MUTANT 0.5

AN EXPERIMENTAL PROGRAMMING-LANGUAGE

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Abstract

A **programming language** which continues the extension and simplification
of **ALGOL** 60 in the **direction** suggested by EULER is defined and described.
Techniques used in an experimental implementation of that language, called
MUTANT 0.5, are briefly summarized. The final section of this report is an
attempt to assess the potential value of the approach to procedural program-
ming language design exemplified by MUTANT 0.5. Implementation and use of the
experimental system have indicated **a** sufficient number of conceptual and
practical problems to suggest that the general approach is of limited value;
however, a number of specific features were found to be convenient, useful,,
and adaptable to other philosophies of language design.

A. Introduction

In his thesis, **McKeeman** [McKee 66] describes MUTANT, a "kernel" language which he proposes as a nucleus for the design of procedural programming languages. Many features of that language appeared useful for expressing algorithms of both graph theory and graphical data processing. In addition, MUTANT suggests possible approaches to the problems of data structuring and the specification of parallel processing. To gain some experience with such facilities, an experimental language with semantics **similar** to those of MUTANT was designed. Certain semantic concepts were generalized, and others restricted; also the syntax was substantially altered. In addition, the current version of the language does not include all facilities of **MUTANT** (most notably, unordered sets and real number arithmetic); it is therefore called MUTANT 0.5.

A processing system for MUTANT 0.5, consisting of a compiler and an interpreter, was implemented on the IBM **System/360,** and some experience with that system has been obtained. The language has been found to allow a concise and natural expression of many algorithms, but a number of difficulties were experienced in designing both the language and the interpreter for the system. Although certain language improvements are obviously needed and efficiency could be significantly increased by use of more suitable hardware, I agree with Wirth's conclusion [Wirth 67a] that difficult logical problems underlie both the design and implementation of such a language. No further development or use of the current system is planned. Thus in terms of providing a useful language and processor, the project was a failure. It was, however, a valuable exercise in language design; this report is an attempt to analyze, for the benefit of future **work,** some of-the strengths and weaknesses of the MUTANT 0.5 design revealed by both the implementation and the use of the language.

A.1 Organization of the Report

In section **B,** MUTANT 0.5 is defined in the style of the **ALGOL** 60 report [Naur 63]. Syntax is described by productions in Backus-Naur form (BNF); semantics, by English prose. Some examples of programs in MUTANT 0.5 **are** then presented and explained. Section C is a brief summary of the techniques used in implementing the experimental compiler and interpreter. Use of these **programs** is described in section D. Finally, section E is an attempt to **charac-**

terize MUTANT-like programming languages, to identify some inherent problems in their definition and implementation, and to assess their practical utility. That section is a minor revision of a draft written in September 1967; some of the positions stated there have since been substantially extended or reformulated as a result of more recent reading, discussion, and research.

Appendices III, IV, and V, although referenced in the text, are not reproduced in this report. They are compilation listings of the various programs used in the experimental implementation of MUTANT 0.5.

A.2 Comments on Notation

In this report, two different character and terminal symbol representa-. tions are used in the description of the syntax of MUTANT 0.5 as well as for the representation of programs written in the language. One may be considered the publication representation; the other, a hardware representation reflecting the available character set. The former is introduced in the belief that it is somewhat more agreeable and readable. Appendix I establishes the correspondence between these two representations. In addition, a slight variant of BNF has been adopted for compatability with the output of certain processing programs: alternate right parts of a production are placed on consecutive lines without repetition of the corresponding left part. In the remainder of this report, publication and hardware representations will be freely cross-referenced, usually without explicit comment.

A.3 Acknowledgements

B. The MUTANT 0.5 Language

    The syntax and semantics of MUTANT 0.5 are defined below. In general, McKeeman's statement of the principles of language design [McKee 66, pp. 71-73] has been accepted as valid. Conciseness of notation has been carried somewhat further by adapting the notation of set theory whenever possible. The concepts and notation of the language were primarily inspired by McKeeman's MUTANT [McKee 66]; they also draw directly and indirectly from ideas found in ALGOL 60 [Naur 63], EULER [Wirth 65a], APL [Iver 62], and PL/I [IBM 66].

B.1 The MUTANT 0.5 Grammar

    The grammar of MUTANT 0.5 is listed, in the hardware character set, in Appendix II. In addition, -relevant productions of the grammar will be included at appropriate, points in the following discussion of the semantics of MUTANT 0.5. Such productions are related to Appendix II by the use of marginal production numbers. The somewhat artificial appearance of some productions reflects two constraints placed on the grammar, namely

  (1) the production set must lead to a simple precedence grammar [Wirth 65a];

  (2) the productions must be chosen to simplify the translation of the language during the process ofsyntactic analysis.

    For the reasons given by McKeeman [McKee 66, p. 93], it is convenient to define the syntax of identifiers, strings, and integers external to the formal grammar of MUTANT 0.5; informally, it may be described by the following set of productions.

```
(identifier)  ::= (letter)
                  (identifier) (letter)
                  (identifier) (digit)
(integer)     ::= (digit)
                  (integer) (digit)
(string)      ::= (string head) "
(string head) ::= "
                  (string head) (non-quote character)
                  (string head) " "
```

B.2 Semantic Description of MUTANT 0.5

MUTANT 0.5 programs describe the creation and manipulation of values. In the language, values of three unstructured types (integer, process, and name) and two structured types (string and list) are available to the programmer. Values of type integer have the properties of mathematical integral values. process values are designations of computational processes (procedures); name values designate special computational processes which, upon activation, compute the name of a storage cell. string values are sequences of character values, which correspond to elements of a fixed set of symbols. In MUTANT 0.5, list values are ordered sequences of structured or unstructured values of arbitrary length, in which all elements are not required to be unique in value.

> Comment
> The above types were chosen as a minimal set adequate for experimentation. In any serious programming language, real number arithmetic would be essential. McKeeman's type set also appears to be a valuable addition to programming languages, omitted only because of limited time and goals.

Since MUTANT 0.5 is a highly involuted language, description of many constructs requires the use of terms before they are defined. The reader unfamiliar with MUTANT or a similar language is advised to consider some of the simpler examples of section B. 3 before continuing.

B.2.a Constants

syntax

(constant) . ::= (integer)		(64)
(string)		(65)
⟨begin⟩ }		(66)
(begin) ::= {		(70)
(declare) |		(71)

Semantics

A non-negative integer is denoted by a sequence of decimal digits, and the value of that integer is the value of the digit sequence interpreted as a decimal number. Negative integers are syntactically recognized as primaries.

A string is a sequence of characters and is denoted by a sequence,

delimited by string quotation marks ("), of the graphic symbols corres-
ponding to the character values. In the denotation of a string, two
contiguous string quotation marks signify a single string quotation character.

The construct " { } " (or " (declare) | } ") denotes the null list ,
i.e., a value of type list with no elements.

A constant alwayshas a value.

Examples

    0   3   100   32767
    "This is a string."   " " "Hamlet " " "
    { }

B.2.b Declarations

syntax

(declare)	::= { $	(72)
	(declare) (identifier)	(73)
	(declare) (identifier) ((v-expression))	(74)

Semantics

MUTANT 0.5 provides values of several types as well as storage cells
into which such values may be placed. Declarations serve to create cells
and also to provide names for either cells (and their contents) or for
values. At most one declaration appears at the head of a list (B.2.c), and
the scope of the identifiers in that declaration is exactly the corresponding
list.

If the identifier is immediately followed by an expression in
parentheses, that identifier is considered to name the value of that ex-
pression. All such expressions are computed sequentially before com-
putation of-the values of any of-the list elements, and these expressions
are evaluated as if they were written in an immediately containing list.
No explicit assignment to an identifier naming a value is permitted.

If the identifier is not so followed, it names a cell. Values of
any type may be assigned to any cell, and such assignment dynamically
determines the cell structure. Thus the structure of a cell may be undefined,
or atomic, if the cell contains a value of unstructured type, or structured.
If, in the last case, the cell contains a value of type list, that cell
has a composite structure consisting of a sequence of (atomic or structured)
subcells, one for each list element. Similarly, if the cell contains a value
of type string, that cell is structurally a sequence of atomic character cells.

An identifier names the cell or value associated with it by a declaration.

Every non-reserved identifier not contained in a declaration either
must designate a controlled value (B.2.1) or procedure formal parameter
value (B.2.m) or must occur within the scope of an identifier of the
same name. If an identifier is associated with more than one scope, a
use of that identifier designates the cell or value associated with
it in the smallest possible containing scope. Subcells or subvalues are
designated by a uniform indexing scheme (B.2.f).

Examples

    { $ a b newidentifier

    { $ x y twotothe15th **(32768)**

    { $ sum (a+b) difference (a-b)-

Comment

Named values may alternatively be viewed as the contents of cells
which may be initialized upon scope entry but are "read-only" within
the scope of the naming identifier. The rules of scope and evaluation
of the initializing expression do not admit initialization to recursive
procedure values; a facility similar to Landin's rec [Land 64, 66] is absent.

B.2.c Lists

Syntax

(list)	::=	(list head) }	(67)
(list head)	::=	(begin) (g-expression)	(68)
		(list head) , (g-expression)	(69)
(begin)	::=	{	(70)
		(declare) |	(71)

Semantics

A list is an ordered sequence of general-expressions. In the execution
of a MUTANT **0.5** program, the expressions within the list are computed success-
ively from left to right. A general-expression may conditionally fail to
designate any value. Lists have structured values of type list; the value
of a list is the (possibly empty) sequence of values of those contained
general-expressions yielding values. A declaration does not have a value or
constitute a list element. In general, the number of elements in the list value
cannot be determined a priori. A list always has a value.

Examples

    { 1, 2, 3, "abc" }   { 1, { 2, { 3 } } }

```
{ 1 → x, y-2 → y, 10⊗a }
{ $ a b | x → a, y → b, a+b, a-b }
{ $ a | { $ a | 2 → a }, 2 → a }
{ a+b, a-b, a⊗b, b≠0 => a÷b }
```

B.2.d <u>Simple Primaries</u>

<u>syntax</u>

⟨**s-primary**⟩	::= (s-primary *)	(53)
(s-primary *⟩	::= (constant)	(54)
	<u>get</u>	(55)
	(list)	(56)
	(primary *⟩ (list)	(57)
	⟨ (v-expression))	(58)
	(case head) (v-expression))	(59)
	(for head) }	(60)
	(while head)' }	(61)
	(for/while head) }	(62)
	(s-primary *⟩ [(v-expression)]	(63)

<u>Semantics</u>

Productions 57 (B.2.m), 59 (B.2.e), and **60-62** (B.2.1) are listed for completeness but are not discussed in this section.

Every simple primary has a value, which may be of either structured or unstructured type.

The value of the primary <u>get</u> is of type string and consists of the next string (according to the MUTANT **0.5** conventions) found in the interpreting mechanism's sequential input stream when the primary is evaluated, and such evaluation causes that string to be deleted from the input stream.

Parentheses serve to control the association of operands, and hence the application of operators, in the conventional way.

Square brackets are used to designate the subscripting of simple primaries. In the application of the subscript operator, the simple primary and then the subscripting value-expression are evaluated, and the value of the result is determined by application of the following algorithm:

(1) If the value of the simple primary is of unstructured type, then the result is not defined.

(2) If the value of the simple primary is of type <u>list</u>, then

(a) if the value of the subscripting **expression is** of type <u>integer</u>

and that integer is positive and not greater than the number of elements in the list, then the resulting value is the list element with that integer as index, where element indices begin with one and increment by one;

(b) if the value of the subscripting **expression** is of type list, then the resulting value is the list of values obtained by **successively** applying each element of the subscripting list to the simple primary;

(c) otherwise, the result is not defined.

(3) If the value of the simple primary is of type string, then

(a) if the value of the subscripting expression is of type integer and that integer is positive and not greater than the number of characters in the string, then that integer is used as an index to select a string character, and the resulting value is an encoding of that character of type integer;

(b) if the value of the subscripting expression is a list of integers, all satisfying the bounds conditions of (a), then the value of the result is a string consisting of the sequence of characters obtained by successively using each integer in the list as a subscript;

(c) otherwise, the result is not defined.

Examples

    3   "abc"   get   { 1, { 2, 3 }, 17 }   (a+b)

In the following examples, all those on the same line have identical values.

{ 1, 2 }[1]	1	{ 2,1 }[2]
{ 1, { 2, 3 } }[2]	{ 2, 3 }	{ 1, 2, 3 }[{ 2, 3 }]
{ 1, 2, 3 }[{ 1, { 2, 3 } }]	{ 1, { 2, 3 } }	
"ABC"[1]	193	"(A)"[{ 2 }][1]
"abc"[2 3]	"bc"	{ {"bc" }[1][1]

Comment

In MUTANT 0.5, lists are considered linear sequences. The operation of subscripting of lists has been extended from selection to the construction of general sublists. Subscripting has similarly been extended to provide a substring operation.

B.2.e <u>Case Expressions</u>

<u>syntax</u>

(s-primary)	::=	(case head) (v-expression))	(59)
(case head)	::=	(case index) ((v-expression) ;	(75)
		(case head) (v-expression) ;	(76)
(case index)	::=	[(v-expression)]	(77)

<u>Semantics</u>

A case expression consists of a case index followed by a sequence of
value-expressions. In the evaluation of a case expression, the value of the
expression in the case index is determined. If that value is of type <u>integer</u>
and is positive and not greater than the number of expressions in the sequence,
then that integer is used as an index to select an expression for evalu-
ation, and the value of that expression is the value of the case expression.
Otherwise, the result is not defined. A case expression **always** has a
value.

Examples

[n] (3; 2; 1)

[opcode] (0 → **acc; acc+a → acc;** ace-a → **acc;** a → pc)

[(x=0) + 1] ("x is non-zero"; "x is zero")

<u>Comment</u>

Case expressions are generalizations of **AIGOL** 60's conditional
expressions and **conditional** statements, which have not been specially
distinguished in MUTANT **0.5.**

B.2.f <u>Cell Designators</u>

<u>syntax</u>

(cell id)	::=	(cell id *)	(46)
(cell id *)	::=	(identifier)	(47)
		(cell id *) [(v-expression)]	(48)
		(cell id *).	(49)

<u>Semantics</u>

MUTANT 0.5 provides named cells in which values may be stored and also
named **values** which are not associated with storage cells. A cell designator
is used in the formation of either a primary **(B.2.h),** in which case it desig-
nates a value, or an assignment **(B.2.k),** in which case it designates a cell
or subcell. As explained in section **B.2.b,** the structure of a cell is determined

dynamically by the structure of its contained value; thus the interpretation of a (sub)ceU designator is dependent upon the concurrent contents of the cell.

If the cell designator is used in the formation of an assignment, then the named (sub)cell is determined as follows:

(1) If the designator is not subscripted or dotted, then by the rules governing the scope of identifiers (B.2.b), that identifier must name a declared cell and it designates that cell; otherwise, the result is not defined.

(2) If the cell designator terminates with a subscript, then the contents of the cell named by that simpler cell designator obtained by deleting the rightmost subscript is determined, and the subscripting expression is evaluated. If the cell contents is not a value of type list or if the subscripting expression is not of type integer, the result is not defined. If the value of that integer is positive and not greater than the number of elements in the list, the designated cell is that subcell containing the list element selected by use of that integer as an index.

(3) If the cell designator terminates with a dot, then the value named by the cell designator obtained by deleting the rightmost dot is determined according to the algorithm of the next paragraph. If that value is of type name, the computation designated by that value is activated to determine the designated cell (B.2.g). Otherwise, the result is not defined.

If the cell designator is used in the formation of a primary, then the named (sub)value is determined as follows:

(1) If the cell designator is not subscripted or dotted, then
   (a) if, by the rules governing the scope of identifiers, the identifier names a value (B.2.b), a controlled value (B.2.l), or a procedure formal parameter value (B.2.m), then the value of the cell designator is the named value;
   (b) if, by the rules of scope, the identifier names a cell, then the value of the cell designator is the concurrent value of the contents of the named cell.

(2) If the cell designator terminates with a subscript, then the value named by the cell designator   obtained by deleting the rightmost

    subscript is determined. The subscripting expression is evaluated
and used as an index operating on the previously obtained value to
produce a resulting new value as described in section **B.2.d.**

(3) If the cell designator terminates with a dot, then the value named
by the cell designator obtained by deleting the rightmost .dot
is determined. If that value is of type <u>name</u>, the computation desig-
nated by that value is activated to **determine** the designated cell
(B.2.g), and the resulting value is the value contained in that cell.
Otherwise, the result is not defined.   '

Thus in the cases in which a cell designator is valid in the formation of
either a primary or an assignment, the value in the first case corresponds
to the contents of the cell named in the second case, but more general
indexing is allowed in the formation of primaries.

<u>Examples</u>

    a   b[1]   a[2][x[3]]
    pointer.   x[i]·   x[2]·[1]

B.2.g <u>References</u>

<u>syntax</u>

    (reference)   ::= (reference *)   (50)

    (reference *)   ::= ℓ (identifier)   (51)

                  (reference *) [(v-expression)]   (52)

<u>Semantics</u>

    Values of type <u>name,</u> which are computational processes for determining
cell names, are designated by references. Thus every reference has a value
of type <u>name</u>. Upon activation of such a process **(B.2.f),** the resulting cell
name is determined by **analysis,** as described in section **B.2.f,** of the cell
designator obtained by deleting the "ℓ" in the formulation of the reference.

<u>Examples</u>

    ℓa ℓb ℓa[x+y][1]

<u>Comment</u>

References provide an explicit method of processing cell names as
values. They **are** intended primarily for use as "pointers" to complex
data structures and as procedure actual parameters. References are
defined as computational processes rather than actual cell names for
technical reasons; **EULER** [Wirth **65a]** demonstrates an alternative

approach using cell names. Unlike MUTANT, MUTANT 0.5 requires the **programmer** to distinguish between cell name and value.

B.2.h <u>primaries</u>

<u>syntax</u>

⟨**primary**⟩	:.'=	(primary *)	(33)
		(prefix) (primary)	(34)
		(infix) / (primary)	(35)
⟨**primary ***⟩	::=	(cell)	(43)
		(reference)	(44)
		⟨**s-primary**⟩	(45)
(prefix)	::=	#	(36)
		<u>type</u> ˉ	(42)
		<u>abs</u>	(39)
		<u>neg</u>	(40)
		¬	(37)
		<u>list</u>	(38)
		<u>put</u>	(41)

<u>Semantics</u>

A **primary** always has a value. The value of a primary without prefix or infix operators is the value of the corresponding cell designator, reference, or simple primary.

A prefix operator designates a partial function of one argument; the value of the corresponding primary is obtained by evaluation of the operand followed by the application of that function. If the following rules do not specify the resulting value, then the result is not defined.

(1) If the operator is "#" and the operand is of type <u>list</u> or <u>string</u>, the result is of type <u>integer</u> and is the number of top level elements in the list or string.

(2) If the operator is "<u>type</u>", the result is of type <u>integer</u> and is an encoding of the type of the operand.

(3) Otherwise the operator is applied recursively according to the following algorithm:

  (a) If the type of the operand is not <u>list</u>, then the result is defined if the operator and **operand type** correspond to one of the following table entries:

Operator	Operand Type	Result Type
abs	integer	integer
neg	integer	integer
⌐	integer	integer
list	integer	list
put	string	string

The first three are numeric operators which may be defined.
by the following λ-expressions [Land 64]:

abs = λx. <u>if</u> x ≥ 0 <u>then</u> x else -x

neg = λx. -x

⌐ = λx. <u>if</u> x = 0 <u>then</u> 1 else 0 .

The operator "<u>list</u>" produces a list of elements with unspecified **value; the number** of elements is the maximum of the operand value and 0. The operator "<u>put</u>" is an identity function with the side effect of writing a carriage return followed by the operand onto the sequential system output stream.

(b) If the type of the operand is <u>list</u>, then the result is a value of type <u>list</u>, the elements of which are the values obtained by applying the operator to each element (sequentially in the case of "<u>put</u>") of the list, if all such elements are defined.

(c) Otherwise, the result is not defined.

An infix operator designates a partial function of two arguments as described in section **B.2.i.** In the application of an infix operator to a primary, the primary is first evaluated. If the value obtained is not of type <u>list</u>, the result is not defined. Otherwise, the value of the primary is obtained as follows:

(1) An initial value is chosen according to the operator **from** the following table:

Operator	Initial Value
+, -, V	0
⊗, +, m<u>od,</u> A	1
=, ≠, <, ≤, >, ≥	not defined
base	not defined
⌐	" " or { } *

* The empty string is chosen unless the first list element is a **list.**

(2) Beginning with that initial value as an intermediate result, the
operator is applied to the intermediate result and a list element
to produce a new intermediate result.

(3) The resulting value is the value of the intermediate result after
each list element, chosen in sequence, has been used as indicated
in (2).

Thus the value of the primary so obtained is an accumulation, relative
to the operator, over the entire list.

Examples

$$a \qquad \{ a, x \} \qquad \{ \$ \, Y \, I \, x{+}z \rightarrow y \} \qquad z[2]$$

$$\underline{abs} \, x \qquad \text{put}ITLE \text{ "} \qquad \underline{list} \, \{ 1, \{2,2\} \}$$

In the following examples, all those on the same line have identical values.

# { 1, 2, 3 }	3
# { 1, { 2, 3 } }	2
¬ { 1, 0, 1 }	{ 0, 1, 0 }
neg { 1, { 2, 3 } }	{ neg 1, { neg 2, neg 3 } }
type 0 = type "0"	0 .
+ / { 1, 2, 3 }	6
| / { "a", "b", "c" }	"abc"
| / { { 1, 2 }, { 3, 4 } }	{ 1, 2, 3, 4 }

Comment

The extension of the definition of prefix operators in MUTANT 0.5 is
a slight generalization of Iverson's extension of such operators to
vectors and matrices. Accumulation over a list with respect to an infix
operator corresponds to Iverson's reduction [Iver 62].

B.2.i Simple Expressions .

syntax

(s-expression)	::=	(s-expression *)	(15)
⟨s-expression *⟩	::=	(primary)	(16)
		(s-expression *) (infix) (primary)	(17)
(infix)	::=	|	(32)
		+	(18)
		-	(19)
		⊗	(20)
		+	(21)

$$mod \hspace{4cm} (22)$$
$$= \hspace{4.2cm} (24)$$
$$\neq \hspace{4.2cm} (25)$$
$$> \hspace{4.2cm} (26)$$
$$\geqq \hspace{4.2cm} (27)$$
$$< \hspace{4.2cm} (28)$$
$$6 \hspace{4.2cm} (29)$$
$$A \hspace{4.2cm} (30)$$
$$\mathbf{V} \hspace{4.2cm} (31)$$
$$\underline{\mathbf{base}} \hspace{3.8cm} (32)$$

Semantics

Every simple expression has a value. The value of a simple expression without an infix operator is the value of the corresponding primary.

An infix operator designates a partial function of two arguments; the value of the corresponding simple **expression** is obtained by evaluating the left operand, then evaluating the right operand, and then applying that function to the operand values. If the·rules below do not specify the resulting value, then the result is not defined.

(1) If the operator is "|" and

    (a) if both operand values are of type <u>list</u>, then the resulting value is of type <u>list</u> and is obtained by appending in sequence the list elements of the right operand to the list value of the left operand;

    (b) if both operand values **are** of type <u>string</u>, then the resulting value is of type **<u>string</u>** and is obtained by concatenation of the two operand values, taken in order.

(2) Otherwise the operator is applied recursively according to the following algorithm.

    (a) If the type of neither operand is <u>list</u>, then the result is defined if the operator and operand types correspond to one of the following table entries:

Operator	Type of Operands	Result Type
+, -, ⊗	<u>integer</u>	<u>integer</u>
÷, <u>mod</u>	<u>integer</u>	<u>integer</u>
=, ≠, >, ≥, <, ≤	<u>integer</u>	<u>integer</u>
∧, ∨	<u>integer</u>	<u>integer</u>
<u>base</u>	<u>integer</u>	<u>string</u>

The operators "**+**", "**-**", and "**⊗**" designate the mathematical functions of integral addition, subtraction, and multiplication respectively. The operators "**÷**" and "<u>mod</u>" are not defined if the value of the right operand is 0. Otherwise, they are defined for integral operands by the following h-expressions, using real division and Iverson's floor and ceiling operators [Iver 62]:

$$\div = \lambda(x,y). \text{ if } x \otimes y \geqq 0 \underline{\text{then }} \lfloor x/y \rfloor \text{ else } \lceil x/y \rceil$$

$$\underline{\text{mod}} = \lambda(x,y). \; x - y \otimes (x \div y)$$

The relational operators have integral value 1 if the mathematical relation on the integers is satisfied and value 0 otherwise.

The operators "∧" and "∨" may be defined for integral operands by the following h-expressions:

$$\mathbf{\wedge} = \lambda(x,y). \; \underline{\text{if }} x = 0 \text{ then } 0 \text{ else if } y = 0 \underline{\text{then }} 0 \underline{\text{else }} 1$$

$$\vee = \lambda(x,y). \; \underline{\text{if }} x \neq 0 \underline{\text{then }} 1 \text{ else if } y \neq 0 \underline{\text{then }} 1 \underline{\text{else }} 0$$

The operator "<u>base</u>" produces a string, the characters of which are a sequence of digits constituting a representation of the left operand to the base specified by the right operand.

(b) If the type of exactly one operand is <u>list</u>, the result is a value of type <u>list</u>, the elements of which are the values obtained by sequential application of the operator to the non-list operand and each element of the list operand (taken in the original order), if all such elements are defined.-

(c) If the type of both operands is <u>list</u>, the result is a value of type **list.** The number of **elements in** that list is the minimum of the numbers of elements in the operand lists; the resulting list elements are obtained by sequential application of the operator to corresponding elements of the operand lists (taken in the original order), if all such elements **are** defined.

All infix operators have equal precedence, and the association of operands is from the left.

<u>Examples</u>

    3   a **+** b   c ⊗ <u>abs</u> x   a **+** b **-** c   a ∧ (b ∨ c)

In the following examples, all those on the **same** line have identical values:

    3 **+** 4 **-** 1   3 ⊗ 2   13 ÷ 2   13 <u>mod</u> 7   6
    3 > 4   1 **-** 2 **+** 1   (3 = 3) **-** 1   0
    "abc" | "def"   "abcdef"

{ 1, 2 }|{ "2", { 2} }   { 1, 2, "2", { 2 } }
2 ⊗ { 0, 1, 2 }   { 0, 2, 4 }   { 4, 6, 8 } ⎯ 4
{ 1, 2, 3 } ⊗ { 3, 2, 1 }   { 3, 4, 3 }
15{base 2}{ 2, {8}, 4 }165 } + { 0, 1, 2, 3 }   { { 1, 2 }, { 4, 5 }, 7 }
                  10,   }   { "1111", "17", "15", "F" }

Comment

The extension of infix operators follows Iverson [Iver 62]. It corresponds to both scalar and vector operation in ordinary vector arithmetic.

B.2.j Segments

syntax

        (v-expression *) ::= (segment)   (6)
        (segment)   ::= (s-expression)   (12)
                                (s-expression) _ (s-expression)   (13)
                                (s-expression) _ (s-expression) _ (s-expression) (14)

Semantics

        A segment always has a value. The value of a segment without the " " operator is the value of the corresponding simple expression.

        'Otherwise, the value of the first (leftmost) simple expression is called the initial value; of the second, the limit value; and of the third (if present), the step value. The value of the segment is obtained by the following process:

  (1) All of the simple expressions are evaluated in the order of appearance; if the step value is not explicitly provided, it is taken to be the integer 1.

  (2) If the values so obtained are all of type integer, then the result is a value of type list. Otherwise, the result is not defined.

    (a) If the step value is positive, the elements of the list are all those integers, ordered in algebraically increasing value,' which are obtained by adding non-negative integral multiples of the step value to the initial value and which are not greater than the limit value.

    (b) If the step value is negative, the elements of the list are all those integers, ordered in algebraically decreasing value, which are obtained by adding non-negative integral multiples of the step value and which are not less than the limit value.

(c) Otherwise, the result is not defined.

Examples

    1   n   2 '_ #S-1   { 1, 2, 3 }   0

In the following **examples**, all those on the same line have identical values.

    1 _ 3   1 _ 3 _ 1   { 1, 2, 3 }

    2   10 4   2 _ 13 _ 4   { 2, 6, 10 }

    3 _ 1 _ <u>neg</u> 1   { 3, 2, 1 }

    1   0   2 _4 _ <u>neg</u>   { }

B.2.k <u>Assignments</u>

Syntax

    ⟨ **v-ex**pression *⟩ ::= (v-expression *⟩ → (cell)   (8)

Semantics

    Assignments serve to assign values to cells. In the evaluation of an assignment, the value of the expression to the left of the "→" is obtained, and then the (sub)cell named by the cell designator is determined as described in section **B.2.f.** If both these'processes produce results which are defined, the computed value is assigned to the designated (sub)cell. Such assignment may dynamically change the structure of the cell.

    Every assignment has a value, which is the value of the expression to the left of the arrow.

Examples

    0 → a   [index]⟨ a+b; a-b) → p[2][1]

    d·[1_n 1 → c·[3]   0 → x → y → z

B.2.1 <u>Iterative Statements</u>

<u>Syntax</u>   -

(s-primary *⟩ ::= (for head) }		(60)
(while head) }		(61)
(for/while head) }		(62)
-(for head) ::= (begin) (for set) (g-expression)		(78)
(for set) :.'= (for set *⟩ :		(81)
(for set *⟩ ::= (identifier) ε (v-expression)		(82)
(while head) ::= (begin) (while cdn) (g-expression)		(79)
(while cdn) ::= (while ') :		(85)

```
(while ')        ::= (while) (q-clause)                                   (84)
(while)          ::= *                                                    (83)
(q-clause)       ::= (v-expression) =>                                    (4)
(for/while head)::= (begin) (for set) (while cdn) (g-expression)          (80)
```

Semantics

Iterative expressions provide for 'controlled repetitive evaluation of a general expression, which in each of the various forms of the iterative expression is called the controlled expression. Such an expression may conditionally fail to have a value. The value of every iterative expression, if defined, is of type list; the elements of that list are, in order, the successive values obtained from those evaluations of the controlled expression producing values. A declaration may be included in the heading of any iterative expression; the scope of the identifiers in such a declaration is the iterative expression.

For-iterative expressions specify iteration over a list. The evaluation of such an expression proceeds as follows:

(1) Any declarations in the heading are processed as described in section B.2.b.

(2) The value-expression of the for-set is evaluated. If the resulting value is not of type list, the result is not defined.

(3) With the identifier of the for-set naming a value of an element of the list thus obtained, the controlled expression is evaluated. That identifier is said to designate a controlled value; it is implicitly declared by its appearance in the for-set, and its scope is the controlled expression. The list element values named are successively taken in order over the entire list value.

(4) The final value of the iterative expression is a list as specified in the preceding paragraph.

While-iterative expressions specify repeated evaluation of the controlled expression as long as a specified condition holds. The evaluation of such an expression proceeds as follows:

(1) Any declarations in the heading are processed as described in section B.2.b.

(2) The value-expression of the qualifying clause contained in the while-condition is evaluated. If the resulting value is not of type integer,

the result is not defined. If that value is 0, evaluation of the
iterative expression is terminated, and its final value is a list
as specified above. Otherwise, the controlled expression is evaluated,
and the step is repeated.

For/while-iterative expressions specify iteration over a list as
long as a specified condition holds. They are processed as described for
for-iterative expressions with the following exceptions:

(1) The scope of the identifier designating the controlled value is
extended to include the while-condition.

(2) Before each evaluation of the controlled expression, the value-expres-
sion of the qualifying clause contained in the while-condition is
evaluated. If the resulting value is not of type integer, the result is
not defined. If that value is 0, evaluation of the iterative expression
is terminated, and its value is the list of values obtained to that point.
Otherwise, processing continues with evaluation of the controlled ex-
pression.

Examples

$\{\ i\ \epsilon\ 1\ n\ \ :\ \ S + (i \otimes i) \to S\ \}$

$\{\ *\ abs(x1 - x2)\ >\ delta \Rightarrow\ :\ \ \{\ x2 \to x1,\ f\{x1,x2\} \to x2\ \}\ \}$

$\{\ x\ \epsilon\ table\ :\ *\ looking \Rightarrow\ :\ \ x[1]\ =\ arg \Rightarrow \{\ 0 \to looking,\ x[2]\ \}\ \}$

AU the following examples have identical values.

$\{\ x\ \epsilon\ 2\_10\ :\ \ (x\ mod\ 2)\ =\ 0 \Rightarrow x\ \}$

$\{\ \$\ x\ |\ 0 \to x,\ \{\ *\ x{<}10 \Rightarrow\ :\ \ x4\text{-}2 \to x\ \}\ \}[2]$

$\{\ x\ \epsilon 2\ 100\ \_2\ :\ *\ x{\leq}10 \Rightarrow\ :\ \ x\ \}$

$\{\ 2,\ 4,\ 6,\ 8,\ 10\ \}$

Comment

The for-iterative expression provides the effect of a generalized list
mapping function. Since the controlled expression may conditionally
fail to have a value, that function can include selection.

B.2.m Procedures

syntax

⟨v-expression *⟩ ::= (procedure head) (v-expression) '	(7)
(procedure head) ::= ⟨proc head +⟩ |	(11)
⟨proc head +⟩ ::= '	(9)
⟨proc head +) (identifier)	(10)

$$\langle s\text{-primary}\rangle \quad ::= \langle\text{primary}\ *\rangle\ \langle\text{list}\rangle \tag{56}$$

<u>Semantics</u>

A procedure definition is delimited by apostrophes (') and designates a value of type <u>process</u>.

The computational process designated by a value of type <u>process</u> is activated by the evaluation of a simple primary consisting of a primary followed by a list. If the value of such a primary is not of type <u>process</u>, the result is not defined. Otherwise, the expression in the definition of the procedure corresponding to the <u>process</u> value is evaluated, subject to the rules below, and the resulting value is also the value of the simple primary. The rules governing such evaluation are the following:

(1) The identifiers appearing in the procedure head are associated, in order, with the values of the elements of the argument list. If the number of identifiers exceeds the number of list elements, the values named by the extra identifiers are not defined.. If the number of list elements exceeds the number of identifiers, the extra list elements are disregarded. Such identifiers&e said to designate procedure formal parameter values.

(2) In the application of rules of scope in the evaluation of the expression, the applicable scopes are those at the place of procedure definition, not procedure activation*

<u>Examples</u>

The following examples define and assign <u>process</u> values:

 ' | a + 1 → a ' → increment1

 ' a | a• + 1 → a• ' → increment2

 ' x y | { x+y → sum, sum+ 2}[2]' → average

The following examples indicate the activation of the above <u>process</u> values.

 increment11 }

 increment21 ℓx }

 average{ a+b-c, sum }

 <u>Comment</u>

 In MUTANT 0.5, a parameter list, which can be empty, must be associated with every procedure activation.

B.2.n <u>Expressions</u> with Value

<u>Syntax</u>

$$\langle \text{v-expression} \rangle \quad ::= \quad (\text{v-expression } *) \tag{5}$$

$$\langle \text{v-expression } * \rangle ::= (\text{segment}) \tag{6}$$

$$(\text{procedure head}) \ (\text{v-expression}) \ ' \tag{7}$$

$$(\text{v-expression } *) \rightarrow (\text{cell}) \tag{8}$$

Semantics

A value-expression, if defined, always has a value. It is the least restricted type of **expression** with such a property provided in MUTANT 0.5.

B.2.o General Expressions

syntax

$$(\text{g-expression}) \quad ::= \quad (\text{v-expression}) \tag{2}$$

$$(\text{q-clause}) \ (\text{g-expression}) \tag{3}$$

$$(\text{q-clause}) \quad ::= (\text{v-expression}) \Rightarrow \tag{4}$$

Semantics .

A general expression may conditionally fail to designate a value. If it does not contain a qualifying clause, then it has a value, and that value is identical to that of the corresponding value-expression. Otherwise, .
the value, if any, of the general expression is determined by first evaluating the expression in the leftmost qualifying clause. If that value is not of type integer, the result is not defined. If the value is 0, the general expression has no value. Otherwise, the value, if any, is that of the general expression obtained by deletion of the leftmost qualifying clause.

Examples

$$y \neq 0 \Rightarrow x \div y \qquad \qquad \text{predicate}\{x\} \Rightarrow \text{function}\{x\}$$

$$x < \text{max} \Rightarrow y > \text{min} \Rightarrow x \div y$$

Comment

In MUTANT 0.5, an unsatisfied qualifying clause gives rise to no value, not an undefined value. Thus general **expressions** can be used in contexts only in which such a property is meaningful, i.e., in the formation of list values.

B.2.p Programs

syntax

$$(\text{program}) \quad ::= \quad \underline{\text{eof}} \ \langle \text{v-expression} \rangle \ \underline{\text{eof}} \tag{1}$$

Semantics

A program is a **value-expression** delimited by end-of-file marks. The value of a program is that of the value-expression.

Examples

See section B.3.

Comment

In MUTANT **0.5,** the end-of-file marks are assumed to be supplied by the interpreting mechanism and are not normally written.

B.3 Examples

Listings produced during the compilation and execution of some sample MUTANT **0.5** programs are included as Appendix III. In these examples, comments are delimited by question marks. Selected examples are repeated below, with commentary, in the (more readable) publication character set.

B.3.1 Factorial Calculation

Program

```
{ $ factorial |
    ' n | [2 - (n=O)] ( 1; n ⊗ factorial{n-1} ) ' → factorial,
    { n ∈ 1 6 :
        put ( (n base 10) | " factorial = " | (factorial{n} base 10) )
    }
}
```

Output

```
1 factorial = 1
2 factorial = 2
3 factorial = 6 ,
4 factorial = 24
5 factorial = 120
6  factorial  =  720
```

Comment

This example corresponds closely to McKeeman's Example 1 [McKee 66, p. 75]. The following is a similar ALGOL **60** program, which assumes a suitable write statement.

```
begin integer n;
    integer procedure factorial(n); value n; integer n;
        factorial := if n=0 then 1 else n ⊗ factorial(n-1);
    for n := 1 step 1 until 6 do
        write( n, " factorial = ", factorial(n) )
end
```

In the **MUTANT** 0.5 program, the **process** value (delimited by apostrophes)
assigned to the cell "factorial" gives the usual **recursive** definition of
the factorial function. The parameter **"n"** is used to **compute** a case index
for selection of one of two expressions to be evaluated. Thus case expres-
sions are generalizations of **ALGOL** 60's conditional expressions and state-
ments. Note that in **MUTANT** 0.5, the **expression** "n=0" has integral value
1 if the value of n is zero and value 0 otherwise. The expression "1_6" is
equivalent to the expression "{ 1, 2, 3, 4, 5, 6 }", and iteration over
each element of that list is specified.

B.3.2 Extended Factorial Calculation

Program

```
    { $ factorial prod |
        {' n | [2-(n=0)]( 1; n ⊗ factorial[1]{n-1} ) ',
         ' n | ⊗ / (1_n) ',
         ' n | prod{ 1_n }'
        } → factorial,
        ' L |[2 - (#L=1)] ( L[1];
          prod{ L[1   #L+2] } ⊗ prod{ L[#L+2+1 _ #L]) ' → prod,
        { i ∈ 1_3 :
           { put " ", put ("method "| (i base 10)),
              { n ∈ 1_8 :
                  put ( (n base 10)|" factorial = "|(factorial[i]{n} base 10) )
              }
           }
        }
    }
```

Output

```
    method 1
    1 factorial = 1
    2 factorial = 2
       • • •
    8 factorial = 40320


    method 2
    1 factorial = 1
       •  •  •
```

<u>Comment</u>

In this example, the value assigned to the cell "factorial" is a list
of three <u>process</u> values giving possible definitions of the factorial function.
The first is the recursive computation of the previous example. The second
is an example of Iverson's reduction, in which the multiplication operator
is used to reduce a vector (list) of the first n positive integers. The
third process applies the auxiliary function "prod" to the **same vector.**
"prod" designates a process intended to illustrate one possible hardware
implementation of multiplicative reduction in which, recursively, the'vector
is bisected and reduction applied to each part. Note the use of a list-valued
subscript to select a **sublist,** which in turn is used as a procedure parameter.

B.3.3 <u>Further Examples from MUTANT</u>

<u>Program</u>

```
put( ( + / ({1,2,3} ⊗{3,2,1} ) ) base 10 )
```

<u>Output</u>

```
        10
```

<u>Program</u>

```
    { $ perm |
        ' x | [2 - (#x=1)]
           ( {x}; .
           |/{ i ∈ 1 _ #x :
                 { t ∈ perm{ x[1 _ i-1]|x[i+1 _ #x] } :  x[i_i]|t }
                 」
           ) ' → perm,
        { test ∈ { "a", "ab", "abc", "abcd" } :   put perm{test}
    3
```

<u>output</u>

```
        a
        ab
        ba
        abc
        acb
        bac
        bca
        cab
        cba
         •  •  •
```

<u>Comment</u>

These programs for computation of inner product **and** permutations of string characters or list elements are MUTANT 0.5 versions of **McKeeman's** Examples 2 and 4 [McKee 66, pp. 77-78]; they are presented'mainly for comparison.

B.3.4 <u>A prime Sieve</u>

<u>Program</u>

```
{ $ primesieve
   ( ' n | { $ L t | 2_n → L,
           { * #L≠0 => :
                { L[1] → t, { i ∈ L : imodt ≠ 0 => i } 3 L }[1]
           } }[2] '
   ) |
   {n ∈ {  25,  250}:
      { put ("primes in 2 to "|(n base 10)|":"),
        put (primesieve{n} base 10)
      }
   }
}
```

<u>Output</u>

```
primes in 2 to 25:
2
3
5
7
11  .
13
17
19
23 .

primes in 2 to 250:
2

   •  •  •
```

Comment

This program is an adaption of the sieve of .Eratosthenes to the com-
putation of all prime integers not exceeding a given integer. "primesieve"
names a **process** value. In that process, a list of the integers from 2 to
the given value is assigned to the cell named **"L".** While the length of that
list is non-zero, the first element of the list is saved and then the list
is replaced by a new list consisting of all the former list elements not
multiples of the first element. Note that the saved value is selected as
the value of the controlled expression in the while-iterative **expression**
by the second subscript **"[1]";** thus the value of the entire iterative
expression is a list of the primes so saved. The subscript "[2]" selects
that list as the value of, the procedure. Also note the use of the extended
"put" and "base" operators.

B.3.5 Other Examples

Also included in Appendix III are programs illustrating the following:
 (1) a slightly different permutation generator;
 (2) a set of algorithms adapted from **Pohl's** graph package [Pohl 67] for
    computing the reachability matrix and maximal strongly connected **sub-**
    graphs of a graph from its connectivity matrix;
 (3) an integer square root routine based on **Newton's** method.

C. Implementation Techniques

An experimental processing system for the language MUTANT 0.5 was developed. It consists of a compiler, which translates MUTANT 0.5 programs to a compact internal string code based upon Polish suffix notation, and an interpreter, which performs processing as directed by such strings. The processing system was implemented on the IBM System/360 hardware; it functions in the environment provided by the PL360 system [Wirth 67d]. In addition, an existing syntactic analysis program, written in Burroughs B5500 Extended ALGOL, was modified for use as an aid in developing the compiler.

C.1 The Syntax Processor (see Appendix IV for listing)

The syntax processor is an extension of a B5500 Extended ALGOL program originally developed-by Professor Niklaus Wirth at Stanford. Blocks B1 and B2 were taken from that program without significant modification. Block B1 establishes the precedence matrix as described by Wirth and Weber [Wirth 65a], using partial word operations for storage efficiency. Block B2 establishes the precedence functions using Wirth's algorithm [Wirth 65b].

Additional pre- and post-processing was added to produce punched tables in the PL360 syntax suitable for direct insertion into the compiler source deck. This processing includes:

(1) classification and sorting (according to the IBM EBCDIC collating sequence) of the terminal symbols of the syntax,

(2) assigning internal codes to the symbols,

(3) encoding and sorting the productions of the grammar,

(4) formatting the required tables.

A B5500 ALGOL program was chosen for modification because of the relatively powerful format capabilities provided.

Those cards at the beginning of the compiler (Appendix V) lacking "CMP" in the sequence field were produced by the syntax processing program. (Strictly, they are translations from such cards produced for a previous version of PL360, translated by a conversion program). The availability of this syntax processing program greatly facilitated modification of the syntax of MUTANT 0.5 as the system developed.

C.1.1 Symbol Recognition Tables

The following tables produced by the syntax processor are used by the

compiler procedure **INSYMBOL** in **recognizing** the terminal symbols of the
language:

    CCODES   a translation table which maps' characters occurring in the
input stream into either their internal symbol codes or
entries into other tables.

    BREAK   a table of partitioning indices classifying characters, by
their translation codes, as

        (1) single character terminal symbols,

        (2) characters possibly forming character pair terminal
symbols, or

        (3) characters initiating identifiers, numbers, strings,
or **comments.**

    PAIRTAB   , a sorted table of special character pairs forming terminal
symbols.

    RSVD   **a table** of entry indices into the reserved word table.

    RSVWD   a table of reserved words, ordered by length and, within
each length group, alphabetically.

C.1.2 Parsing Tables

    The following tables produced by the syntax processor are used by the
compiler% syntactic analysis routine in parsing input strings:

    F, G   tables of precedence functions for the **symbols of** the vocab-
ulary.

    PLIM   a **table** of entry indices into the table **RIGHTPART** according
to the leftmost symbol of the production right part.

    RIGIDPART   a table of production right parts, exclusive of leftmost
symbol, ordered by the **(omitted)** leftmost symbol.

    LEFTPART   a table of corresponding production left parts.

    RULE   a permutation vector giving the original interpretation rule
number for each of the (reordered) productions.

C.2 The Compiler (see Appendix **V** for listing)

    The **compiler** is a syntax directed, one-pass translator using the prin-
ciples of semantic analysis controlled by **a** simple 'precedence syntactic
analysis. The general organization of such **translators** described by Wirth
[Wirth **65a, 67c,** Shaw **66**] has been adopted. In addition to the "value
stack", information about previously scanned symbols is collected in an

identifier table and a separate (nested) table used in the processing of
case expressions.

The compiler is written in PL360 [Wirth 67c]. Since analysis is table
driven, the syntax processor was designed to produce tables which could be
efficiently scanned (see section C.1). In particular, binary search 'is used
for the table of special character pairs, while entries into the tables
of reserved words and production right parts are controlled by key trans-
formations on the identifier length and leftmost symbol of the right part
respectively [Iver 62]. The table of declared identifiers is organized to
reflect the block structure of the language [Shaw 66].

C.3 The Interpreter (see Appendix VI for listing)

   The interpreter is a program simulating a machine for processing the
Polish suffix string-code produced by the compiler from MUTANT 0.5 source
programs. It is basically similar to well-described proposals for EULER
machines [Wirth 65a, Weber 67]. In particular, it incorporates:

 (1) the traditional ALGOL 60 stack organization and addressing structure   .
     [Rand 64],
 (2) organization of composite data structures based on descriptor logic
     similar to that of the Burroughs B5500, and
 (3) data-directed interpretation of operators.

Data storage for the interpreter is organized into a push-down stack and a
free storage area. Composite data structures are implemented as collections
of cells, defined by a descriptor scheme, in the free storage area. In the
interpretation of a 'Polish suffix string, syllables of that string are sequen-
tially scanned. Action specified by most such syllables falls into one of the
following-classes:

 (1) branching within the program string, possibly with analysis and
     modification of the top stack elements;
 (2) fetching of values to the top of the stack, either from the program
     string or, under the direction of existing stack entries, from free
     storage;
 (3) replacing a number of the top stack elements by a function of those
     elements, including constructing from them a composite data structure
     in free storage and placing a new descriptor in the stack;
 (4) storing a stack value into a composite data structure as directed by
     other stack entries.

The interpreter is written in PL360 [Wirth 67c]. Its general organization resembles the EULER interpreter written for the Burroughs B5500 by Wirth and McKeeman [Wirth 65a]. A machine cell (System/360 double word) containing a list or string value actually contains a descriptor, which includes a type code and the base address and length of a contiguous block of machine cells that contain the values of the list elements or string characters. A compacting garbage collection scheme originally proposed by Weber [Wirth 65a] is used, so that available free storage always consists of a single contiguous area. Data-directed recursive application of 'certain operators is controlled by the interpreter procedures MAP, MAPLEFT, MAPRIGHT, and MAPBOTH.

D. Use of the MUTANT 0.5 Processor,

D.1 Language Restrictions

The following restrictions are imposed upon programs to be processed by the experimental system:

(1) The hardware character set (Appendix I) is used; thus the reserved words of that character set cannot be used as identifiers, and spaces are significant in delimiting adjacent reserved words or identifiers.

(2) No limit is imposed on the length of identifiers, but only the first eight characters are used in distinguishing them.

(3) No single string constant can consist of more than 256 characters.

(4) Arithmetic operations are defined by the IBM System/360 hardware. In particular, addition, subtraction, and multiplication are actually the corresponding operations in the ring of integers modulo 2^{32} (with appropriate interpretation of negative numbers).

In addition, certain valid MUTANT 0.5 programs can cause overflow of compiler tables or object code instruction fields (see D.3).

D.2 Operating Instructions

The MUTANT 0.5 compiler and interpreter must be compiled and the object programs placed in the PL360 system library by the use of SYSTUP [Wirth 67d]. In systems to date, these programs have been named MUTANT 1 and MUTANT 2 respectively. The compiled MUTANT 0.5 program is written by the compiler onto logical device 8, which must be appropriately defined, and is read by the interpreter initialization process. The following deck set-up (within a PL360 batch) is then required:

```
    %MUTANT 1
          (MUTANT 0.5 source program)
    %MUTANT 2
          (data, if any)
    %EOF
```

D.3 Compilation Listing

The source program is listed as it is compiled. The hexadecimal numbers printed to the left of each line indicate the number of bytes of object program produced prior to analysis of that line. Under the RASP spooling system, the printed time is primarily a measure of the time required to load

the compiler or interpreter.

The following messages correspond to errors detected by the compiler. A vertical bar is printed beneath the character being scanned at the point of error recognition, and compilation is terminated. A possible error recovery technique has been described by Wirth [Wirth 67c].

SYNTAX	A syntax error (according to the grammar of Appendix II) was detected.
PROG OVFL	A program assembly area in the compiler overflowed.
BRANCHADDR OVFL	The relative address generated for an implicit branch overflowed the allocated instruction field.
CASE TABLE OVFL	An internal table used in processing case expressions overflowed.
UNDCL ID	An undeclared identifier was used.
IMPROPER ID	An identifier associated only with a value (named value, procedure parameter value, or controlled value) was used in a context (assignmerit or reference formation) in which an identifier associated with a cell is required.

E. <u>Reflections on Language Design</u>

The present MUTANT 0.5 system would benefit 'substantially from further development. There are a number of rough edges in the language definition and several known errors in the design of the interpreter. Some of the more unpleasant features of the language reflect oversights or poor decisions in the system design, and no conceptual problems arise in their elimination. Some examples are cited in section E.3.e. Other rough edges are related to fundamental questions about the design and use of MUTANT-like languages; some progress in resolving these questions should be made before further detailed implementation work is justifiable. The remainder of this section is an attempt to characterize such languages, to consider their potential as practical programming tools, and to discuss some specific issues raised by the definition and implementation of MUTANT 0.5.

E.1 <u>MUTANT-like Programming Languages</u>

In the past few years, several languages which attempt to extend and simplify ALGOL 60 [Naur 63] have been designed and experimentally implemented at Stanford. The two most directly of interest, in addition to MUTANT 0.5, are Wirth and Weber's EULER [Wirth 65a] and McKeeman's MUTANT [McKee 66]; the following remarks should also be applicable in part to similar languages, such as LISP 2 [Abra 66] and the AED family [Ross 66], being developed elsewhere. To a first approximation, theselanguages may be considered ALGOL 60 extended to allow various types of list (ordered set) manipulation. In particular, such languages include the following features:

(1) Programs consist of conditionally selected sequences of imperatives.
(2) Named variables are provided in the context of a block and declaration structure.
(3) An assignment operator is provided.
(4) Structured values may be created and manipulated dynamically, and the format of these structures need not be defined prior to program execution.
(5) Definitions of certain operators are extended to be dependent upon dynamic analysis of the operands.

E.2 <u>Practical Applications</u>

For purposes of this analysis, problems currently amenable to computer

attack fall into the following three broad catagories:

(1) Problems in which the natural data structures are simple, fixed, and reasonably well reflected in the storage'organization and operation set of existing machines. Many problems of classical numerical analysis fall in this catagory. In many cases, efficient use of the machine hardware is essential.

(2) Problems in which the natural data structures are complex but pre-determined and well-defined. Processing requirements may or may not be easily satisfied by machine facilities. Much of systems programming and business data processing belongs in this catagory. Again a premium Is often placed on efficiency.

(3) Problems in which the natural data structures are complex and cannot be predefined. Examples are found in such areas as artificial intel-ligence, general symbol manipulation, and graphical data processing. In most cases, a moderate amount of avoidable system overhead is acceptable if it significantly increases flexibility and ease of programming in the system.

Experience with MUTANT 0.5 indicates that algorithms for solving problems in the first and third catagories can be naturally expressed in a MUTANT-like language. Since the structure of values is arbitrary in such a language, a uniform scheme (e.g., indexing) must be used to name sub-structures. Algorithms in the second class, however, can usually be ex-pressed more clearly in the notation advocated by Wirth [Wirth 66a, 67a] in connection with record classes, a notation which demands static spec-ification of possible data structures.

Experience also suggests that a simple translator-interpreter mech-anism for a MUTANT-like language is unable to achieve the high efficiency required in applications in the first two areas. Translator recognition of, and optimization for, simple cases is, in fact, precluded by the lack of a descriptive declaration facility in EULER and MUTANT. Such a declaration structure, possibly including the record concept, could be used to advan-tage only by a considerably more sophisticated translator; even then, it is not clear that a great deal of efficiency can be gained without sacrifice of all dynamic features. Thus it appears that, with current machine designs, MUTANT-like languages are of potential practical value in the third problem area above and that they may be fairly evaluated in the context of such

problems.

E.3 Language Design

Presented below are some of the issues which were found to be critical in the design and use of the MUTANT 0.5 system. Some of these became clear only after much of the system had been implemented, and no claim is made that many optimal, or even good, solutions were found.

E.3.a Assignment of Structured Values

In MUTANT-like languages, declarations serve to name cells but not to define their structure. Instead, structured values may be created in an arbitrary way by computation, and such values may be assigned to any named (sub)cell; at the time of assignment, that cell assumes the structure of the assigned value. Thus the structures of cells must be dynamic. The principal objections to such a scheme have been discussed by Wirth [Wirth 67a, 67b]. Briefly, they are the following:

(1) Restructuring of cells is highly implicit, generally expensive in interpretation, and deceptively simple in appearance to the programmer. Known storage allocation and referencing methods for implementation are not efficient enough, especially in the first two of the problem areas above.

(2) Subcells (subvalues) must be referenced by a fixed and uniform naming scheme (such as indexing) with little mnemonic value.'

(3) The compiler has very limited information for selecting code, type-checking, etc.

Wirth [Wirth 67a,67b] proposes to avoid these problems by assigning to each named cell a structure, possibly complex, fixed at the point of declaration. He claims that "for practical purposes this turns out to be hardly a restriction at all" [Wirth 67a, p. 3]. The claim is reasonable for programs arising in the first two problem areas above, but it is questionable as a general assertion. Among evidence to the contrary are the following points:

(1) Programs from the third problem area inherently deal with dynamic, complex, and interacting data structures. The information content of such structures can indeed be represented within a set of static data structures, but often this requires considerable bookkeeping effort on the part of the problem programmer and makes the resulting

program difficult to write, to document, and to modify or extend
without drastic revision.

(2) Experience with MUTANT 0.5 indicates that some of the most useful
and convenient features of the language generate or depend on
dynamically structured values. Notable examples are the iterative
expression and the Iverson interpretation of certain operators.

It is tempting to conclude that a desirable solution is to allow the
programmer to specify that a cell must have structures from some subset
of the set of structures of all values computable within the system. In
particular, if the specified subset contains exactly one element, the
translator is expected to check and optimize appropriately. There is some
merit in such a scheme; however, experience suggests that the effort required
to produce and adequately test such a translator using currently known tech-
niques is usually very great, even for languages much "simpler" than MUTANT
0.5. In addition, the optimization gained has often been rather disappointing.

E.3.b The Name-Value Problem

A familiar problem in the design of programming languages is dis-
tinguishing the denotation of the name of a cell and the name of the con-
tents of that cell (or more generally, the name of an expression and its
value). EULER and MUTANT 0.5 (but not MUTANT) resolve this problem by
allowing (and normally requiring) the programmer to make the distinction.
Thus in MUTANT 0.5, "a" denotes the value contained in the cell a, while
"ℓa" is the name of (address of, pointer to, etc.) the cell itself. A
concession to tradition is made in assignment; Although this is an opera-
tion between a value and a cell, MUTANT 0.5 allows, e.g.,

$$b + 3 \to a$$

in place of

$$\underline{assign} \; (\; b+3, \; \ell a \;) \; or \; b + 3 \to \ell a$$

Allowing the programmer to explicitly manipulate cell names creates
some subtle but fundamental problems in MUTANT-like languages:

(1) The role of block structure and the interpretation of declarations
is unclear, as illustrated by the following example:

$$\{ \; \$ \; a \; | \; \{ \; \$ \; b \; | \; \ell b \to a \; \}, \; 0 \to a \cdot \; \}$$.

If the second assignment is considered valid, then the cell b must
remain accessible after it can no longer be directly named; in

particular, the machine storage assigned to b cannot be reallocated after exit from the block (list) to which b is local. On the other hand, if the second assignment is considered invalid, detection of such assignments within the block and procedure structure of MUTANT-like languages becomes a surprisingly subtle problem, and no satisfactory solution was discovered.'The difficulty of the problem is indicated by the following example:

```
{ $ x y p |
    ' a |  {$b  | ℓb → a•, x → y, 0 → x }' → p,
    p{ ℓx }, { $ c | 0 → y• }
}
```

A quite similar problem arises in the assignment of values of type <u>process</u>, as indicated in the following:

```
. { $ p |
    { $ a | 10 → a, ' x | x + a ' → p },
    PC 3}
}
```

(2) Names which are meaningful at the point of creation may become meaningless at the point of use due to the dynamic structuring of cells, as shown in the example below:

```
{ $ a b | { 1, 2,3} → a, ℓa[1] → b, 0 → a, 1 → b• }
```

Such situations cannot be detected easily by an interpretation mechanism using machine addresses or equivalents as the representation of values of type name. MUTANT 0.5 effectively treats such values as parameterless procedures which return a machine address upon activation. This solution also defers evaluation of subscripts, sometimes with undesirable results. A better scheme is to construct a similar procedure after evaluation of all subscripts, but such a solution can be quite expensive.

E.3.c The Copy problem

In MUTANT 0.5, the traditional notion of assignment of values to cells has been retained. This decision has fundamental implications for the design of an interpreting mechanism implemented using a conventional digital computer. In such machines, cells have simple fixed structures,

and values are generally not accessible except as contents of such cells. As a **result,** the structured cells **(values)** of MUTANT-like languages must be implemented as collections of machine cells (values). Furthermore, since structure is dynamic in such languages, these collections must include descriptive information sufficient to identify the structure.

In interpreting the assignment of such structured values (possibly contained in named **cells)** to named cells, the question **arises** of 'how much of this collection must of logical necessity be copied upon **assignment.** For example, the interpretation mechanism must compute 3, not 0, as the value of the following expression:

{ $ a b I { 1, { 2, 3 } } } → a, a[2] → b, 0 → b[2], a[2][2] }[4]

The answer is that, if by any name and process, the contents of a machine cell can be changed, there must be at most one name (which may, however, be the value of the contents of any number of cells) through which that machine cell or its contents can be referenced. Such names are created by explicit or implicit assignment to a structured cell. Implicit assignments in **MUTANT-like** languages include use of a value as a procedure actual parameter as well as the implicit assignments within an iterative **expression.**

In the implementation of interpreters of MUTANT-like languages, assuring such uniqueness proves to be very expensive in terms of efficiency. Such implementations to date have used an interpreter based upon a pushdown **stack, manipulated** by program **operators, and** a free storage area of machine **cells, from** which structured cells are created. Uniqueness of reference to machine cells can **be guaranteed** by unconditionally copying completely every structured value as it (or a descriptor of it) is fetched to and stored from the stack. Copying is itself expensive; moreover, each copying reduces the (finite) number of machine cells in free storage available. Eventually, free storage must be restructured ("garbage collected"), and a second substantial expense is incurred. Implementations to date have, in fact, attempted to avoid some of this copying. In Wirth and **McKeeman's B5500** implementation of **EULER [Wirth 65a],** for example, values are copied only upon fetch-into the stack; as a result, in that **EULER** implementation,

expressions such as

$$a \leftarrow b \leftarrow c$$

and
$$p(\ a \leftarrow c\ )$$

are semantically disallowed if (**and** only if) c is found to contain a
structured value at the time of interpretation. An alternate approach is
to adopt a scheme of including marking **information** with **(sub)structures**
and deferring copying until it is logically demanded. In this investiga-
tion, no such scheme was discovered which seemed sufficiently attractive
(see below).

In view of the expense of copying, it is important to note that in
mostcases such action is neither anticipated nor desired by the programmer.
Furthermore, in many cases, difficult or impossible to detect during the
translation process, omission of such copying will not change any of the
final values produced (or, even more frequently, any of the output strings
written). Given the high cost of copying and associated storage management
in available machines, this observation is probably the basis of the most
fundamental objection to the practical use of MUTANT-like languages. A num-
ber of partial solutions to the copy problem are considered below.

(1) In **EULER** and MUTANT 0.5 programs, it is possible to create a value of
type **name.** This facility creates certain logical problems (see above),
but it is valuable in allowing the programmer to create references to
a named cell (and hence the contained value). In certain situations
(not necessarily obvious to the programmer), it will be more efficient
to access a value with complex structure indirectly via a reference **than**
it will be to copy the value. Such indirect reference is particularly
natural and appropriate in connection with procedure parameters. It has
several drawbacks:

(a) Each value to be indirectly referenced must first be assigned to
to some named cell.

(b) Efficiency is critically dependent upon the programmer's careful
(implementation dependent) choice of reference or value in each
situation.

(c) The programmer must be exactly aware at all times of the level of
indirectness being used.

(2) In SLIP [Weiz 63], a list-processing **language** of quite different design,

a superficially similar problem was encountered and solved by the use
of a reference counting scheme. A count of the number of valid names
referencing each relevant collection of machine cells is encoded in
that collection and dynamically adjusted. A brief examination failed
to discover a reasonably efficient adaptation suitable for MUTANT-like
languages, but further investigation might be profitable., Briefly the
difficulty seems to be that the encodings of such counts which can
be efficiently maintained are not the encodings efficiently usable in
avoiding copying.

(3) It is possible to interpret the notion of value in a manner consistent
. with any particular scheme of internal representation and strategy of
copying that is convenient for implementation. In particular, if a
cell contains a structured value in the MUTANT 0.5 sense, it is attractive
to instead consider the value of the cell to be a description of that
structured cell and its subcells. In certain situations (such as array
procedure parameters called by name in ALGOL 60) such an interpretation
is consistent with the spirit of the language and represents an efficient
implementation trick. In general, however, there are several valid ob-
jections to such an interpretation:

   (a) It is an ad hoc expedient and tends to make the semantics of a
       language dependent upon the implementation facilities which happen
       to be available.

   (b) It further confuses the distinction between the name of a cell and
       of its value.

   (c) As most naturally implemented, an embarasing lack of consistency
       arises in the meaning of the language. In particular, it is more
       convenient and efficient to reference unstructured values directly
       but structured values indirectly.

(4) Analysis of programs in various languages with an assignment operator
suggests that a significant fraction of all cells are declared and used
to preserve intermediate results and avoid repeated calculation of the
same value. Such cells are created for the purpose of naming values; the
fact that these cells (as opposed to the contained values) are structured
is of no interest or use to the programmer, for he never assigns to a
subcell. This suggests that the language should provide a facility for
naming computed values without requiring assignment to a logically

. distinguished cell. Such a facility exists for simple constant values in present languages.

MUTANT 0.5 recognizes that previously computed values may be used as such intermediate values and thus may effectively be 'constants throughout the scope of a declared name. A construct is provided to initialize at the point of declaration the value denoted by a name to a constant (which may be computed from the values denoted by names non-local to the corresponding block). Such values will be called locally constant. Since all procedure parameters in MUTANT 0.5 are effectively called by value, it is easy for the translator to check that such names are never used in the (implicit or explicit) formation of cell names.

The important fact is that such naming does not create a name by which the contents of a machine cell can be changed. Thus in the composition of the designated value, any subvalue which is a constant, either by denotation or by being locally constant in a containing block, need not be copied. The idea can be extended somewhat further than is done in MUTANT 0.5. If a value contained in a named cell is used in the computation of a locally constant value, then there are various sets of sufficient conditions, verifiable by the translator, that insure that the contained value cannot be changed within the scope of the name of the local constant. If these conditions are satisfied, it is again not necessary to copy the contained value in formation of the local constant.

The effectiveness of this solution is critically dependent upon the programmer's style. Programmers experienced with LISP 1.5 [McCar 62] find it relatively easy to make effective use of local constants; in fact, such use is very similar to one use of LISP h-expressions. There is also a trade-off of run-time efficiency versus compiler speed; in particular, code generation based on a very sophisticated set of sufficient conditions for local constancy is probably incompatible with one-pass translation. Experience with the MUTANT 0.5 interpreter suggests that the most promising approach to the copy problem is a finer distinction among the various uses of the traditional assignment operator and a syntactic structure which distinguishes among such uses. The provision of ":=", "=", and "≃" for assignment, "initialization by value", and "initialization by reference", respectively, in CPL [Buxt 66] reflects exactly such a distinction. Landin's let

--

and <u>where</u> constructs [Land 66] are also used in CPL and are attractive syntactic devices for designating local constants.

E.3.d <u>Extended Operator Definitions</u>

In MUTANT and MUTANT 0.5, definitions of operators have been extended in the sense of Iverson [Iver 62] whenever possible. Such extension leads to at least three difficulties:

(1) For the results of a given computation to be well defined, the exact order of the evaluation of operands as well as the application of operators must be specified. This is due to the involution of assignment as well as the possibility of procedures with side effects. Difficulties are not limited to pathological cases; using the extended assignment operator of MUTANT, McKeeman [McKee 66] illustrates a useful application of

$$\{ a, b \} \leftarrow \{ b, a \} \qquad .$$

Specification of either complete evaluation of both operands in a specified order followed by operator application (as in MUTANT 0.5) or any of various levels of conceptual parallelism is likely to lead to gross inefficiencies in some implementations. McKeeman [McKee 67] has suggested a partial solution based upon the distinction between types <u>set</u> (unordered) and <u>list</u> (ordered).

(2) The meanings of operators intended to act upon structured values generally cannot be extended without the loss of such ● me'ani.ng. For example, the value of

$$\{ 1, 2, 4 \} = \{ 1, 3, 4 3$$

will be 0 or { 1, 0, 1 } depending upon the interpretation of the extended equality operator: In the first case, the extended meanings of equality operators will be very different from those of the other relational operators; in the second case, comparisons of structured values must be explicitly programmed (as in MUTANT 0.5) or require another equality operator. Extension of the subscripting and assignment operators present special difficulties:

(a) There are two common interpretations of subscript notation. In one, such notation is considered simply a naming device. In the other, the subscript brackets are considered to denote an operator which maps a value (or cell name) and a numerical value into a subvalue

(or subcell name). From this viewpoint, there is a natural gen-
eralization of the subscript operator: a value subscripted by an
ordered set (list) yields an ordered'set of values obtained by
applying each 'element of the set as a subscript, e.g.,

$$a[\ \{2,\{3,4\}\}\ ] \ \equiv \ a\_sub\ \{2,\{3,4\}\} \ \equiv \ \{\ a[2],\{a[3],a[4]\}\ \}\ .$$

Such an interpretation allows a very powerful and elegant method
of constructing new ordered sets from a collection of elements and
has been adopted by MUTANT and MUTANT 0.5. Note, however, that the
extension is not quite Iverson's; the subscripted value 'must be
structured but must be treated formally as unstructured. Further-
more, if cell names are allowed to be subscripted by sets (as in
MUTANT), the result must be a collection of (sub)cell names, and
one is led to an extended interpretation of assignment. If such
subscripting is not allowed (as in MUTANT 0.5), string manipulation
is quite awkward and an asymmetry is introduced in the language.

(b) There is a fairly obvious similar extension of the assignment
operator. It is again, however, not quite the Iverson extension
used elsewhere in MUTANT 0.5, for one would prefer

$$\{\ 1,\ \{\ 2,\ 3\ \}\ \}\ \rightarrow\ \{\ a,\ b\ \}\ \ \equiv \{\ 1 \rightarrow a,\ \{\ 2,\ 3\ \} \rightarrow b\ \}$$

instead of

$$\{\ 1,\ \{\ 2,\ 3\ \}\ \}\ \rightarrow\ \{\ a,\ b\ \}\ \ \equiv \{\ 1 \rightarrow a,\ \{\ 2 \rightarrow b,\ 3 \rightarrow b\ \}\ \}\ \ .$$

In addition, sequencing is critically important in assignment;
by one possible definition,

$$\{\ a,\ b\ \}\ \rightarrow\ \{\ b,\ a\ \}\ \ \equiv\ \{\ a \rightarrow b,\ b \rightarrow a\ \}\ \ \ ,$$

which is usually not the desired interpretation.

(3) Some data types are not either clearly structured or clearly unstructured.
The primary examples in MUTANT 6.5 are strings. It is desirable, for
example, to be able to access substrings by the subscript notation for
structured values; on the other hand, when used as operands to, e.g., the
put operator, it is convenient to consider them unstructured. A heir-
archy of structure can be introduced, but probably at the cost of some
loss of uniformity, and hence simplicity, in the interpretation mech-
anism.

E.3.e <u>Miscellaneous Problems</u>

A number of decisions made in the design and implementation of MUTANT 0.5

were later found to be mistakes, but these mistakes do not reflect fundamental problems in the design of **MUTANT-like** languages. Some of these **are** listed below:

(1) Choice of **Character Set**

In the design of **MUTANT** 0.5, it was decided to choose as concise a notation as possible and to reflect the usage of set theory as well as conventional algebra. When desired special symbols were not available in the IBM EBCDIC character set, they were usually represented by pairs of special characters rather than by word delimiters'or reserved words. **The** elegance of this approach is debatable; however, it is clear that readability suffers severely, especially in the hardware representation.

(2) Deletion **Operator**

The value of a **MUTANT 0.5** program at any point is generally a very 'large list structure, the structure of which reflects the history of interpretation up to that point in considerable detail. Such lists consume a large amount of storage and often **are** of no practical use. A sequencing operator, similar to the **comma** but deleting the last value canputed for an element of the list being constructed, would be very useful, **particularly** when an expression is evaluated **for** its effect rather **than** its value.

(3) Extended Case Expressions

McKeeman [McKee **66**] has demonstrated an elegant application of a list-valued case index in his **MUTANT** compiler. Such indices are prohibited in MUTANT 0.5 only because of **an** oversight in the design of the interpreter.

E.4 Methodology

Implementation of **MUTANT 0.5** has followed the example of **EULER** and MUTANT; it is based upon a straight-forward compiler producing Polish postfix operator strings and a stack-oriented interpreter of such strings. For experimental purposes, such a system seems entirely adequate. Weber [Weber **67**] has demonstrated the suitability of presently available hardware for implementing proven **compilation** and interpretation algorithms in microcode, and presumably results with specially designed hardware would be

even better than what he'reports,. In addition, it should be noted that
with sufficiently powerful operators the additional overhead of **inter-**
pretation is **relatively small;** for example, the MUTANT 0.5 interpreter
makes quite efficient use of the **System/360** general registers in vector
manipulation when such manipulation is **expressed** in **Iverson's** notation,
and this efficiency is possible without an optimizing compiler.

The grammar of MUTANT 0.5 was chosen to be a simple precedence grammar
because of **familiarity** with the techniques involved and availability of
suitable syntax processing programs. Other well understood formalisms,
summarized by Feldman and Gries **[Feld67],** could have been used equally
well, with some trade-offs among speed, space, **and** generality. In general,
it was found that, with the available machinery, modifications to the
MUTANT 0.5 **grammar** or compiler were fairly trivial to make. **On** the other
hand, many unfortunate features of the interpreter could not be changed
without substantial rewriting; further investigation of the related **prob-**
lems of formal semantics and machine description seems more appropriate
than continued work oriented entirely toward syntactic questions.

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Appendix I

Publication / Machine Character Set Mapping

Publication Character Set	Machine Character Set (EBCDIC)	Publication Character Set	Machine Character Set (EBCDIC)
a	(no equivalent)	⊗	*
...	...	+	DIV
z	(no equivalent)	mod	MOD
A	A	base	BASE
...	...	=	=
Z	Z	≠	⌐=
0	0	>	GT
...	...	≥	GTE
9	9	<	LT
"	"	≤	LTE
{	<	∧	AND
}	>	∨	OR
(	(	/	/
)	)	ℓ	∂
[	(_	.	4
]	_)	→	->
$	$		
|	⏐	'	'
,	,	⇒	⇒
get	GET	:	:
#	#̇	;	;
¹	¹	∈	ℰ
list	LIST	*	.
abs	ABS	eof	!
neg	NEG	(comment bracket)	?
put	PUT		
type	TYPE		
+	+		
-			

%SYNPROC

```
 1    <PROG>        ::=  !  <V-EXPR>  !
 2    <G-EXPR>      ::= <V-EXPR>
 3                       <Q-CLAUSE> <G-EXPR>
 4    <Q-CLAUSE>    ::=  <V-EXPR>  =>
 5    <V-EXPR>      ::= <V-EXPR*>
 6    <V-EXPR*>     ::= <SEGMENT>
 7                       <PROC HD>  <V-EXPR>  '
 8                       <V-EXPR*>  ->  <CELL>
 9    <PROC HO+>    ::=  '
10                       <PROC HO+>  (IDENT)
11    <PROC HO>     ..= <PROC HO+>   |
12    <SEGMENT>     ..= <S-EXPR>
13                       <S-EXPR>  _  <S-EXPR>
14                       <S-EXPR>  _  <S-EXPR>  _  <S-EXPR>
15    <S-EXPR>      ::= <S-EXPR*>
16    <S-EXPR*>     ::= <PRIM>
17                       <S-EXPR*>  <INFIX>  <PRIM>
18    <INFIX>       ::= +
19
20                       *
21                       DIV
22                       MOO
23                       BASE
24                       =
25                       ¬=
26                       GT
27                       GTE
28                       LT
29                       LTE
30                       AND
31                       OR
32                       |
33    <PRIM>        ::= <PRIM*>
34                       <PREFIX> <PRIM>
35                       <INFIX>/<PRIM>
36    <PREFIX>      ::= #
37                       ¬
38                       LIST
39                       ABS
40                       NEG
41                       PUT
42        '          TYPE
43    <PRIM*>       ::= <CELL>
44                       <REF>
45                       <S-PRIM>
46    <CELL>        ::= <CELL*>
47    <CELL*>       ::= (IDENT)
48                       <CELL*>(_  <V-EXPR>  _)
49                       <CELL*>   %
50    <REF>         ::= <REF*>
51    <REF*>        ::= a (IDENT)
52                       <REF*>  (_  <V-EXPR>  _)
53    <S-PRIM>      ::= <S-PRIM*>
54    <S-PRIM*>     ::= <CONSTANT>
55                       GET
56                       <LIST>
57                       <PRIM*>  <LIST>
58                       ( <V-EXPR>  )
```

```
59                          <CASE  HD>  <V-EXPR>  )
60                          <FCR H O > >
61                          <WHILE H O > >
62                          < F / W HD> >
63                          < S - P R I M * > (_ <V-EXPR> _)
64    <CONSTANT>    ::= (INTEGER)
65                      (STRING)
66                      <BEGIN> >
67    <LIST>        ::= <LIST  HO>  >
68    <LIST HD>     ::= <BEGIN> <G-EXPR>.
69                      < L I S T HD> ,  <G-EXPR>
70    <BEGIN>       ::⊠ <
71    <BEGIN>       .. . = <DECLARE> |
72    <DECLARE>     ::= < $
73                      <DECLARE>  (IDENT)
74                      <DECLARE> (IDENT)  (  <V-EXPR>  )
75    <CASE HO>     ::= <CASE IOX>  (  <V-EXPR>  ;
76                      < C A S E HD> <V-EXPR>;
77    <CASE I OX>   ::= (_  <V-EXPR>  _)
78    <FOR HD>      ::= <BEGIN> .< F O R SET> <G-EXPR>
79    <WHILE HD>    ::= <BEGIN>  <WHILE  CDN> <G-EXPR>
8C    <F/W HD>      ::= <BEGIN> <FOR  SET> <WHILE CON> <G-EXPR>
81    <FOR SET>     ::= .<FCR SET*>  :
a2    <FOR SE T*>   ::= (IDENT)  &  <V-EXPR>
83    <WHILE>       ::= .
84    <WHILE'>      ::= <WHILE> <Q-CLAUSE>
a5    <WHILE CON>   ::= <WHILE'>:
```

52

PRECEDENCE FUNCTIONS

1	`<PROG>`	1	1
2	`<G-EXPR>`	3	2
3	`<Q-CLAUSE>`	2	3
4	`<V-EXPR>`	5	4
5	`<V-EXPR*>`	4	5
6	`<PROC HO+>`	9	5
7	`<PROC HD>`	4	5
a	`<SEGMENT>`	7	5
9	`<S-EXPR>`	7	5
1C	`<S-EXPR*>`	a	6
11	`<INF IX>`	6	a
12	`<PR I M>`	10	6
13	`<PREFIX>`	6	7
14	`<PRIM*>`	10	7
15	`<CELL>`	12	7
16	`<CELL*>`	12	8
17	`<REF>`	12	7
18	`<REF*>`	12	7
19	`<S-PRIM>`	12	7
20	`<S-PRIM*>`	12	7
21	`<CONSTANT>`	13	7
22	`<LIST>`	13	10
23	`<LIST HO>`	2	11
24	`<BEGIN>`	2	11
25	`<DECLARE>`	9	11
26	`<CASE HD>`	4	7
27	`<CASE IDX>`	13	7
28	`<FOR HD>`	2	7
29	`<WHILE HO>`	2	7
30	`<F/W HD>`	2	7
31	`<FOR SET>`	2	2
32	`<FOR SET*>`	1	3
33	`<WHILE>`	3	3.
34	`<WHILE'>`	1	3
35	`<WHILE CDN>`	2	2
36	!	4	5
37	=>	14	5
38	'	10	5
39	->	7	6
40	(IDENT)	13	9
41		14	9
42	_	5	7
43	+	14	9
44	-	14	9
45	8	14	9
46	DIV	14	9
47	MOD	14	9
48	EASE	14	9
49	=	14	9
50	¬=	14	9
51	GT	14	9
52	GTE	14	9
53	LT	14	9
54	LTE	14	9
55	AND	14	9
56	CR	A4	9
57		6	6
58	#	14	7
59	¬	14	7
60	LI ST	14	7
61	ABS	14	7
42	NEG	14	7
63	PUT	14	7
64	TYPE	14	7
65	(_	4	1'2
66	_)	14	5
67	%	13	12
68	@	9	7
49	GET	13	7
70	(	4	13
71	)	13	5
72	>	13	2
73	(INTEGER)	13	7
74	(STRING)	13	7
75	,	2	2
76	<	14	11
77	$	10	14
78	;	14	5
79	:	14	1
a0	&	4	13
81	.	14	3

ELAPSED TIME IS 00:06:00

%MUTANT 1

```
                    ?
   0000          $     FACTORIAL  CALCULATION — SECTION 8.3.1    ?  .
   0000        <    FACTORIAL |
   000 1        • N  I  (_ 2-(N=0)_)(1;N*FACTORIAL<  N-1  > )' ->FACTORIAL
   0032         < N & 1_6 :
   003 D          PUT((N    BASE   10)| " FACTORIAL = " | (FACTORIAL< N > BASE 10; )
   0060        >
   0061      >
```

END   OF COMPILATION . '

ECAPSEC TIME IS 00:00:49

%MUTANT 2

```
1 FACTORIAL = 1
2 FACTORIAL = 2
3 FACTORIAL = 6
4 FACTORIAL = 24
5 FACTORIAL = 120
6 FACTORIAL = 720
```

ELAPSED TIME IS 00:00:36

%MUTANT 1

```
   0000             ?    EXTENDED   FACTORIAL CALCULATION – SECTION 8.3.2    ?
   000C          <$ FACTORIAL PROD |
   0002            < ' N | (_ 2-(N=0) _) ( 1 ; N*FACTORIAL(_1_)< N-1 > ) ' ,
   0033             'N| */( 1_N) ' ,
   0043             ' N | PROD< 1_N > '
   0053           > -> FACTORIAL,
   0059           ' L |  (_ 2-(#L=1) _)
   0067             ( L(_1_) ; PROD< L(_ 1_#L DIV 2 _) >*PROD< L(_ #L D | V 2+1_#L _) > )
   00A4            -> PROD,.
   00A9
   00A9           < I & 1_3 :
   0004             C PUT "",PUT("METHOD "|(I BASE 10) ),
   00CA               < N &1_8 3
   00D5                 PUT((N BASE 10)|" FACTORIAL ="|(FACTORIAL(_I_)< N >BASE 10) )
   00FC             >
   00FD           >
   0100         >
   0101       >
```

ENDOF COMPILATION

ELAPSED TIME IS 00:00:40

%MUTANT   2

METHOD 1
```
1 FACTORIAL = 1
2 FACTORIAL = 2
3 FACTORIAL = 6
4 FACTORIAL = 24
5 FACTORIAL = 120
6 FACTORIAL = 720
7 FACTORIAL = 5040
8 FACTORIAL = 40320
```

METHOD 2
```
1 FACTORIAL = 1
2 FACTORIAL = 2
3 FACTORIAL = 6
4 FACTORIAL = 24
5 FACTORIAL = 120
6 FACTORIAL = 720
7 FACTORIAL = 5040
a FACTORIAL = 40320
```

METHOD 3
```
1 FACTORIAL = 1
2 FACTORIAL = 2
3 FACTORIAL = 6
4 FACTORIAL = 24
5 FACTORIAL = 120
6 FACTORIAL = 720
7 FACTORIAL = 5040
8 FACTORIAL = 40320
```

ELAPSED TIME IS 00:00:43

$MUTANT 1

```
0000              ?    INNER PROOUCT - SECTION 8.3.3(A)    ?
0000         PUT ( ( +/( < 1,2,3 >*< 3,2,1 > ) ) BASE LO )
```

END Q F COMPILATION

ELAPSED TIME IS 00:00:35

$MUTANT 2

10

ELAPSEC TIME IS 00:00:37

%MUTANT 1

```
0000            ?     PERMUTATION GENERATOR - SECTION 8.3.3(8) ?
000C        < $ PERM |
000 1          ' X  | (_ 2-(#X=1) _)
0013            ( < X > ;
001A             |/< I & 1_#X :
0029                 < J  &PERM<X(_ 1_I-1 _)|X(_ I+1_#X _) > : X(_ I_I _)|T >
006 1               >
0064            ) ' -> PERM,
0076         < T E S T & < " A ", "AB", "ABC","ABCD" > : P U T PERM< T E S T>>
009A        >
```

E N D CF COMPILATION

ELAPSEC TIME IS 00:00:36 .

%MUTANT 2

A
A8
BA
ABC
ACB
BAC
BCA
CAB
CBA
ABCD
ABDC
ACBD
ACDB
ACBC
ADCB
BACD
BADC
BCAD
BCDA
BDAC
BDCA
CABD
CAD8
CBAC
CBDA
CDAB
CCBA
DABC
CACB
DBAC
CBCA
DCAB
DCBA

ELAPSED TIME IS 00:00:43

%MUTANT 1

```
C000            ?    PRIME SIEVE SAMPLE PROGRAM - SECTION 8.3.4    ?
0000         C  $ PRIMESIEVE
0000            { '  N    I< $ L T | 2_N -> L,
0014                      < .  #L -= □ => :
001E                       <  L(_1_)  ->T,<I&L:I  MQD  T-=0 =>   I   >  ->  L  >(_1_)
004 B                       >
004C                  >(_2_) '
0053         ) |
0054         < N & < 25, 250 > :
0C64           <   PUT  ("PRIMES   IN   2   TO  "|(N   BASE  10)|":"),
0082              P U T(PRIMESIEVE< N >BASE 10)
008E           >
008F      >
0090      >
```

E N D OF COMPILATION

ELAPSED TIME IS 00:00:40

%MUTANT 2

PRIMES IN 2 T O 25:

2	
3	
5	
7	
11	97
13	101
17 .	103
19	**107**
23	**109**
PRIMES IN '2 TO 25C: ·	**113**
2	127
3	131
5	**137**
7	139
11	149
13	151
17	**157**
19	163
23	167
	173 ·
29 31	**179**
37	181
41	191
43	193
47	197
53	199
59	**211**
61	223
67	227
71	229
73	233
79	239
83	**241**
89	

ELAPSED TIME IS 00:01:09

%MUTANT 1

```
0000          ?    PERMUTATION GENERATOR ?
000C          < $ PERM |
000 1            • X | (_ 2-(#X=1) _)
0013               ( < X > ;
001A                 |/< I & 1_#X :
0029                      < T & PERM< X(_  1-I-1 _) | X(_ I+1_#X _) >:
0052                       < X(_ I _) > | T
0C5B                      >
005F                  > )• -> PERM,
0074          C  TEST &< 1_1, 1_2, 1_3, 1_4 > :
009C             < P & PERM<  TEST  > :PUT(|/(P  BASE  10) ) >
00AB          >  >
```

END OF COMPILATION

ELAPSED J IME IS C0:00:39

%MUTANT 2

```
1
12
21
123
132
213
231
312
321
1234
1243          .
1324
1342
1423
1432
2134
2 143
2314
2341
2413
2431          .
3124
3142
3214
3241
3412
3421   .
4123   .
4132
4213
4231
4312
4321
```

ELAPSED T I M E I S 0C:00:44

XMUTANT 1

```
0000                ?GRAPH MANIPULATION ROUTINES?
0000            C $REACHVEC
0000             (' c I |
0004               <$  PR  R  BB  N (#C)|
000B                 ( 1_N)¬=I -> BB, C(_I_) ->R,   LIST N ->PR,
0030                 < . +/(PR=(R->PR))¬=N => :
0047                    <J &  1_N :BB(_J_)A N D PR(_J_)=>
0062                      ' < 0 -> BB(_J_), R  OR  C(_J_)-> R > >
007F                 >, R >(_5_) ')
0080             DISPLAYMATRIX
0080            (' C TITLE|<PUT " ",P  U  T TITLE,
009A              < I & 1_#C :P U T(|/(C(_I_)B A S E 2))>>')
00BC            REACHMATR  I  X MAXSC SUBGRAPH T
00BE             c ( < <1,1,0,0,0,0>, <0,1,0,1,0,0>, <0,1,1,0,0,0>,
00EA                  <0,0,0,1,1,0>, <0,1,0,0,1,0>, <1,0,0,0,0,1> > ) I
0115            ' c I < I & 1_#C : REACHVEC<'C, I >3 ' -> REACHMATRIX,
013E            'R|<   1  &1_#R:< J &  1_#R :R(_I_)(_J_) AND R(_J_)(_I_) > > '
0179               -> MAXSC SUBGRAPH,
017E            DISPLAYMATRIX<C,"C M A T R I X">,
0191            OISPLAYMATRIXC REACHMATRIX< C >,"R MATRIX">,
01AA            DISPLAYMATRIX<  MAXSC SUBGRAPH<REACHMATRIX< C >>,"MSC M A T R I X">
```

END CF CUMPILATION

ELAPSED T I M E I S 0C:00:42

XMUTANT 2

C MATRIX
```
1 10000
010100  .
011000
000110
010010
10000 1
```

R MATRIX
```
1101.10
010110
011110
010110 .
010110
110111
```

MSC MATRIX
```
10000C
010110
00100C
010110
010110
C0000 1
```

ELAPSEC **TIME** IS   0C:00:48

%MUTANT 1

```
0000          < $ SQRT
OOOC            (' N |< $   X   ERR  |
0006              ( N DIV 2  -> X )*N*2-> ERR,
001F              C . ERR  GT(ABS( X*X -- N )->   ERR  ) =>:  ( X + (N DIV X)) DIV 2 ->
004B              X   >(_3_) ' )
0053           PRIMESIEVE
0053            (' N | < $ L  T | 2_N -> L,
0067           <. #L¬=0 => :
0071              < L(_1_) -> T, < I & L : I MOD T ¬= 0 => I > -> L >(_1_) >
009F           >(_2_)' ) |
00A7           PUT" PRIMES AND INTEGERIZED SQUARE ROOTS",
0002           < I & PRIMESIEVE<    250   >:
00E0              PUT (( I·BASE 10 )|"    "|( SQRT< I > BASE 10 )) >  >
```

END GF COMPILATION

ELAPSE0 **TIME** IS **00:00:39**

%MUTANT 2

PRIMES ANG INTEGERIZED SQUARE ROOTS

2	1			
3	1			
5	**2**			
7	**2**			
11	**3**		149	12
13	**3**		**151**	12
17·	**4**		**157**	12
19	**4**		163	12
23	4		**167**	12
29	**5**		**173**	13
31	**5**		**179**	13
37	**6**		**181**	13
41	**6**		**191**	**13**
43	**6**		**193**	13
47	**6**		197	14
53	7		199,	14
59	7		211	**14**
6**1**	7		**223**	**14**
67	8		**227**	**15**
71	8		**229**	15
73	**8**		233-	15
79	8		239	**15**
83	9		241	**15**
89	9			
97	9		ELAPSED TIME IS **0C:01:17**	
101	10			
103	**10**			
107	10			
1C9	10			
113	**1C**			
127	11			
131	11			
137	11			
139	11			