserved words.   The final expression in a function procedure may be labeled,

6.2. The Jump Statement

go to may be written as GO TO or GOTO in ALGOL W.

6.2.1. Jumps out of loops or conditional statements

The value of the loop variable is not accessible outside of the loop in ALGOL W.

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6.2.2. Inadmissible Jumps

It is not possible to jump from outside into a loop in ALGOL W.
Likewise, it is not possible to jump into a conditionalstatement.

In general, it is not possible to jump into the middle of any
statement, viz. for statement, conditional statement, while statement,
compound statement, block,

6.4. Another Form of Loop Statement

The statement described in the text does not exist in ALGOL W.

However, ALGOL W has another form of loop statement which is
useful -- it is called the while statement.

FORM   while B do S;

B is a condition like that described in Chapter 5. As long as B is
true, the statement S will be repeated. It is possible that S is
never executed. More precisely, this loop may be interpreted

L: if B then

     begin S; goto L

     end

The example in Section 6.3 can be rewritten as follows:

BEGIN COMMENT DETERMINATION OF THE CUBE ROOT;

     REAL A, APPROXIMATIONVALUE, X, Y, D;

     READ (A, APPROXIMATIONVALUE);

     X := APPROXIMATIONVALUE;   D := ABS X;

```
            WHILE D > .5'-9 * ABS X DO

            BEGIN

                Y :=x;   x   := (2*Y + A/(Y*Y))/3;

                D := ABS (X-Y);

            END;

        END.
```

7.. Block Structure

For the purposes of block structure in ALGOL W compound statements
must be considered as blocks, namely blocks without declarations. A
compound statement with a label defined in it is a block.   (Reread the
notes in this paper concerning Chapter 6.) In for statements the scope
of the variable V in the for clause is the statement S following the do.

7.4. Dynamic Array Declarations

The expressions specifying the subscript bounds in dynamic array
declarations must be of type integer.

8. Propositions and Conditions

The word "Boolean" in the text should be replaced throughout by
"logical".

8.1. Logical Operations

Some of the symbols for logical operations are different in
ALGOL W.

Operation	ALGOL	ALGOLW	READ AS
negation	¬	¬	not
conjunction	∧	AND	and
disjunction	∨	OR	or
equivalence	≡	~	is equivalent to

ALGOL W does not have an equivalent form of the ALGOL implication
symbol, ⊃. The effect of A⊃B is gotten by (¬A) OR B. The ALGOL W
expression A¬ = B is equivalent to the ALGOL 60 expression-,(&B).

The following hierarchical arrangement defines the rank of the
operator with respect to other operators.

Level	Operations Symbol
1	LONG, SHORT, ABS
2	SHL, SHR, **
3	¬
4	AND, *, /, DIV, REM
5	OR, +, -
6	<, < =, >, > =, =, ¬ =, IS

In a particular construct, the operations are executed in a sequence
fr m the highest level (smallest number) to the lowest level (largest
number). Operations of the same level are executed in order from left
to right when logical operations are involved and in undefined order
in arithmetic expressions.

The discussion in this section is correct except concerning the
hierarchy of operators. In general, the extra parentheses are required
in ALGOL W when using arithmetic expressions with logical operators.
The examples below are correct ALGOL W and correspond to examples in

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the text. All parentheses are necessary.

EXAMPLES

$(A > 5)$ OR $(B > = 1)$

$(A * B > = C + D) = (ABS (21 + Z2) > M)$

$(0 < = xj$ AND $(X < = 1)$

$(X = 3)$ OR $(1 < = X)$ AND $(X < = 2)$

means $(X = 3)$ OR $((1 < = X)$ AND $(X < = 2))$

9. Designational Expressions

The designational expressions described in the text do not exist
in ALGOL W.   The chapter may be skipped.

However, ALGOL W provides a designational statement and expression
which is equivalent to that described by the text.

9.1. The Case Statement

The form

CASE E OF

BEGIN

$S_1; S_2; \dots !$ $_n$.

END

is called a case statement.   The expression E must be of type integer.
The value of the expression, E, selects the S_E statement between the
BEGIN END pair.   Execution is terminated if the value of E is less
than 1 or greater than n.   After the designated expression is executed,
execution continues with the statement following the END.

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EXAMPLE

```
CASE I OF

BEGIN

    BEGIN J := I; GOTO Ll;

    END;

    I := I + 1;

    IF J < I THEN GOTO Ll

END
```

If the value of the expression, I, is 3, for example, the statement, IF $J < I$ THEN GOTO Ll is executed, If $J \geq I$ then execution continues following the END,

9.2. The Case Expression

Analogous to the case statement, the case expression has the form

$$CASE\ E\ OF\ (E_1, E_2, \ldots, E_n)$$

The value of the case expression is the value of the expression selected by the value of the expression E. If the value of E is e, *then* the value of E_e is the value of the case expression. The type of the case expression is

integer	if all E_i's *are* integer
real	if any E_i is real and no Ei **is** complex or long complex
long- real	if any E_i is long real and **all** E_i's are long real *or* integer
complex	if any E_i is complex
long complex	if any E_i is long complex and **all** E_i's are long complex, long real, or integer

EXAMPLE '

CASE 3 OF $(4.8, 12, 17, 4.9)$ has the value 17 in floating
point representation since the type of the case expression is real.

10. Procedures

10.1.1. Global and formal parameters

Labels may not be used as formal parameters.   Switches do not exist
ii? ALGOL W.

10.1.2.1. Arguments

Arguments serve to introduce computational rules or values into
the procedure.   A rule of computation can be brought into the procedure
if the computation is defined by means of another procedure declaration,
or a statement.

Formal simple variables, formal arrays, and formal procedures can
be arguments.

Example 3 is correct in the text.

A formal array can be used as an argument in only one way, "call
by name".   The discussion concerning "call by value" should be ignored.

10.1.2.3. Exits

Because labels may not be used as actual parameters to a procedure,
the text's discussion of exits is not correct for ALGOL W. However,
a statement (in particular a GOTO statement) may be used as an actual
parameter corresponding to a formal procedure identifier.   In this way
side exits leading out of the procedure are provided,

10.1.3. Function procedures and proper procedures

From given pieces of programs, procedures can be derived either in the form of function procedures or in the form of proper procedures.

The body of a function procedure is either an expression or a block with an expression before the final END in the procedure body. The value of the expression is the value of the function procedure.

The way in which a procedure is set up and used is a fixed characteristic of the procedure and is established directly in the declaration by means of the introducing symbols. The declaration of functions is introduced by the symbols

  INTEGER PROCEDURE

  REAL PROCEDURE

  LOGICAL PROCEDURE

    .

according to the type of the resulting value, The type of the expression giving the value of the procedure must be assignment compatible with the declared type of the function procedure.

The declaration of the proper procedure begins with the symbol

  PROCEDURE

No resulting expression can be placed at the end of the procedure body.

10.1.4. The procedure head

All necessary assertions about the formal parameters and the use of the procedure are contained in the head of the procedure declaration. In ALGOL W the head consists of three parts:

(1) Introductory symbol

(2) Procedure name

(3) List of formal parameters, and their specifications

(1) The introductory symbol determines the later use of the procedure
(cf. Section 10.1.3.)

(2) The procedure name can be chosen almost arbitrarily. The only
restriction is the general limitation concerning some reserved
. names (cf. Section 1.3).

(3) The type, value specification, and identifier name of formal
parameters appear in the list of formal parameter specifications,
and not separately as in ALGOL 60. The comma serves as the
general separation symbol between formal parameter identifiers
of the same type and value specification. The semicolon serves
as the general separation symbol between specifications of formal
parameters of different types or value specifications,

The type of the formal parameter is specified by the symbols

    REAL
    LONG REAL
    INTEGER
    COMPLEX
    LONG COMPLEX
    LOGICAL
    REAL ARRAY
    LONG REAL ARRAY
    COMPLEXARRAY
    LONG COMPLEX ARRAY
    INTEGER ARRAY
    LOGICAL ARRAY

```
REAL  PROCEDURE
LONG  REAL  PROCEDURE
COMPLEX  PROCEDURE
LONG  COMPLEX  PROCEDURE
INTEGER  PROCEDURE
LOGICAL  PROCEDURE
PROCEDURE
```

The value specification is used only for parameters called by
value .   It is specified by the symbol value,   It may only follow the
types INTEGER, REAL, LONG REAL, LOGICAL, COMPLEX, LONG COMPLEX,

EXAMPLES

PROCEDURE P (REAL X, Y; INTEGER VALUE I; PROCEDURE Q, R);

REAL PROCEDURE Z (LOGICAL L, M, N; REAL PROCEDURE P);

Note that in the case of formal parameters used as array identifiers,
information about the number of dimensions must be given. The last
identifier following each array specification must be followed by "("
followed by one asterisk for each dimension separated by commas, followed
by ")".

EXAMPLE

-PROCEDURE P (REAL ARRAY X, Y (*,*); REAL ARRAY Z (*)) .

10.2.   The Procedure Call

The procedure call in ALGOL W is unchanged from ALGOL 60. This
section should be read carefully,

Since labels are not allowed as parameters, it was earlier suggested
that jump statements be used and that the corresponding formal parameter
be a proper procedure (cf. 10.1.4. Example 8). In general, any

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statement may be used as an actual parameter corresponding to a formal proper procedure which is used without parameters,

EXAMPLE

```
BEGIN

        PROCEDURE VECTOROPERATIONS (INTEGER J; INTEGER VALUE N;
                            PROCEDURE P);
                BEGIN J := 1;
                        WHILE J < = N DO
                        BEGIN P; J := J + 1
                        END
                END;
                REAL PROD; INTEGER I;
                REAL ARRAY A, B, C(1::10);
                        (initialize A and B)
        L1: VECTOROPERATIONS (I, 10, C(1) := A(1) + B(1));
                PROD := 0.0;
        L2:     VECTOROPERATIONS (I, 10, PROD := PROD + A(1) * B(1));
        END
```

The statement L1 is a procedure call which causes a vector addition of A and B to be placed in C. The statement L2 causes the **element-by-**element vector product of A and B to be calculated and placed in PROD.

10.3. Example

```
REAL PROCEDURE ROMBERGINT (REAL PROCEDURE FCT;

    REALVALUEA, B;   INTEGER VALUE ORD);

  BEGIN REAL T1, L;

    ORD := ENTIER ((ORD + 1) / 2);

    BEGIN INTEGER F, N; REAL M, S;

        REAL ARRAY U, T (1 :: ORD);

        L :=  B-A;

        T(1) := (FCT(A) + FCT(B)) / 2;

        U(1) := FCT ((A + B) / 2);

        F := := 1;

        FOR H :=2 UNTIL ORD-1 DO

        BEGIN N := 2 * N; S := 0;

            M := L / (2 * Nj;

            FOR J := 1 STEP 2 UNTIL 2 * N - 1 DO

                S := S + FCT (A + J * M);

            U(H) := S / N;

            T(H) := (T(H - 1) + U(H - 1)) / 2;

            F := 1;

            FOR J := H - 1 STEP -1 UNTIL 1 DO

            BEGIN F := 4 * F;

                T(J) := T(J + 1) + (T(J + 1) - T(J)) / (F - 1);

                U(J) := U(J + 1) + (U(J + 1) - U(J)) / (F - 1);

            END;

        END;

        IF ORD > 1 THEN
```

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```
          BEGIN

              T(2) := (U(1) + T(1)) / 2;

              T(1) := T(2) + (T(2) - T(1)) /(4 * F - 1)

          END;

          Tl := T(1)

      END;

      Tl * L

  END;
```

The names of standard functions and standard procedures cannot appear
as actual parameters in ALGOL W.   Therefore the calls to RØMBERGINT
in Section 10.3 are incorrect.   However, this situation may be overcome
by declaring a procedure which returns the value of the standard function
or performs the computation of the standard procedure.

    EXAMPLE

```
        REAL PRØCEDURE SINE (REAL VALUE X); SlN(X);
```

Then a call to RØMBERGINT might be

```
        A := ROMBERGINT (SINE, X(1), x(2), lo);
```

    -EXAMPLE 6

```
        REAL PROCEDURE TRACE (REAL ARRAY A(*,*); INTEGER VALUE N);
          BEGIN REAL S;
              s := 0;
              FOR I := 1 UNTIL N DO
                  S := S + A(I,I);
              S
          END
```

EXAMPLE 7

```
PROCEDURE COUNTUP (INTEGER X);

    X := X + 1
```

EXAMPLE 8

```
PROCEDURE ROOTEX (REAL VALUE X; REAL Y; PROCEDURE P);

    IF X > = O THEN

        Y :  = SQRT(X)

    ELSE

        BEGIN Y := SQRT(ABS X);

            P

        END
```

The actual parameter corresponding to the formal parameter P should be a jump statement.

PART II: Some Extensions of ALGOL 60 in ALGOL W

1.   Procedures

1.1.   Call by Result

Besides "call by value" and "call by name", ALGOL W allows parameters
to be called by result.   The formal simple variable is handled as a local
quantity although no declaration concerning this quantity is present.
The value of the simple variable is not initialized at the procedure
call.   If the procedure exits normally; the value corresponding to the
formal simple variable is assigned to the corresponding actual parameter.
The formal parameter must be assignment compatible with the actual
parameter.   To specify a result parameter, insert the word RESULT after
the type and before the identifier (as with VALUE).

EXAMPLE

PROCEDURE P(REAL RESULT X,Y; INTEGER VALUE I; LONG COMPLEX RESULT Z);

1.2.   Call by Value Result

Formal simple variables may be called both by value and result.
This combines the calls of value and result so that the formal identifier
is initialized to-the value of the corresponding actual parameter at
procedure call and the value of the formal identifier is assigned to
the corresponding actual parameter at a normal procedure exit, To
specify-a value result parameter, insert the words VALUE RESULT after
the type and before the identifiers.

EXAMPLE

PROCEDURE Q(INTEGER VALUE RESULT I,J,K);

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2.   <u>Procedure Calls</u>

201.   <u>Sub-arrays as Actual Parameters</u>

In ALGOL W, it is possible to pass any rectangular sub-array (array of few dimensions, i.e., a generalized row) of an actual or formal array to a procedure.   Those dimensions which are to be passed to the procedure are specified by **'s,** and those which are to remain fixed are specified by integer expressions.   The number of dimensions passed must equal the number of dimensions specified for the corresponding formal array.

EXAMPLE

The actual parameter may be a sub-array of a three dimensional real array A.   Examples of possible actual parameter specifications and corresponding formal parameter specifications are listed below.

<u>Actual Parameter</u>	<u>Corresponding Formal Parameter Specification</u>
A or A(*,*,*)	<u>real array</u> B(*,*,*)
A(I,*,*)	<u>real array</u> B(*,*)
A(*,I,*)	<u>real array</u> B(*,*)
A(*,*,I)	<u>real array</u> B(*,*)
A(I,J,*)	<u>real array</u> B(*)
A(I,*,J)	<u>real array</u> B(*)

EXAMPLE

Read in the size of one dimension of a cubic array **X,** then read in the elements of **X.**

Calculate and write out the sum of the traces of all possible two dimensional arrays in A using the previously defined real procedure TRACE.

```
BEGIN
    REAL SUM;
    REAL PROCEDURE TRACE (REAL ARRAY A(*,*); INTEGER VALUE N);
        BEGIN COMMENT THE BODY OF THIS PROCEDURE IS GIVEN IN A
            PREVIOUS EXAMPLE;
        END;
    INTEGER N;
    READ(N);
    BEGIN
        REAL ARRAY X(1::N,1::N,1::N);
        FOR I  := 1 UNTIL N DO
            FOR J :=1 UNTIL N DO
                FOR K := 1 UNTIL N DO READON(X(I,J,K));
        SUM := 0;
        FOR I  := 1 UNTIL N DO
            SUM := SUM + TRACE(X(I,*, )  N)+ TRACE (X(*,L,*) ,N)
                + RACE (X(*,*,I),N);
        WRITE (SUM)
    END
END.
```

· 3.   <u>String Variables</u>

Frequently, it is desirable to manipulate sequences of characters,
This facility is available in **ALGOL** W in the form of string variables,,
Each variable has a fixed length specified in the string declaration,,
The form of the declaration is

string (<integer number>) <variable list>

The integer number must be greater than 0 and less than or equal to 256. The specification "(<integer number>)" may be omitted; a default length of 16 is assigned to the variables, Arrays of strings also may be declared,

EXAMPLE

    STRING A, B, C

    STRING (24) X, Y, Z

    STRING (10) ARRAY R, S(0::10, 5::15)

In order to be able to inspect elements of the string or to manipulate portions of the string, a substring designator is provided, of the form:

    <string identifier> (E | <integer number>)

The expression E must be of type integer, This string expression selects a substring of the length specified by the integer number from the string variable beginning at the character specified by the integer expression, The first character of the stringhasposition 0.

EXAMPLE

    BEGIN STRING (5) A;

        A := "QRSTU";

        A (3|2) := A (0|2);

        WRITE (A)

    END

In this example the constant string "QRSTU", is assigned to the variable A which is declared to be of length, 5. Then the character positions G and 1 of A are assigned to positions 3 and 4 of A.

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Consequently, when the string A is written its value is QRSQR. It should be noted that the assignments are made character by character from left to right. If the second assignment statement in the example above had been

A (2|3) := A(0|3)

the resulting value of A would have been QRQRQ.

The variable on the left of an assignment statement must be of length greater than or equal to the length of the expression on the right. Ifashorter string is assigned to a longer string, the shorter string is extended to the right with blanks until the lengths are equal.

EXAMPLE

BEGIN STRING(5) S;

    S := "ABCDE"; S := "XY"; WRITE(S)

END;

The string XY is printed.

Strings within a CASE expression or an IF expression must be all of the same length.

All the relational operators may be used with string arguments. The EBCDIC representations of the strings are compared character by character. If one string is shorter than the other, the shorter string is filled with characters less than any possible EBCDIC character.. Strings of unequal length are never equal.

Relation	Value
"A" < "B"	TRUE
"A" = "A"	TRUE
"A" > "2"	FALSE
"A , ," = "A"	FALSE

4. Records and References

Records and structured quantities composed of quantities of any of the simple types such as REAL, INTEGER, STRING, etc. Records themselves do not have values; only the quantities which compose the records may have values.

4.1. Record Class Declarations

Record declarations indicate the composition of a record. Unlike simple type declarations or array declarations no storage is reserved for a record when the record declaration is encountered. Essentially, the record declaration only describes the form of records to be created. The record declarations appear with all' other declarations. The form is:

RECORD V (<declarations of variables of simple type>);

The name V is the name of the record class. The variables declared between the parentheses are called the fields of the record.

EXAMPLES

RECORD A(INTEGER I,J; REAL Z; STRING (5) S);

RECORD B(REAL X; LONG REAL LX; REAL Y);

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The punctuation of the examples should be noted carefully., The names ir. the list of identifiers following the indication of the simple type are separated by **","**. The list is ended with a **";"** unless the **";"** would immediately precede the closing **")"**.

4.2. Reference Declarations

REFERENCE is a simple type in **ALGOL W.** The value of a variable of type reference is an address of a record. This address is sometimes **called** a pointer to a record.

Reference declarations appear in a program where all other declarations appear,

FORM

REFERENCE (V) V_1;

V is a name of a record class. V_1 is a name of a reference variable or a **list** of names of reference variables separated by **","**.

EXAMPLE

REFERENCE (A) R1, R2; R3;

The name V af a record class may also be a list of names separated by **","**. This list indicates the record classes to which records referenced by the reference variables must belong.

EXAMPLE

REFERENCE (A,B) R4, R5;

R4 and R5 may point only to records of record class A or **B.**

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The reserved word NULL stands for a reference constant which fails to designate a record,

Arrays of references are declared and used analogously to arrays of other simple types.   The form of the declaration is:

REFERENCE (V) ARRAY V_1 (<subscript bound+);

EXAMPLE

REFERENCE (A,B) ARRAY AR1, AR2 (1::10),3::7);

The implementation requires that all reference arrays declared in a block be declared in the same reference array declaration or immediately following a reference array declaration.

EXAMPLE

REFERENCE (A) ARRAY AR1, AR2 (1::10,3::7);

REFERENCE (B) ARRAY AR(2::17);

In the example above, any other declaration except a reference array declaration is not allowed between the two reference array declarations.

. Reference Expressions

Quantities of simple type reference may be used in assignment statements and comparisons,

EXAMPLES

```
R1 := R2
R1 := NULL
R1 = R2
R2 ¬ = R3
```

Only the relations = and ¬= are allowed between references. In order to inquire to which record class a reference expression is bound, the IS operator is provided. The form is:

    E IS v

E is a reference expression and V is a name of a record class. The value of the IS operator is logical, either TRUE or FALSE.

EXAMPLE

    R4 IS B

4.4. Record Designators

A particular type of reference expression is the record designator. A record designator is the name of a record class.

EXAMPLE 1

    R1 := A
    R4 := B

When the record class name is encountered, the value is a pointer to a new record of that class. The values of the fields of the new record are undefined.

ALGOL W provides a short notation for creating a record and initializing its fields. This modified record creator has the form

$$V(E_L) \ .$$

V is the name of the record class. The expression list E_L between the parentheses is the list of the values of the fields specified in the order they appear in the record class declaration.

EXAMPLE 2

        BEGIN RECORD H (INTEGER C,D; STRING (2) S);

                REFERENCE (H) Rl;

                Rl : = H(5, 8, "AZ")

        END*

Examples 2 is a short program which declares a record class H and one reference variable Rl whose values may point to records of class H. One record of class H is created and each field of the record pointed to by Rl is initialized.

4.5 Field Designators

In order to manipulate the values of the fields of a record, the expression

$$V_1(E)$$

exists in ALGOL W. E is a reference expression. V_1 is a field of the record class of the record pointed to by E. The type of the field designator is the type of the variable V_1.

EXAMPLES

        Z(Rl)

        LX(R4)

EXAMPLE 2 can be rewritten as:

```
BEGIN RECORD H (INTEGER C,D; STRING (2) S);

     REFERENCE (H) R1;

    R1:= H;

    C(R1) := 5;

    D(R1) := 8;

    S(R1) := "AZ"
END.
```

NOTES ON NUMBER REPRESENTATION

ON **SYSTEM/360**

AND RELATIONS TO ALGOL **W**

by

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The following notes are intended to give the student of Computer Science 136 some orientation into how numbers are represented in the IBM System/360 computers. Because we are using Algol W, some references are made to that language. However, very little of what is said here depends on the peculiarities of Algol W, and this exposition is mostly applicable to Fortran or Algol 60 with slight changes in wording, It will also do for the floating-point numbers and full-word integers of PL/1. Users of shorter or longer integers or decimal arithmetic in PL/1 will need more orientation.

On IBM's system $60, the following units of information storage are used:

a) the **bit**, a single 0 or 1

b) the **byte**, a group of eight consecutive bits

c) the (short) word, a group of four consecutive **bytes--** i.e., 32 consecutive bits

d) the long word, a group of two consecutive short words-- i.e., eight bytes or 64 **bits.**

For number representation in **Algol** W the words and long words are the main units of interest .

INTEGERS

Integers are **stored** in (short) words Of the 32 bits of 8 ***short*** word, one is reserved for the sign (0 **for** + and 1 for **-**), leaving 31 bits to represent the magnitude, A positive or zero integer is stored in a binary (base 2) representation Thus 21_{10} (the subscript means base 10) is stored as

0000 0000 0000 0000 0000 0000 0001 0101 。
↑
sign bit

To confirm this, note that

$21 = \underline{0} \times 2^{30} + \ldots + 0 \times 2^5 + 1 \times 2^4 + 0 \times 2^3 + x1\ 2^{\overset{2}{\underset{}{}}} + 0 \times 2^1 + \underline{1} \times 2^0.$

The largest integer that can be stored in a word **is**

$2^{30} + 2^{29} + \ldots + 2^1 + 2^0 = 2^{31} - 1 = (2147483647)_{10}$.

Any attempt to create or store an integer larger than $2^{31} - 1$ will produce erroneous results, and (unfortunately) the user will not always be warned of the error, (See below,)

To save space in wri-king words on paper, each group of four bits in a word is frequently converted to a single base-16 (hexadecimal) digit, according to the following code:

Base	base 16	base 2	base 16
0000	0	1000	8
0001	1	1001	9
0010	2	1010	A
0011	3	1011	B
0100	4	1100	C
0101	5	1101	D
0110	6	1110	E
0111	7	1111	F

Thus A, B, C, D, E, F are used as base-16 representation6 of the **decimal** numbers 10, 11, 12; 13, J-4, 15 respectively, Nevertheless, integers are stored as base-2 numbers

Using hexadecimal notation, the decimal number 21 is represented by

$$00000015_{16} \quad \circ$$

Note that 15_{16} is the base-16 representation of 21_{10}.

Negative integers are **stored** in what is called the "**two's** complement form", For example, -1 is stored as

$$1111 \ 1111 \ 1111 \ 1111 \ 1111 \ 1111 \ 1111 \ 1111 \ ,$$

$$= FFFFFFFF_{16} \quad \circ$$

Also, -21 is stored as

$$1111 \ 1 \ 1 \ 1 \ 1 \ 1111 \ 1111 \ 1111 \ 1111 \quad 10 \ 1011$$

$$= FFFFFFEB_{16} \quad \circ$$

The representation for -21 is obtained from that for +21 by **changing** every 0 to 1 and every 1 to 0, and then adding + 1 in **base-2** arithmetic to the result, Similarly for any negative integers, Every negative integer has 1 as its sign bit, The smallest integer storable in System/360 is $-2^{31} = -2147483648$, and is represented by 80000000_{16}. Another way to **think** of the representation of negative numbers is to consider a 32-**place** binary accumulating register (the base-2 equivalent of the decimal accumulating register in a **desk calculating** machine), If one s-tarts with **all** zeros in this register, one get6 the **representation** for -1 by subtracting 1. The **process** require6 a "borrow" to propagate to the **left all** the way **across the register,** leaving **all ones,** just 86 on a decimal accumulator this would leave **all nines.** Continue& sub-traction **will** give the representations for -2, -3, ...

From the point of view of an accumulator we can also see what happens when we create a positive number larger than $2^{31}-1$. For example, if we add 1 to 2^{31}-1, the resulting carry will go all the way into the sign bit, leaving a sign bit of 1 with all other digits zero. But this is the representation of -2^{31}. Thus the attempt to produce positive numbers in the range from 2^{31} to approximately 2^{32} will yield a negative sign bit. Consequently, positive integers that "overflow" into this range are sensed as negative by System/360. Any anomalous appearance of negative integers in a computation should lead the programmer to suspect Integer overflow anisms of Algol W for detecting integer overflow (not described in this document) can be used to detect addition6 or subtractions that produce integers outside the range from -2^{31} to 2^{31}-1. The presence of an integer product outside that range is not at present detectable in Algol W, although the compiler could (and perhaps should) be modified to make a test. Attempts to divide an integer by 0 will yield an error message and an irrelevant quotient and remainder.

The behavior of System/360 on integer overflow is quite different from the Burroughs B5500. In the latter machine, any integer that overflows is replaced by a round floating-l+. ct number. There are advantages to either approach t integer overflow, depending on the a lication.

If the user suspects that Integers in hi6 program are getting anywhere near 10^9, he should convert them to double-precision floating-point numbers by use of the Algol W operator LONG. Conversion to single-prec n floating-point numbers may lose some precision.

The most important thing for a scientific user to remember is that integers in the range -2^{31} to 2^{31}-1 are stored without any approximation. Moreover, operations on integers (adding, subtracting, multiplying) are done without any error, so long a6 all intermediate and final results are integers between -2^{31} and 2^{31}-1. It is perhaps easier to remember as safe the interval from -2×10^9 to 2×10^9, obtained from the useful approximation $2^{10} \doteq 10^3$.

The operations of division without remainder (called **DIV** in Algol W) and taking the remainder on division (called REM in Algol W) always give integer answers,　If the divisor is 0, an error message is given,,

In Algol W two operations on integers give results that are not stored as integers--namely / and **.

FLOATING-POINT NUMBERS

Numbers in many scientific computations will grow in magnitude well beyond the range of integers described above,　To provide for this, System/360 and most **scientific** computers have a second way to represent numbers--the so-called floating-point representation, The significance of the name "floating-point" is that the radix **point** --for example, the decimal point in base-10 numbers-s-is **permitted** to float to the right or left, thus permitting scaling of numbers by various powers of the radix,　Although a decimal point tha% has floated off to the left will produce a number written like 0.001345, the numbers are actually represented in a form closer to what is often called scientific notation, here 1.345×10^{-3} .

In System/360, floating- int numbers are always represented in base-16 **notation;i.e.,** the radix or number base s 16,　This permits us tc write numbers in abbrevi ed form (as we did with integers earlier), **More important,** the use of base-16 conforms with the hardware arithmetic processes in which shifting is done four **bits** at a time to speed up the operations.　The speed-up is achieved at a slight **cost** in precision, as is learned from detailed error analyses which we cannot go into here.

We first consider the floating-point **representation** of numbers by a single word of 32 bits,　This is the so-called single-precision or short real number, the number of type REAL in Algol **W.**　The 32 bits of a word are numbered from 0 to 31, from left to right, just **to** identify them,　In floating-point representation the left-hand eight bits (bits 0 to 7, equivalent to two hexadecimal digits) are **devoted** to **the** sign of the number and the exponent of 16 associated with the number, The **right-**hand 24 bits (bits 8 to 31, equivalent to six hexadecimal digits)

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represent six significant hexadecimal digits (the significand) of the number.

As with integers, the sign of the number is denoted by bit 0, with 0 representing + and 1 representing -.

Bits 1 to 7 give the binary (base-2) representation of a non-negative integer in the range 0_{10} to 127_{10}, inclusive. This integer is called the biased exponent, for reasons now to be explained. If this integer were taken directly as the exponent, we would have no negative exponents, and our range of floating-point numbers could not include such numbers as 16^{-25}. 1% is desirable to have an exponent range that is approximately symmetric about zero, in System/360 one obtains the true exponent of the floating-point number by subtracting 64 from the biased exponent represented by bits 1 to 7. As a result, the actual exponent range from -64 to 63.

The 24 bits 8 to 31 of a number are regarded as six hexadecimal digits with a hexadecimal point at the left-hand end, If the floating-point number zero is being represented, all the hexadecimal. digits are zero, as are all the other bits, Otherwise, at least one of the hexadecimal digits must be nonzero. A floating-point number is said to be normalized if the left-hand hex decimal digit (the most significant digit) of the significand is nonzero. In System/360 the floating-point numbers are ordinarily normalized, and we will not consider any other forms.

We now give the floating-point representations of some sample numbers. As we said before, the number zero is represented by 32 zero bits, i.e., by eight 0 hexadecimal digits, Thus zero is represented by the same words in floating-point or integer form. No other number has this property,

The number 1.0 is represented by the word

sign bit

⮑ 0,100 0001,   0001 0000 0000 0000 0000 0000, .
     biased   significand
     exponent

To check this, note that the sign is 0 (representing +). The biased exponent is 1000001_2 or 65_{10}. Subtracting 64_{10} yields 1 as the true exponent. The hexadecimal significand is 100000_{16}. Putting a hexadecimal point at the left end gives the hexadecimal fraction $._{16}000016$, which equals $1/16$. Thus the above word represents $+1/16$ times 16^1, or 1.0 .

To save writing, the above word is ordinarily written in the hexadecimal form 41100000 . While one gradually learns to recognize some floating-point numbers in this form, the author knows no easy way to convert such a hexadecimal word into a real number. One just has to take the right-hand six hexadecimal-digi%s, and prefix a hexadecimal point, Then one examines the left-hand two-hexadecimal-digit number (here 41). If this is less than 80_{16} , the floating-point number is positive and one gets the true exponent by subtracting $40_{16} = 641$, . If the left-hand two-hexadecimal-digit number is 80_{16} or larger, the floating-point number is negative, and one gets the true exponent by subtracting $CO_{16} = 80_{16} + 40_{16} = 192_{10}$ and affixing a minus sign. Some facility with hexadecimal arithmetic is required, if one has to deal with such numbers.

In this presentation, we have considered the radical point to be , at the left of the six significant hexadecimal digits, and regarded the exponent as biased high by 64_{10} . As an alternative, the reader may prefer to place the radix point Just to the right of the most significant digit of the significand, and regard the exponent as biased high-by 65_{10} . This brings the significand closer to usual scientific notation but, of course, requires a trickier conversion to get the true exponent, The fact that either interpretation (and many others) are possible shows that really the radical point is just in the eye of the beholder, and not in the computer!

Several examples of floating-point numbers are now given in hexadecimal notation, with the confirmation left to the reader.

decimal		floating-point
0.0	=	00000000
1.0	=	41100000
0.0625	=	40100000
16.0	=	42100000
256.0	=	**43100000**
-1.0	=	C1100000
-16.0	=	C2100000
3.5	=	41380000

The largest floating-point number is 7FFFFFFF, representing .FFFFFF $\times 16^{3F}$ **or** $(1 - 16^{-6}) \times 16^{63} \doteq 7.23 \times 10^{75}$. (Here 10 and **16** denote decimal numbers,)

The smallest positive normalized floating-point number is 00100000, representing

$$\frac{1}{16} \times 16^{-64} \doteq 5.40 \times 10^{-79}$$

Negatives of these two numbers can also be represented, and are the extremes in magnitude of representable negative numbers,

Very few numbers can be exactly represented with six significant decimal digits. (<u>Exercise</u>: Which ones can?) For example, $1/3 = .333333_{10}$ only approximately. In the same way, very few numbers can be exactly represented with six significant hexadecimal digits, (**Exercise:** Which ones can?) For example, $3 = .555555_{16}$ approximately. Moreover, some numbers that are exactly representable in decimal are only approximately representable in hexadecimal; for example,

$1/10 = .100000_{10}$ exactly; but

$1/10 = .19999A_{16}$ only approximately.

Thus <u>round-off error</u> enters into the representation of most floating-point numbers on System/360, and the round off differs from that with decimal numbers. This can easily give rise to unexpected results. For example, if the above number $.19999A_{16}$ $(\doteq 0.1_{10})$ is multiplied by the integer $100_{10} = 64_{16}$, one gets not $A.00000_{16} = 10.0_{10}$, but instead $A.00003_{16}$, as a cumulative effect of the slightly, high approximation to 0.1_{10}. And A.0000316 rounds to 10.00002_{10} on conversion to decimal,

The precision of a single-precision hexadecimal number is roughly 10". One can think of this as being crudely equivalent to seven sig-

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nificant decimal digits-.

Not only do errors appear in the representation of numbers inside **System/360** (or any computer), **but** they arise from arithmetic operations performed on numbers,   For example, the product of two **floating-point** numbers may have up to 12 significant hexadecimal digits.   When the product is stored as a single-precision floating-point number, it **must** be rounded to six hexadecimal digits, This **introduces** an error, even though the factors might have been exact,

The story of round off and its effect on arithmetic is a complex and interesting one.   Only within the current decade have **there** begun to appear even partly satisfactory methods to analyze round off, and we cannot go into the matter now,   Some idea of **this** is **obtained** in Computer Science 137.

When an Algol W program assigns decimal numbers or integer values to variables of type REAL, these are **immediately** converted to hexadecimal floating-point numbers, with (usually) a round-off error,   When one outputs numbers from the computer in Algol **W,** they are converted **to** decimal,   Both conversions are done as well as possible, bu% **introduce** changes in the numbers **that** the ⸱rogrammer must be aware of,   And, of course, all intermediate opera++ions introduce further round offs **and** possible errors,   It is unthinkable **to** do the analysis necessary to counteract these errors and get the true answer **to** the problem, If the user wishes answers **uncontaminated** by round off, he should use integers and integer arithmetic, and be prepared **to** guard against overflow,

Fortunately most users can **accept** an indeterminate amount of round off in their numbers, provided **they** have some **assurance that** round off is not growing **out** of control   It is the business of numerical analysts to provide **algorithms** whose round-off **properties** are reasonably under control.   This has been well accomplished in some **areas,** and hardly at all in others.

DOUBLE PRECISION

The precision of single-precision floating-point numbers seems

very adequate for most scientific and engineering purposes,being at the
level of seven decimals, However, a considerable number of computations
require still more precision in the middle somewhere, just in order to
came out with ordinary accuracy a% the end, As a result, System/360
has provided an easy mechanism for getting a great deal more precision
in the computations, For this purpose a double word of 64 bits is used
to store a floating-point number of so-called double precision or long
precision. In this representation, the sign and biased exponent are
found in the firs% word of the double-word, with precisely the same
interpretation as with single-precision floating-point numbers. The
second word of the double-word consists of eight hexadecimal digits
immediately following the six found in the firs% word, There is no
sign or exponent in the second word. Thus a double-word represents
a signed floating hexadecimal number with 14 significant hexadecimal
digits. As before, nonzero numbers are normalized so that the most
significant digit of the 14 is nonzero.

Examples:

long significand

1.0L   = 41'100000   00000000

0.1L   = 40 199999   9999999A

There is a full set of arithmetic operations for both single
and double-precision operations. Very crudely, for an example, single-
precision multiplication of single-precision factors takes around 4 micro-
seconds, while that for double-precision factors takes around 7 micro-
seconds, For modes% problems the extra time is completely lost in the
several seconds of time lost to systems and compilers, and the use of
double-precision is strongly recommended for all scientific computation.
Normally the only possible disadvantage of using long precision is the
doubling in the amount of storage needed, If one has arrays with tens
of thousands of elements, the extra storage may be very costly, &her-
wise, it should no% matter,

since $16^{-14} \doteq 10^{-17}$, the double-precision numbers are crudely
equivalent in precision to 17 significant decimal digits.

For a machine with the speed of the 360/67, a number precision of

six hexadecimal digits (roughly seven decimals) is considered very low, while a precision of 14 hexadecimal digits (roughly 17 decimals) is very adequate.

The floating-point arithmetic hardware of System/360 provides the possibility of detecting when numbers have gone outside the exponent range stated above. The reader may think that a range from roughly 10^{-79} to 10^{75} should cover all reasonable computations. While exponent <u>overflow</u> and exponent <u>underflow</u> are no% very common, they can be the cause of very elusive errors. The evaluation of a determinant is a common computation, and for a matrix of order 40 is quite rapidly done (if you know how). If the matrix elements are of the quite reasonable magnitude 10^{-3}, the magnitude of the determinant will be no larger than roughly PO^{-90} (and probably much smaller), well below the range of representable floating-point numbers. Such problems are a frequent source of exponent underflow.

We shall not discuss here the mechanisms of Algol W for de%ec%ing exponent overflow and underflow, for these should be written up in another place. Even without these, we see that floating-point numbers behave well for numbers that are at least 10^{66} times as large as %he largest integer in %he system. Hence use of floating-point numbers meets almost all the problems raised by integer verflow. And, of course, it permits the use of a large set of rational numbers, which do not even enter the integer system.

ALGOLWREALS AND LONGREALS

The Algol W manual tells how to represent real variables and numbers to take advantage of both single-and double-precision. The purpose of this section is to bring this information into rapport with the hardware representation of numbers. If a variable X is declared REAL, one word is set aside for its values, and it will be stored in single-precision floating-point form. if a variable is declared to be LONG REAL, a double-word is set aside to hold its values, and it will be stored in double-precision form

If a number is written in one of the decimal forms without an L
at the end, it will be rounded to single-precision, no matter how many
digits are set down, Thus 3.1415926535897932 will be immediately
rounded to single-precision in the program, and all the superfluous
digits are lost at once. Thus the assignment statement

$$xx := 3.1415926535897932$$

will result in the double-word XX receiving a well-rounded form of π
in the more significant half, and all zeros in the less significant
half! Thus one gets a precision of only approximately seven decimals
for the pain of writing 17, and this may well contaminate all the rest
of the computation.

If one wants XX to be precise to approximately full double precision,
one must write the statement in the form

$$xx := 3.1415926535897932L .$$

With the declaration REAL X, the statement

$$X := 3.1415926535897932L$$

will result in X having a single-precision approximation to π , as
the long representation of π is rounded upon assignment to X.

The reader should now go back and examine the specifications of
the types of various arithmetic expressions, as stated on pages 9, 10,
11 of the Algol W Notes, and on pp. 25, 26 of the Language Definition,
Some of the less expected effects are the following: Suppose we have
declaractions

        REAL x, Y, z;
        LONG REAL XX, YY, ZZ;
        INTEGER I, J, K;
        Then X*Y is LONG REAL; I**J is REAL; I*X is LONG REAL;
        The assignment statement
            xx := x := Y*Z
will result in XX having a single-precision rounded version of Y*Z in
the more significant half, and zeros in the less significant word,
        Moreover, I*I is INTEGER, but I**2 is REAL.

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If the reader understands the language Algol W and the preceding pages on number representation, he should have a good basis for understanding the effects of mathematical algorithms . But he should always remain wary of what a computer is actually doing to his numbers9