BIG DATA ANALYTICS ARCHITECTURES, ALGORITHMS AND APPLICATIONS PART #1: SCALABLE BIG DATA ALGORITHMS

EDWARD CHANG 張智威

HTC (PRIOR: GOOGLE & U. CALIFORNIA)

SIMON WU

HTC (PRIOR: TWITTER & MICROSOFT)

Three Lectures

- Lecture #1: Scalable Big Data Algorithms
 - Scalability issues
 - Key algorithms with application examples
- Lecture #2: Intro to Deep Learning
 - Autoencoder & Sparse Coding
 - Graph models: CNN, MRF, & RBM
- Lecture #3: Analytics Platform [by Simon Wu]
 - Intro to LAMA platform
 - Code lab

Lecture #1 Outline

- Motivations Why Big Data is not only desirable but also necessary?
- Applications
 - HTC XPRICE Tricorder
 - Context-aware Computing
- Key Parallel Algorithms
 - Frequent Itemset Mining [ACM RS 08]
 - Latent Dirichlet Allocation [TIST 10]
 - Support Vector Machines [MM 01] [MS 03][NIPS 07]
 - Spectral Clustering [PAMI 10]
 - Deep Learning [NIPS 12][OSDI 14]
- Perspectives and Opportunities

Key References

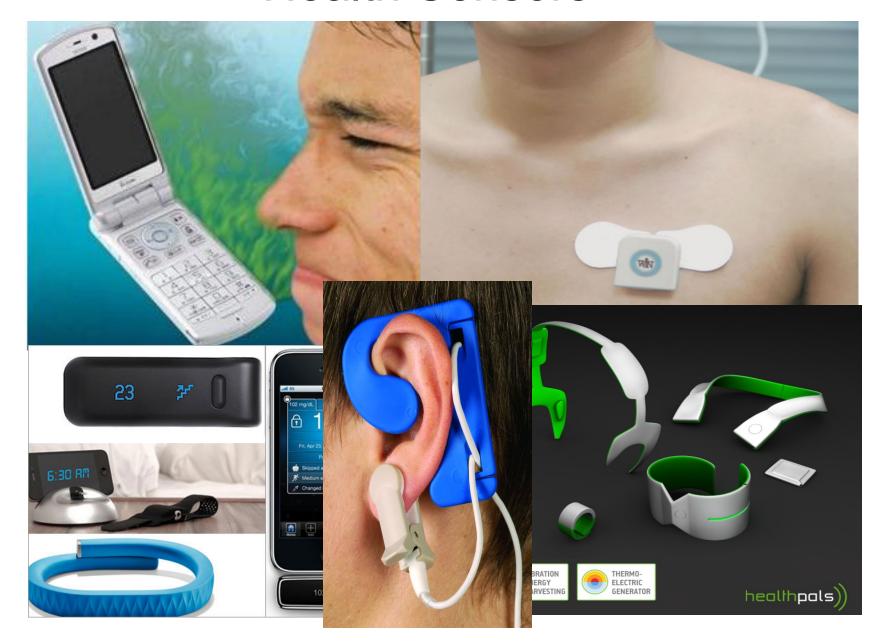
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- [NIPS 07] Parallel Support Vector Machines, E. Y. Chang, et al., NIPS 2007.
- [PAMI 10] Parallel Spectral Clustering, W.-Y. Chen, Y. Song, H. Bai, Chih-Jen Lin, and E. Y. Chang, IEEE Transactions on Pattern Analysis and Machine Intelligence (PAMI), 2010.
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- [VLDB 14] Big Data, Small Footprint: The Design of a Low-Power Classifier for Detecting
 Transportation Modes (with <u>Open Source dataset</u>), M. Yu, T. Yu, C.-J. Lin, and E. Y. Chang, VLDB,
 August 2014.

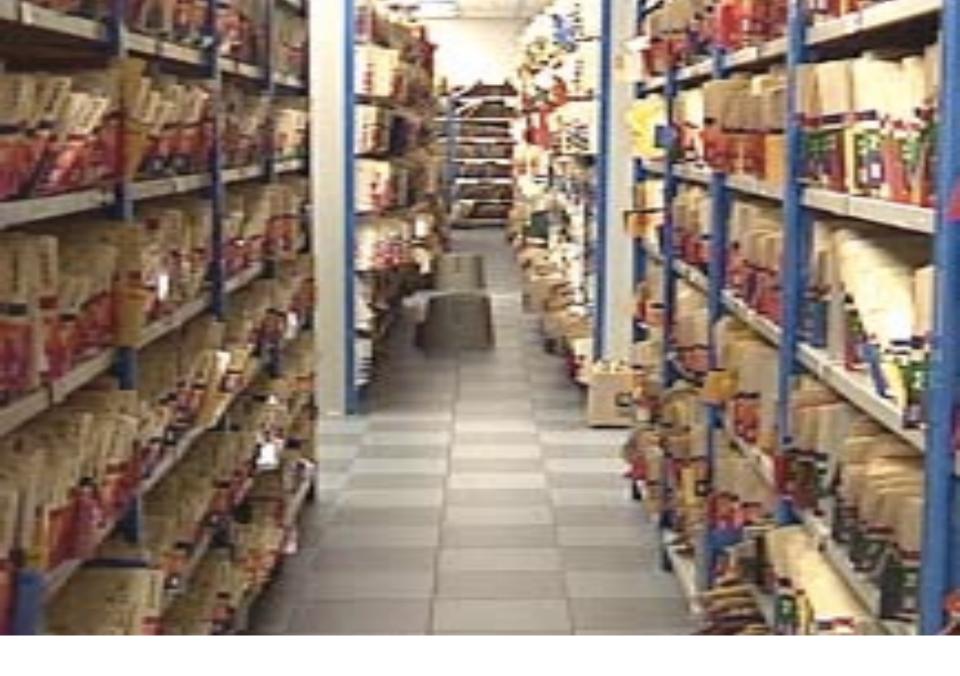
Open Source Links Downloaded > 12,000 times

- <u>PSVM</u>,
- <u>PLDA+</u>,
- Parallel Spectral Clustering, and
- Parallel Frequent Pattern Mining



Health Sensors





Machine Learning

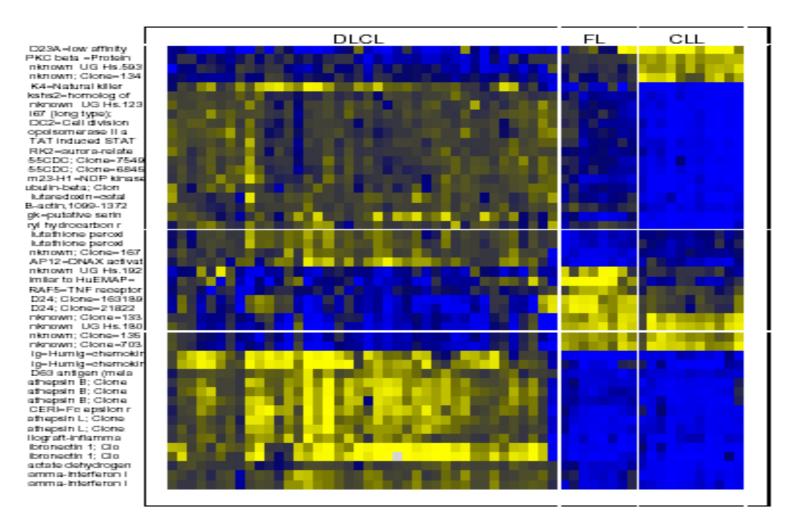
- X: Data
 - U: Unlabeled data
 - L: Labeled data
- Ф: Learning algorithm
 - Implied hypothesis
- $f = \Phi (L + U)$
 - Minimize some error function
 - Regularize parameters to prevent over-fitting
- $\hat{y} = f(u \in U)$

Scalability Issue

- $f = \Phi(L)$ supervised learning
 - Training data can be voluminous
 - A few millions is already too many, though not enough!
 - Training data is scarce

Gene Classification

D = 4026 genes, L = 3, N = 59 cases



Scalability Issues

- $f = \Phi(L)$
 - Training data is too many
 - Training data is scarce
- $f = \Phi (L^* + U)$ semi-supervised learning
 - L* Collect most useful training data
 - U Use unlabeled data
 - L* + U is voluminous!
- $f = \Phi(U)$ unsupervised learning
 - NN, CNN, RBM, Deep Learning

Challenges

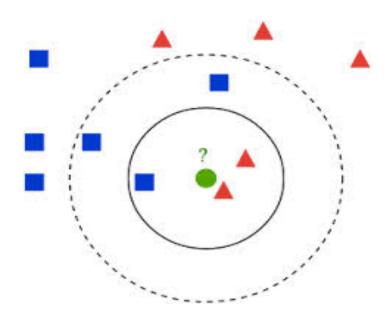
- Volume, both too large and too small
 - Amount of data
 - Amount of labeled data
 - dimensionality of data
- Variety
- Velocity
 - Addressed in Lecture #3 with online learning

Why Big Data

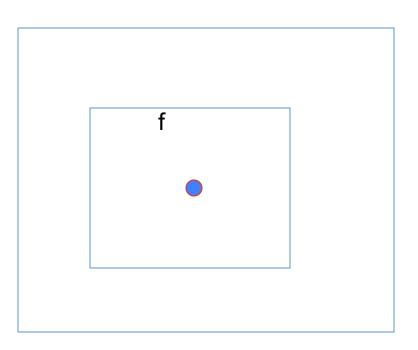
- Simply too many data instances? Yes
- But also growing complexity, or dimensionality of data

Why Big Data

- Every learning model is a variant of the nearest neighbor model (distance computation, likelihood)
- An unseen instance needs to get the labels of its neighbors to predict its label



Why Big Data



- f = .5, d = 2, NN = 25%
- When d is large
 The volume of NN → 0
 f < 1 d > 100, f^d → 0,
- Curse of dimensionality

More Data vs. Better Algorithms

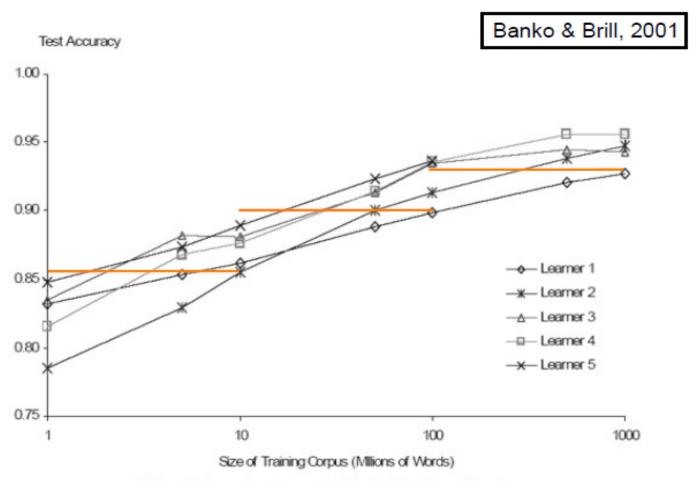


Figure 2. Learning Curves for Confusable Disambiguation

Applications & Algorithms

- Applications
 - HTC XPRICE Tricorder
 - Context-aware Computing
- Key Algorithms
 - Frequent Itemset Mining [ACM RS 08]
 - Latent Dirichlet Allocation [WWW 09, TIST 10]
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XPRIZE Tricorder

Fostering disruptive innovation to bring affordable health care to underprivileged



Portable device weight < 5 pounds

Exam 15+ diseases & monitor 5 vital signs

HTC was selected into ten finalists (from

255) on 8/27/2014

Final round: May, 2015



Diagnosis: Collaborative Filtering

Activities, Food, Symptoms, Diseases, Drugs

Based on *membership* so far, and *memberships* of others

↓

Predict further *membership*

Individuals

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			1	1	1						
		1		1	1		1		1		1
						1		1			1
		1		1		1	1				
I			1								
							1	1			
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	1	1									
I		1								1	
	1										1
		1	1	1	1	1					

Collaborative Filtering

Activities, Food, Symptoms, Diseases, Drugs

Based on *partially* observed matrix

Predict *unobserved* entries

? Individuals

FIM-based Prediction



To grow the base, we need association rules

- An association rule: $a, b, c \longrightarrow d$
- A Bayesian interpretation: $P(d \mid a, b, c) = \frac{N(a, b, c, d)}{N(a, b, c)}$
- The key is to count the occurrences (support) of itemsets N(...)

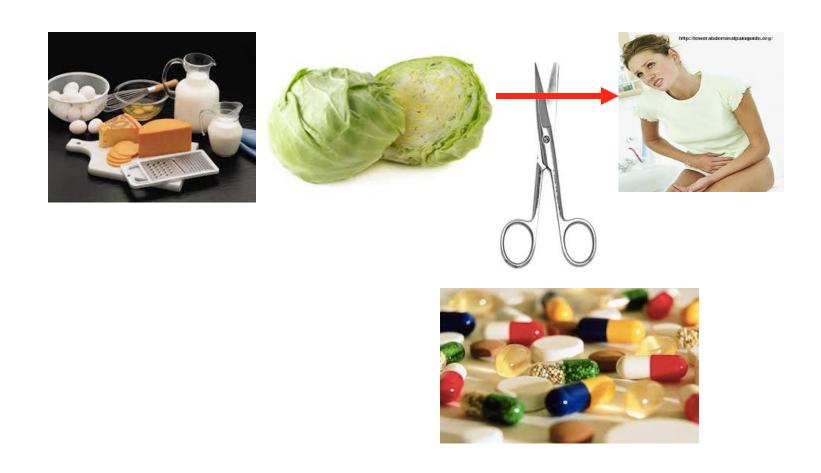
FIM-based Prediction



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FIM-based Prediction



FIM Preliminaries

- Observation 1: If an item A is not frequent, any pattern contains A won't be frequent [R. Agrawal]
 - use a threshold to eliminate infrequent items

```
\{A\} \rightarrow \{A,B\}
```

- Observation 2: Patterns containing A are subsets of (or found from) transactions containing A [J. Han]
 - → divide-and-conquer: select transactions containing A to form a conditional database (CDB), and find patterns containing A from that conditional database

```
\{A, B\}, \{A, C\}, \{A\} \rightarrow \mathsf{CDB} A
\{A, B\}, \{B, C\} \rightarrow \mathsf{CDB} B
```

Observation 3: Duplicates !

Preprocessing

	f : 4
	c: 4
0 1 1	a: 3
facdgimp	b: 3
1 01	m: 3
a b c f l m o	p : 3
bfhjo	o: 2
	d: 1
bcksp	e: 1
	g: 1
a f c e l p m n	h: 1
	i: 1
	k: 1
	1:1
	n: 1

fcamp
f c a b m
fb
c b p
f c a m p

- According to
 Observation 1, we
 count the support of
 each item by
 scanning the
 database, and
 eliminate those
 infrequent items
 from the
 transactions.
- According to
 Observation 3, we
 sort items in each
 transaction by the
 order of descending
 support value.

Parallel Projection

- According to Observation 2, we construct CDB of item A; then from this CDB, we find those patterns containing A
- How to construct the CDB of A?
 - If a transaction contains A, this transaction should appear in the CDB of A
 - Given a transaction {B, A, C}, it should appear in the CDB of A, the CDB of B, and the CDB of C
- Dedup solution: using the order of items:
 - sort $\{B,A,C\}$ by the order of items $\rightarrow \langle A,B,C \rangle$
 - Put <> into the CDB of A
 - Put <A> into the CDB of B
 - Put <A,B> into the CDB of C

Example of Projection

```
fcamp p: {fcam/fcam/cb}

fcabm m: {fca/fca/fcab}

fb b: {fca/fcb}

cbp a: {fc/fc/fc}

fcamp c: {f/f/f}
```

Example of Projection of a database into CDBs. Left: sorted transactions in order of *f*, *c*, *a*, *b*, *m*, *p* Right: conditional databases of frequent items

Example of Projection

```
fcamp p: {fcam/fcam/cb}
fcabm m: {fca/fca/fcab}
fb b: {fca/f/c}
cbp a: {fc/fc/fc}
```

Example of Projection of a database into CDBs.

Left: sorted transactions;

Right: conditional databases of frequent items

Example of Projection

```
fcamp
    p: {fcam/fcam/cb}

fcabm
    m: {fca/fcab}

fb    b: {fca/f/c}

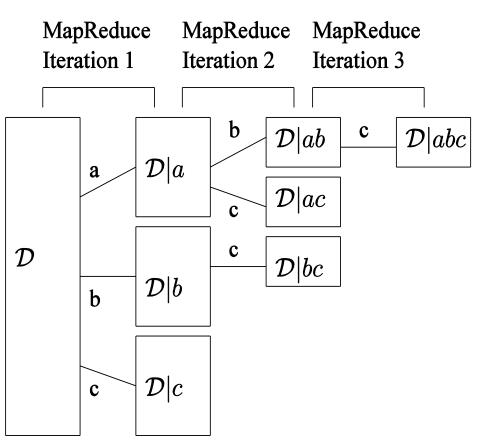
cbp
    a: {fc/fc/fc}
```

Example of Projection of a database into CDBs.

Left: sorted transactions;

Right: conditional databases of frequent items

Recursive Projections [H. Li, et al. ACM RS 08]



- Recursive projection form a search tree
- Each node is a CDB
- Using the order of items to prevent duplicated CDBs.
- Each level of breath-first search of the tree can be done by a MapReduce iteration.
- Once a CDB is small enough to fit in memory, we can invoke FP-growth to mine this CDB, and no more growth of the subtree.

Projection using MapReduce

Map inputs (transactions) key="": value	Sorted transactions (with infrequent items eliminated)	Map outputs (conditional transactions) key: value
facdgimp	f c a m p	p: fcam m: fca a: fc c: f
a b c f l m o	fcabm	m: fcab b: fca a: fc c: f
bfhjo	fb	b: f
bcksp	сbр	p: c b
a f c e l p m n	f c a m p	b: c p: fcam m: fca a: fc c: f

Reduce inputs (conditional databases) key: value Reduce outputs (patterns and supports) key: value

p:{fcam/fcam/cb} p:3, pc:3

	{fca/fca/fcab}	m f:3
		m c:3
		m a:3
m:		m f c:3
		m f a:3
		m c a:3
		mfca:3
b:	{ fca/f/c}	b:3
a:	{fc/fc/fc}	a:3
		a f:3
		a c : 3
		afc:3
		c:3
^.	$\{f/f/f\}$	cf:3

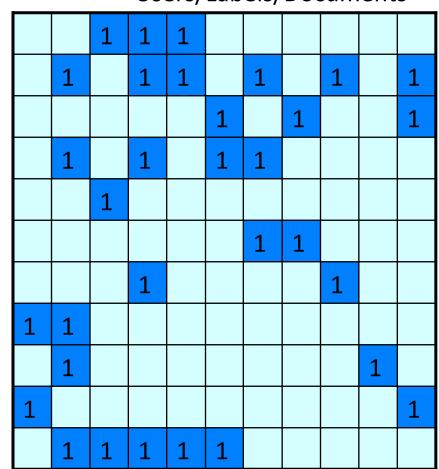
Collaborative Filtering

[Confucius or Google QA, VLDB 2010]

Users/Labels/Documents

Based on *membership* so far, and *memberships* of others

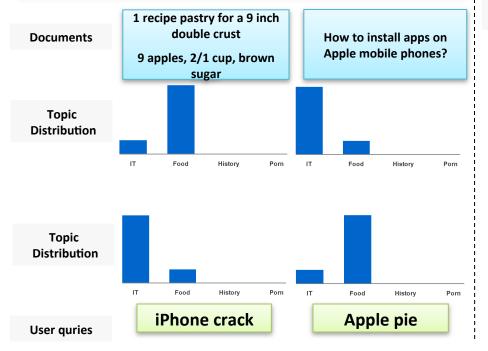
Predict further *membership*



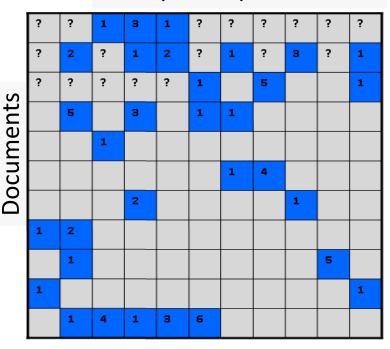
Documents

Latent Semantic Analysis

- Search
 - Construct a latent layer for better for semantic matching
- Example:
 - iPhone crack
 - Apple pie



Users/Labels/Documents



- Collaborative Filtering Apps
 - Recommend Users → Docs
 - Recommend Labels → Docs
 - Recommend Photos → Docs
- Predict the ? In the gray cells

1/26/2015

Ed Chang @ BigDat 2015

The Problem

- Two problems that arise using the vector space model:
 - Synonymy: many ways to refer to the same object, e.g. car and automobile
 - leads to poor recall
 - Polysemy: most words have more than one distinct meaning, e.g. model, python, chip
 - leads to poor precision

The Setting

- Corpus, a set of N documents
 - D={d_1, ...,d_N}
- Vocabulary, a set of M words
 - $W=\{w_1, ..., w_M\}$
- A matrix of size N * M to represent the occurrence of words in documents
 - Called the term-document matrix

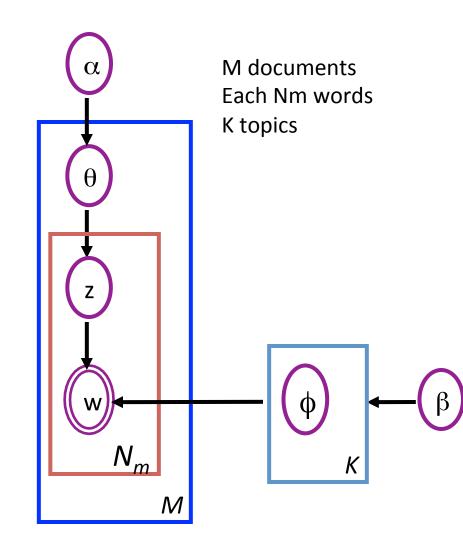
Documents, Topics, Words

- A document consists of a number of topics
 - A document is a probabilistic mixture of topics
- Each topic generates a number of words
 - A topic is a distribution over words
 - The probability of the ith word in a document

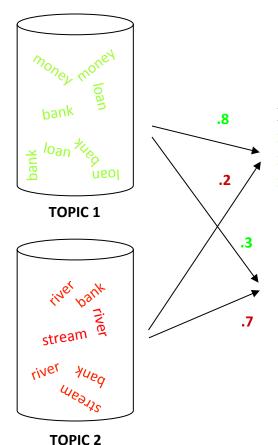
$$P(w_i) = \sum_{j=1}^{T} P(w_i | z_i = j) P(z_i = j)$$

Latent Dirichlet Allocation [M. Jordan 04]

- α : uniform Dirichlet ϕ prior for per document d topic distribution (corpus level parameter)
- β : uniform Dirichlet ϕ prior for per topic z word distribution (corpus level parameter)
- θ_d is the topic distribution of doc d (document level)
- z_{dj} the topic if the jth word in d, w_{dj} the specific word (word level)



Example



DOCUMENT 1: money¹ bank¹ bank¹ loan¹ river² stream² bank¹ money¹ river² bank¹ money¹ bank¹ loan¹ money¹ stream² bank¹ money¹ bank¹ bank¹ loan¹ river² stream² bank¹ money¹ river² bank¹ money¹ bank¹ loan¹ bank¹ money¹ stream²

DOCUMENT 2: river² stream² bank² stream² bank² money¹ loan¹ river² stream² loan¹ bank² river² bank² bank¹ stream² river² loan¹ bank² stream² bank² money¹ loan¹ river² stream² bank² stream² bank² river² bank² money¹ bank¹ stream² river² bank² stream² bank² money¹

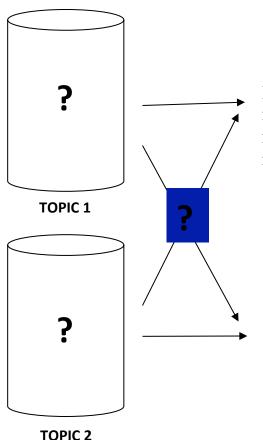
Mixture topics

Mixture weights

Bayesian approach: use priors Mixture weights \sim Dirichlet(α)

Mixture topics \sim Dirichlet(β)

Inverting ("fitting") the model



DOCUMENT 1: money? bank? bank? loan? river? stream? bank? money? river? bank? money? bank? loan? money? stream? bank? money? bank? bank? loan? river? stream? bank? money? river? bank? money? bank? loan? bank? money? stream?

DOCUMENT 2: river? stream? bank? stream? bank? money? loan? river? stream? loan? bank? river? bank? bank? stream? river? loan? bank? stream? bank? money? loan? river? stream? bank? stream? bank? money? river? stream? loan? bank? river? bank? money? bank? stream? river? bank? stream? bank? money?

Mixture components

Mixture weights

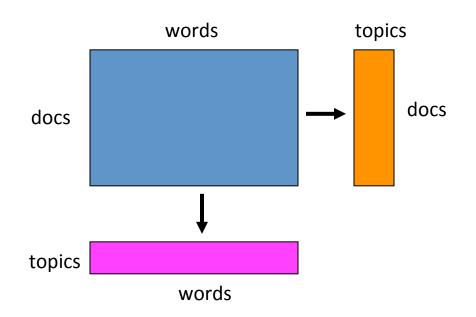
LDA Gibbs Sampling: Inputs And Outputs

Inputs:

- Training data: documents as bags of words
- 2. <u>Parameter</u>: the number of topics

Outputs:

- 1. A co-occurrence matrix of topics and documents
- 2. A co-occurrence matrix of topics and words



Example Application corpus data

- TASA corpus: text from first grade to college
 - representative sample of text

- 26,000+ word types (stop words removed)
- 37,000+ documents
- 6,000,000+ word tokens

Example Topics

- 37K docs, 26K words
- 1700 topics, e.g.:

PRINTING PAPER PRINT PRINTED **TYPE PROCESS** INK **PRESS IMAGE PRINTER** PRINTS **PRINTERS COPY** COPIES **FORM OFFSET GRAPHIC SURFACE PRODUCED CHARACTERS**

PLAY PLAYS STAGE AUDIENCE THEATER ACTORS DRAMA SHAKESPEARE ACTOR **THEATRE PLAYWRIGHT** PERFORMANCE **DRAMATIC** COSTUMES **COMEDY** TRAGEDY CHARACTERS **SCENES OPERA** PERFORMED

TEAM GAME BASKETBALL **PLAYERS** PLAYER **PLAY PLAYING** SOCCER PLAYED BALL **TEAMS BASKET FOOTBALL SCORE COURT GAMES** TRY **COACH** GYM

SHOT

JUDGE TRIAL COURT **CASE** JURY **ACCUSED** GUILTY **DEFENDANT** JUSTICE **EVIDENCE** WITNESSES **CRIME** LAWYER WITNESS **ATTORNEY HEARING INNOCENT** DEFENSE CHARGE **CRIMINAL**

HYPOTHESIS EXPERIMENT SCIENTIFIC **OBSERVATIONS** SCIENTISTS EXPERIMENTS **SCIENTIST EXPERIMENTAL** TEST **METHOD** HYPOTHESES **TESTED** EVIDENCE BASED OBSERVATION **SCIENCE FACTS** DATA RESULTS EXPLANATION

STUDY TEST STUDYING **HOMEWORK NEED** CLASS MATH TRY **TEACHER** WRITE **PLAN** ARITHMETIC **ASSIGNMENT** PLACE **STUDIED CAREFULLY** DECIDE **IMPORTANT** NOTEBOOK **REVIEW**

Polysemy

PRINTING PAPER PRINT PRINTED **TYPE PROCESS** INK **PRESS IMAGE PRINTER PRINTS PRINTERS** COPY **COPIES FORM** OFFSET **GRAPHIC SURFACE** PRODUCED **CHARACTERS**

PLAY

PLAYS
STAGE
AUDIENCE
THEATER
ACTORS
DRAMA
SHAKESPEARE
ACTOR
THEATRE
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OPERA

PERFORMED

TEAM **GAME** BASKETBALL **PLAYERS PLAYER PLAY** PLAYING **SOCCER PLAYED** BALL **TEAMS BASKET FOOTBALL SCORE COURT GAMES** TRY **COACH** GYM SHOT

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Three documents with the word "play"

(numbers & colors → topic assignments)

A Play⁰⁸² is written⁰⁸² to be performed⁰⁸² on a stage⁰⁸² before a live⁰⁹³ audience⁰⁸² or before motion²⁷⁰ picture⁰⁰⁴ or television⁰⁰⁴ cameras⁰⁰⁴ (for later⁰⁵⁴ viewing⁰⁰⁴ by large²⁰² audiences⁰⁸²). A Play⁰⁸² is written⁰⁸² because playwrights⁰⁸² have something

He was listening⁰⁷⁷ to music⁰⁷⁷ coming⁰⁰⁹ from a passing⁰⁴³ riverboat. The music⁰⁷⁷ had already captured⁰⁰⁶ his heart¹⁵⁷ as well as his ear¹¹⁹. It was jazz⁰⁷⁷. Bix beiderbecke had already had music⁰⁷⁷ lessons⁰⁷⁷. He wanted²⁶⁸ to play⁰⁷⁷ the cornet. And he wanted²⁶⁸ to play⁰⁷⁷ jazz⁰⁷⁷

Jim²⁹⁶ plays¹⁶⁶ the game¹⁶⁶. Jim²⁹⁶ likes⁰⁸¹ the game¹⁶⁶ for one. The game¹⁶⁶ book²⁵⁴ helps⁰⁸¹ jim²⁹⁶. Don¹⁸⁰ comes⁰⁴⁰ into the house⁰³⁸. Don¹⁸⁰ and jim²⁹⁶ read²⁵⁴ the game¹⁶⁶ book²⁵⁴. The boys⁰²⁰ see a game¹⁶⁶ for two boys play the game BigDat 2015

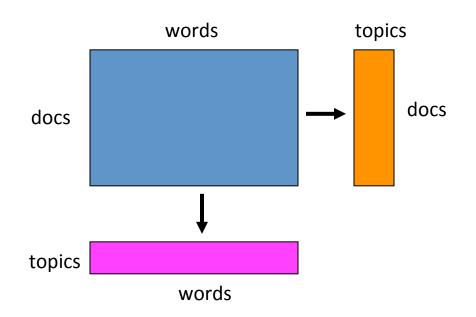
LDA Gibbs Sampling: Inputs And Outputs

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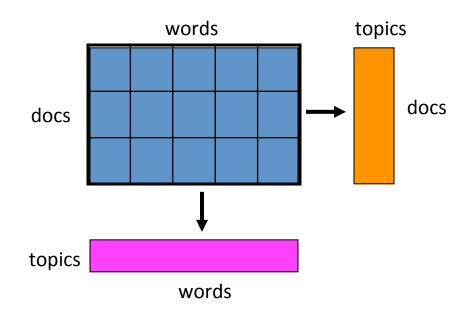
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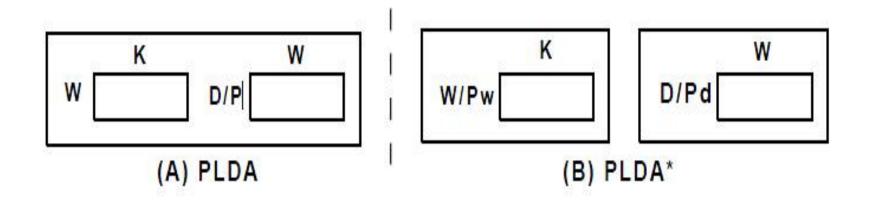
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PLDA+ --- enhanced parallel LDA

[ACM TIST 2010]

- PLDA is restricted by memory: Topic-word matrix has to fit into memory
- WK matrix must be globally synchronized
- Restricted by Amdahl's Law: communication costs too high, e.g., 1/10 cost spent in IOs caps speedup to



Work Order Example

- Words a, b, c, a, c, d, e, f, a, c, b
- Words <u>a</u>, <u>a</u>, <u>a</u>, <u>b</u>, <u>b</u>, <u>c</u>, <u>c</u>, <u>c</u>, <u>d</u>, e, f
- Word sorting per node to improve locality
- Word bundles to balance workload and increase CPU computation unit to mask IO time

PLDA+ --- enhanced parallel LDA

- Take advantage of bag of words modeling: each Pw machine processes vocabulary in a word order
- Pipelining: fetching the updated topic distribution matrix while doing Gibbs sampling
- Ensure tf + tu < ts (4(A) is good, 4(B) suboptimal)

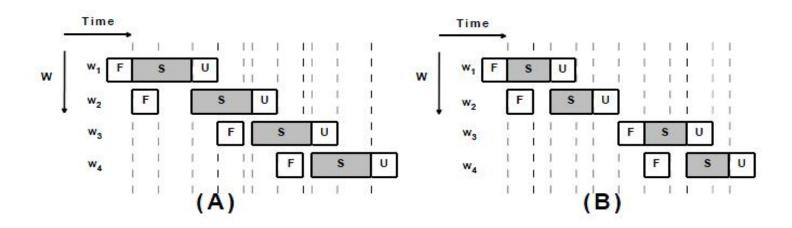


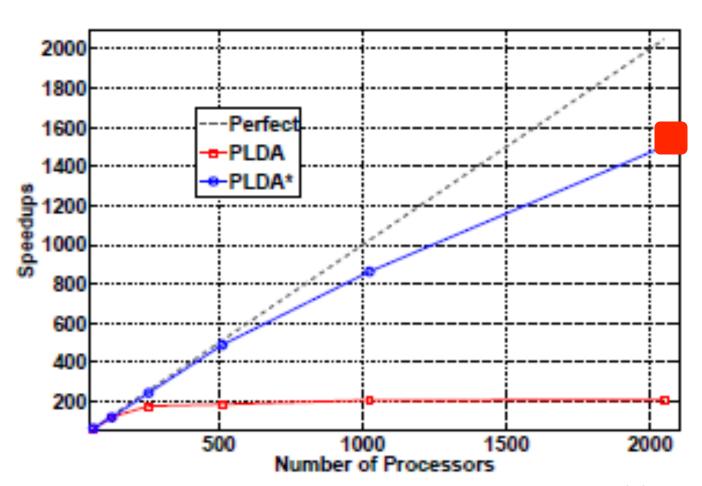
Fig. 4: Pipeline-based Gibbs Sampling in PLDA*. (A): $t_s \ge t_f + t_u$. (B): $t_s < t_f + t_u$.

MapReduce VS. MPI?

	MapReduce	MPI
GFS/IO and task rescheduling overhead between iterations	Yes	No +1
Flexibility of computation model	AllReduce only +0.5	Flexible +1
Efficient AllReduce	Yes +1	Yes +1
Recover from faults between iterations	Yes +1	Apps +0.5
Recover from faults within each iteration	Yes +1	Apps +0.5
Final Score for scalable machine learning	3.5	5

Speedup

1,500x using 2,000 machines



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 - Deep Learning [NIPS 12, OSDI 14]
- Perspectives and Opportunities

Melanoma vs. Nevus



Key Technical Challenges

- Acquire labeled data (most data are unlabeled)
- Formulate distance function
- Train a classifier
- Classify unlabeled data
 - Fast
 - Low power consumption

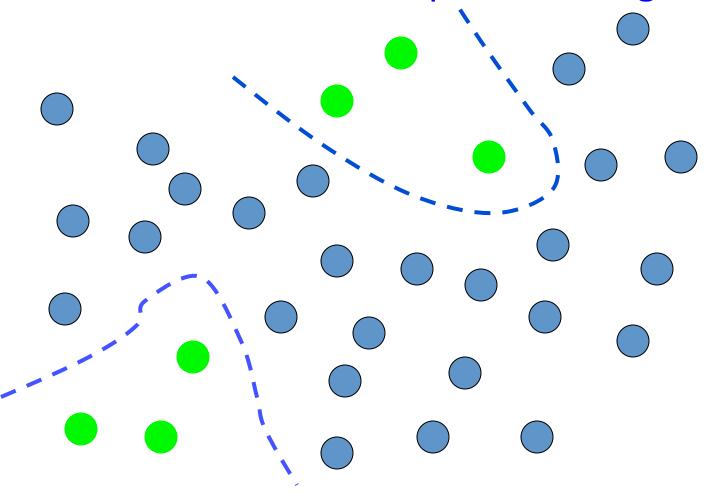
Models

- Generative Models
 - Model distribution
 - One each class
 - Look for maximum likelihood
 - Need a lot of training data

- Discriminative Models
 - Model class boundaries
 - Ignore distribution
 - Support VectorMachines (SVMs)

IR -> A Classification Problem

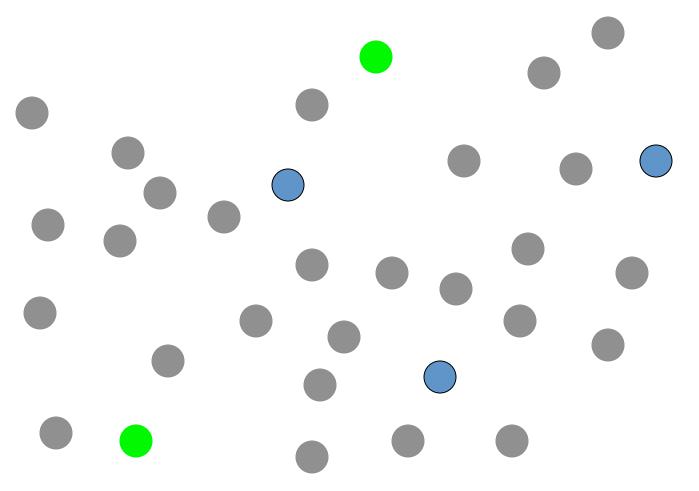
Use SVMActive to Acquire Training Data



Ed Chang @ BigDat 2015

IR \rightarrow A Classification Problem

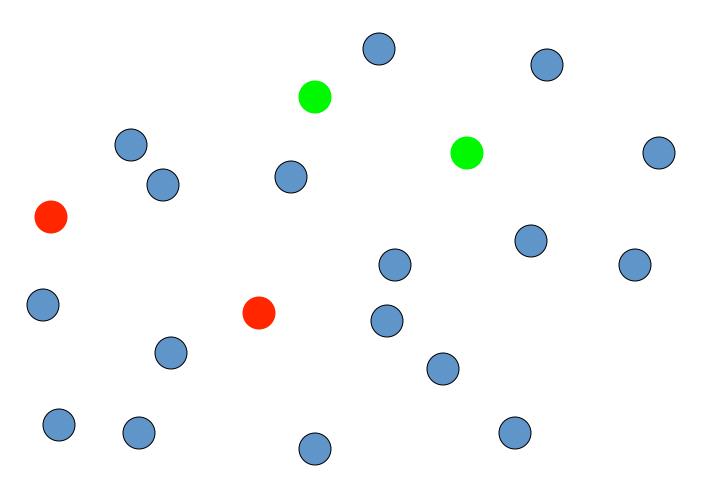
Most Data are Unlabeled



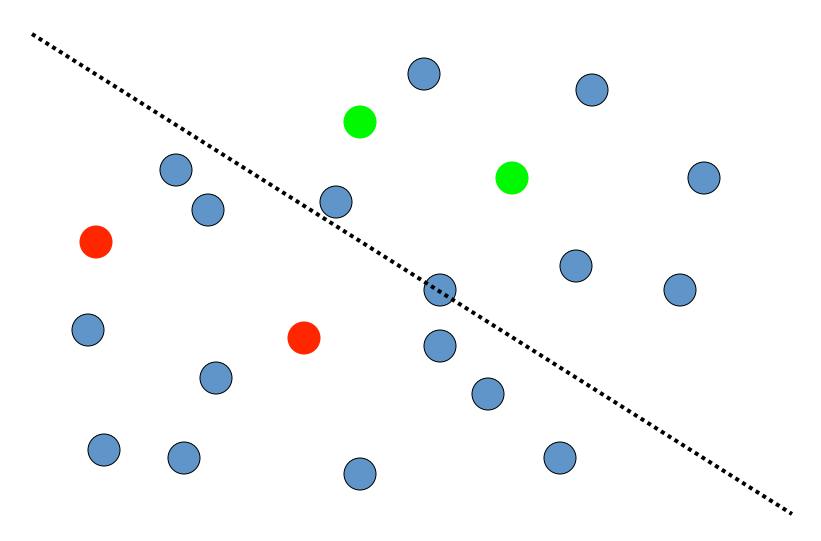
Ed Chang @ BigDat 2015



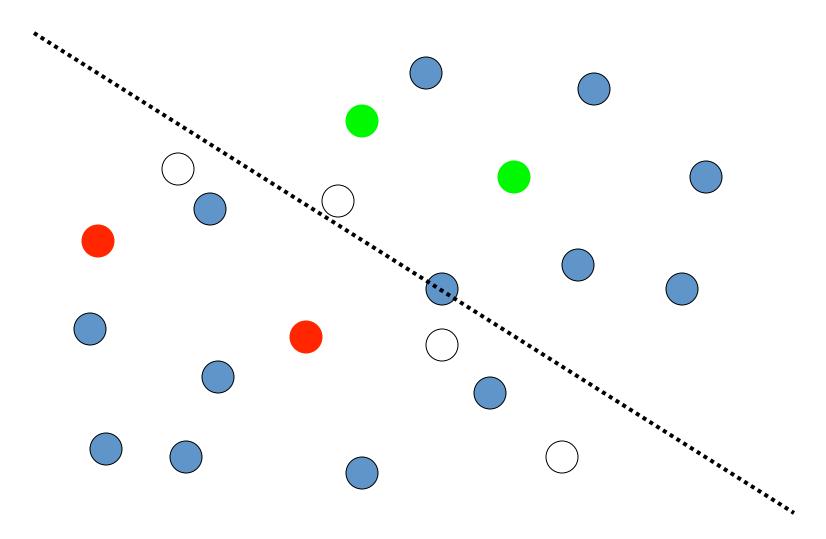
Step #1: Solicit Labels Via Active Learning [MM 01]



Step #2: Compute Boundary

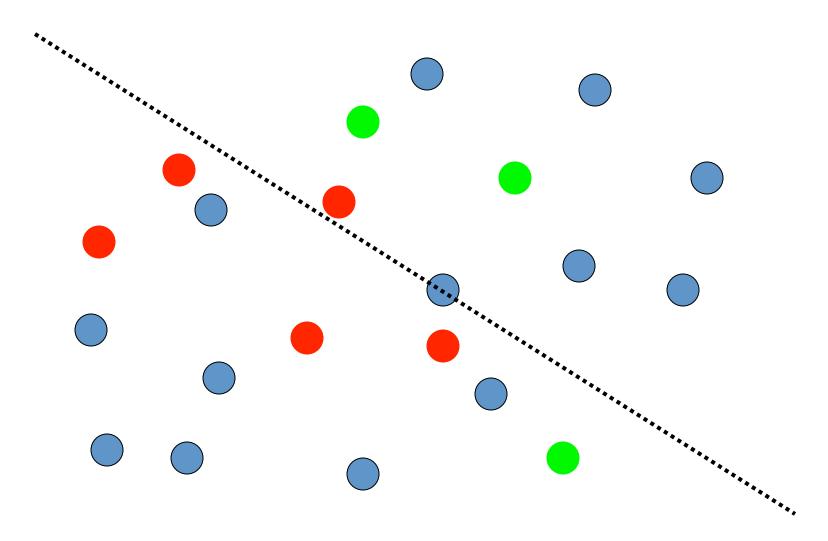


Step #3: Identify Useful Samples

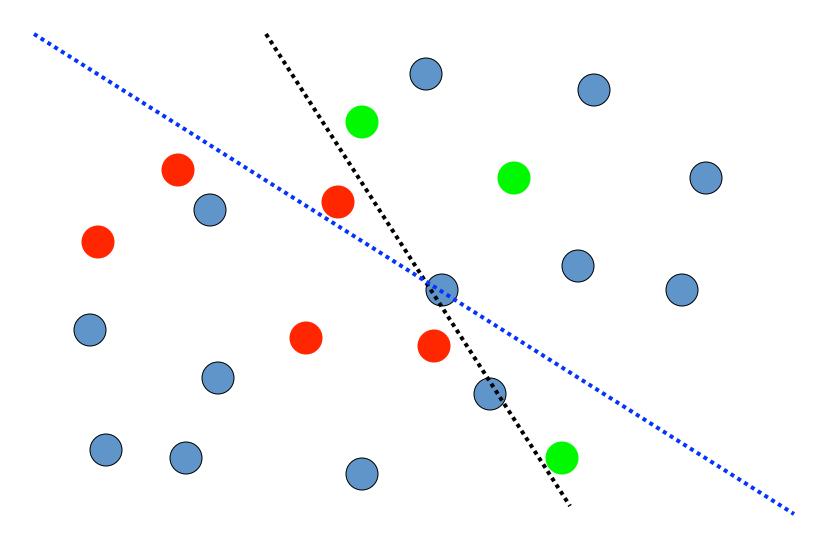




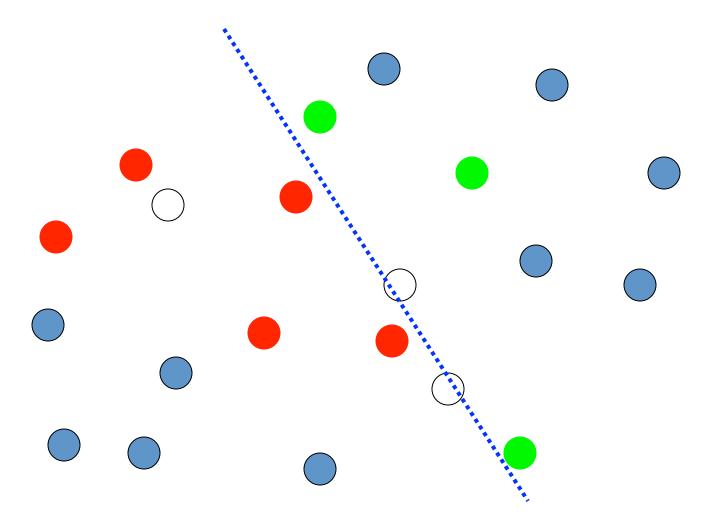
Step #4: Solicit Feedback



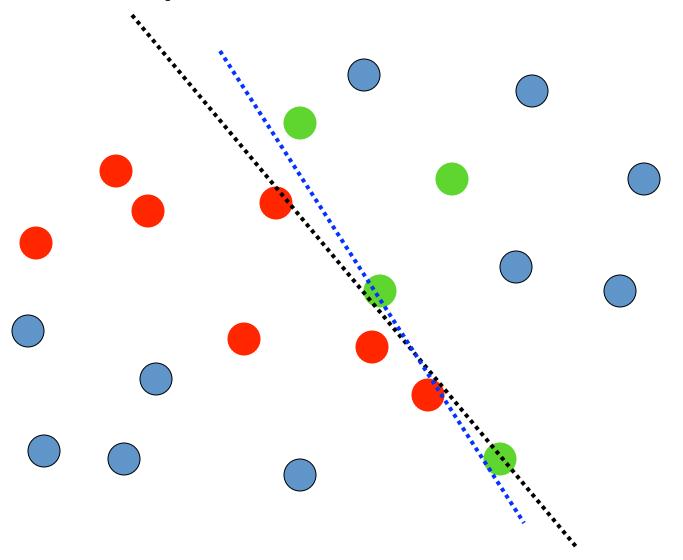
Step #5: Refine Boundary



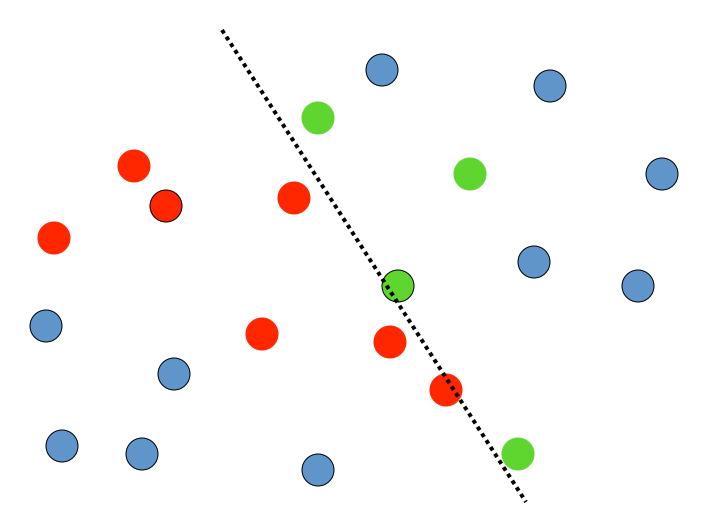
Step #6: Identify Samples



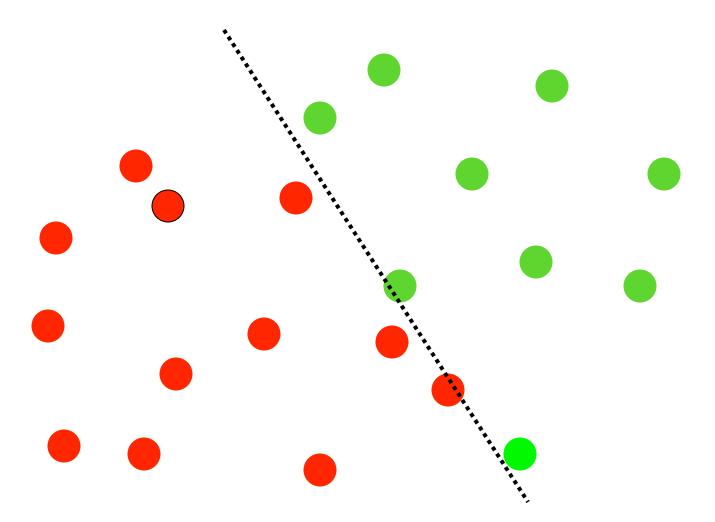
Step #7: User Feedback



Step #8: Refine Boundary



Step #9: Classify Data

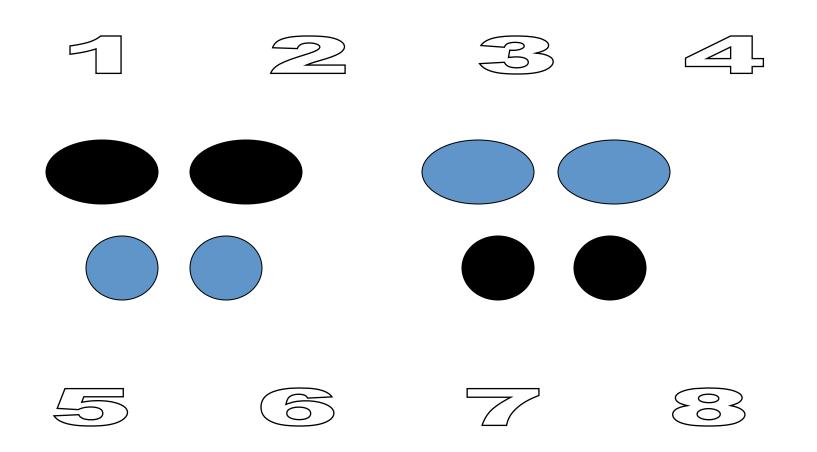


Observations

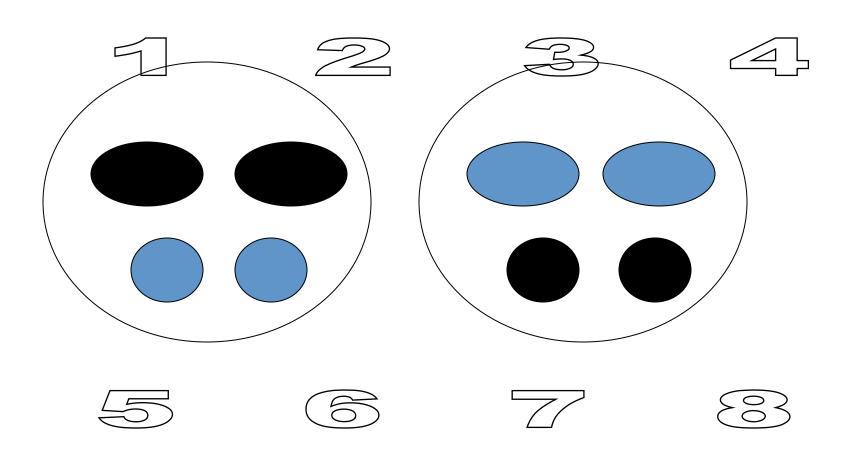
- Identify good samples
- Collect diversified samples
- Provide useful results much earlier
- Eventually, if all data have been labeled, classification accuracy converges
- Next, how to quantify similarity?
 - One way is to hand-craft a kernel matrix
 - The other is to learn a good manifold

Similarity?

Distance Function Formulation



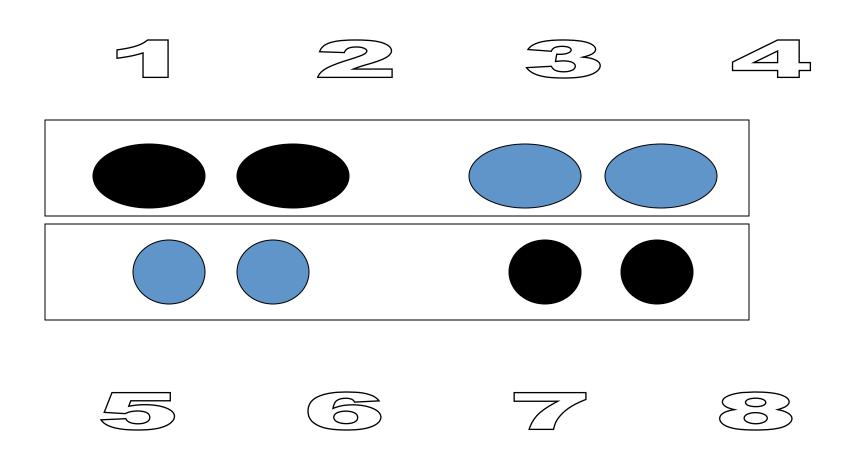
Group by Proximity



Group by Proximity

	x 1	x2	x 3	x4	х5	x6	x 7	8 x	
x 1	1	.7	.4	.3	.7	.6	.2	.1	
x2		1	.4	.3	.6	.7	.3	.2	
x 3			1	.7	.3	.4	.7	.6	
x4				1	.1	.2	.6	.7	
x5					1	.7	.3	.2	
x6						1	.6	.4	
x7							1	.7	
x8								1	

Group by Shape

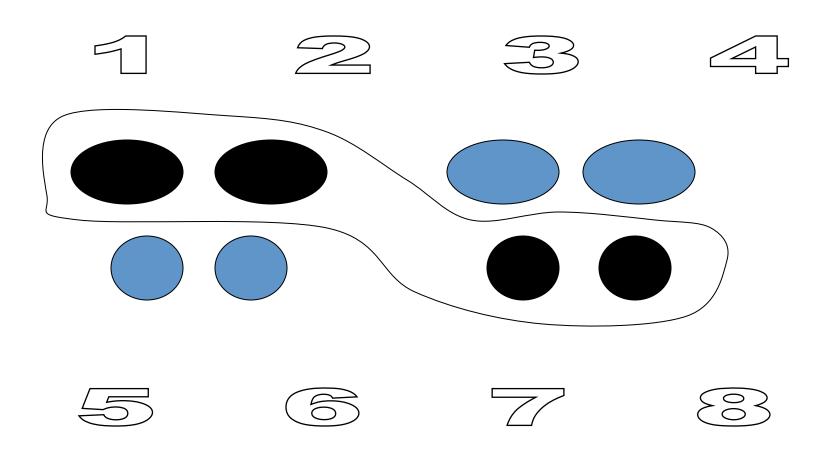


Group by Shape

	x 1	x2	x 3	x4	x5	x6	x 7	x8
x 1	1	.7	.7	.7	.2	.2	.2	.2
x2		1	.7	.7	.2	.2	.2	.2
x 3			1	.7	.2	.2	.2	.2
x4				1	.2	.2	.2	.2
x 5					1	.7	.7	.7
x6						1	.7	.7
x7							1	.7
x8								1

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Group by Color

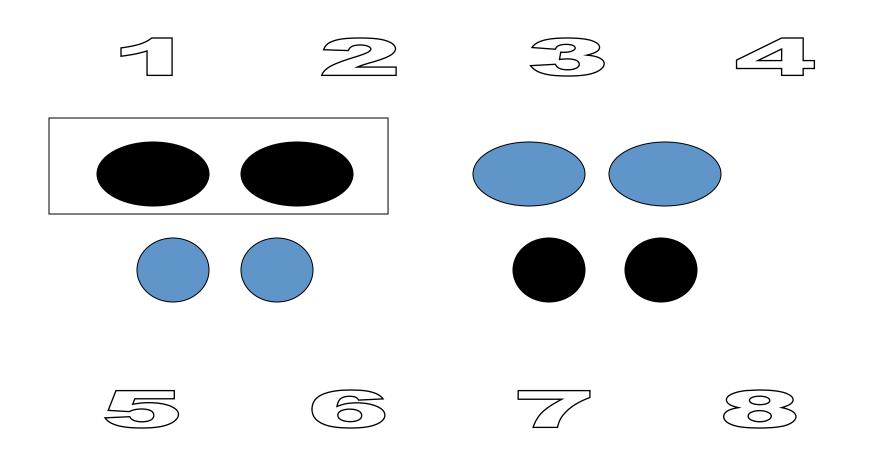


Group by Color

	x 1	x2	x 3	x4	x5	x6	x7	x8
x 1	1	.7	.3	.3	.3	.2	.2	.7
x2		1	.3	.3	.3	.3	.7	.7
x 3			1	.7	.7	.7	.3	.3
x4				1	.7	.7	.3	.3
x5					1	.7	.3	.3
x6						1	.3	.3
x7							1	.7
x8								1

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Similarity? Distance Function Formulation



NORMAL		CANCEROUS
	"A" IS FOR ASYMMETRY • If you draw a line through the middle of the mole, the halves of a melanoma won't match in size.	
	"B" IS FOR BORDER • The edges of an early melanoma tend to be uneven, crusty or notched.	
	"C" IS FOR COLOR • Healthy moles are uniform in color. A variety of colors, especially white and/or blue, is bad.	
	"D" IS FOR DIAMETER • Melanomas are usually larger in diameter than a pencil eraser, although they can be smaller.	
1/26/2015	"E" IS FOR EVOLVING • When a mole changes in size, shape or color, or begins to bleed or scab, this pointesto thanges.	0

Group by Labels Update the Kernel Matrix

	x 1	x2	x 3	x4	x5	x6	x 7	x8	
x 1	1	.7	.3	.3	.3	.2	.2	.7	
x2		1	.7	.3	.3	.3	.2	.7	
x 3			1	.7	.7	.7	.3	.3	
x4				1	.7	.7	.3	.3	
x5					1	.7	.3	.3	
x6						1	.3	.3	
x7							1	.7	
x8								1	

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Similarity Theories

- Objects are similar in all respects (Richardson 1928)
- Objects are similar in some respects (Tversky 1977)
- Similarity is a process of determining respects, rather than using predefined respects (Goldstone 94)

Traditional Similarity Theories

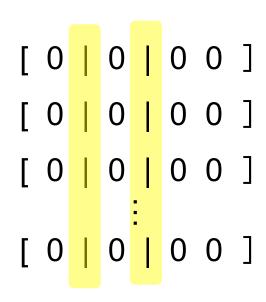
- Objects are similar in all or some respects
- Minkowski Function

$$-D = (\sum_{i=1..M} (p_i - q_i)^n)^{1/n}$$

 Weighted Minkowski Function

$$-D = (\sum_{i=1..M,} w_i(p_i - q_i)^n)^{1/n}$$

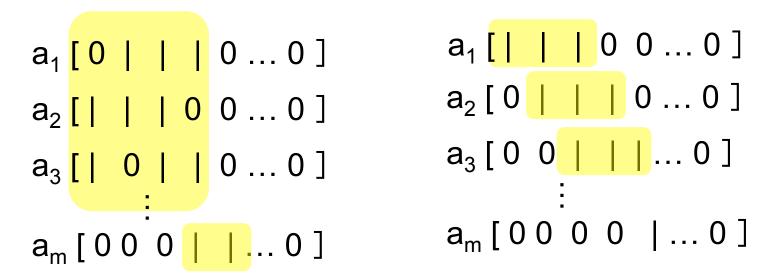
 Same w is imposed to app pairs of objects p and q



DPF: Dynamic Partial Function

[B. Li, E. Chang, et al, MM Systems 2013]

 Similarity is a process of determining respects, rather than using predefined respects (Goldstone 94)



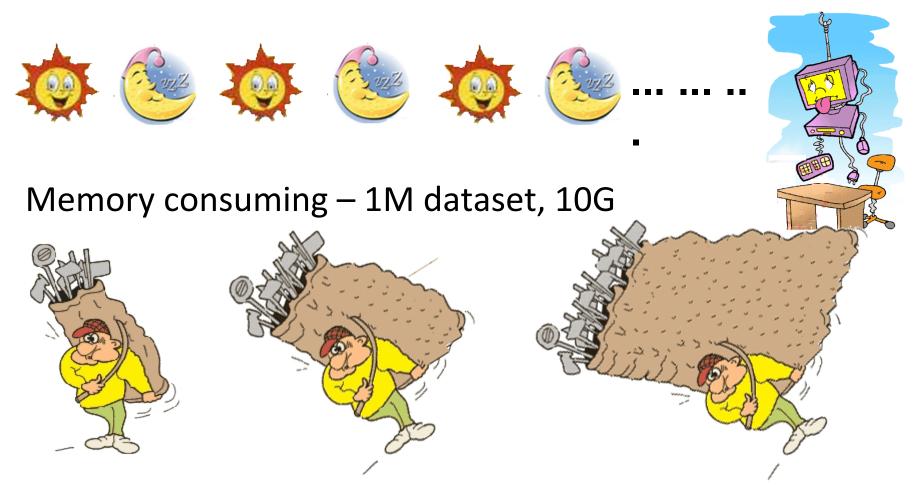
Lecture #2 Preview

- How can deep learning help learn features?
- Sparse coding confirms DPF on the right track

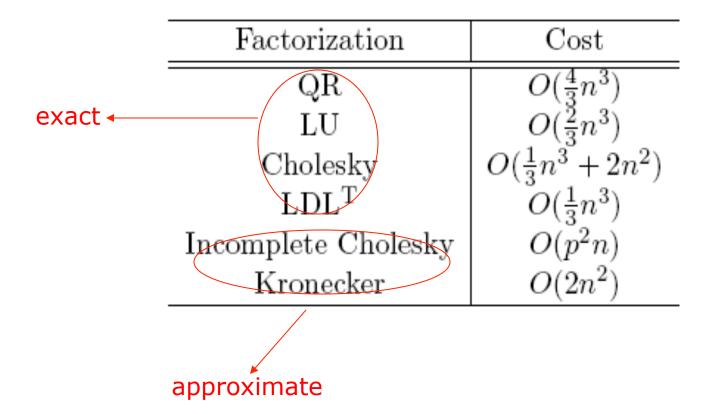
- For now, need to speed up the kernel method
 - Suppose we have a kernel matrix representing pairwise similarity of data instances
 - How to speed up SVM learning w/ kernel?

SVM Bottlenecks

Time consuming – 1M dataset, 8 days



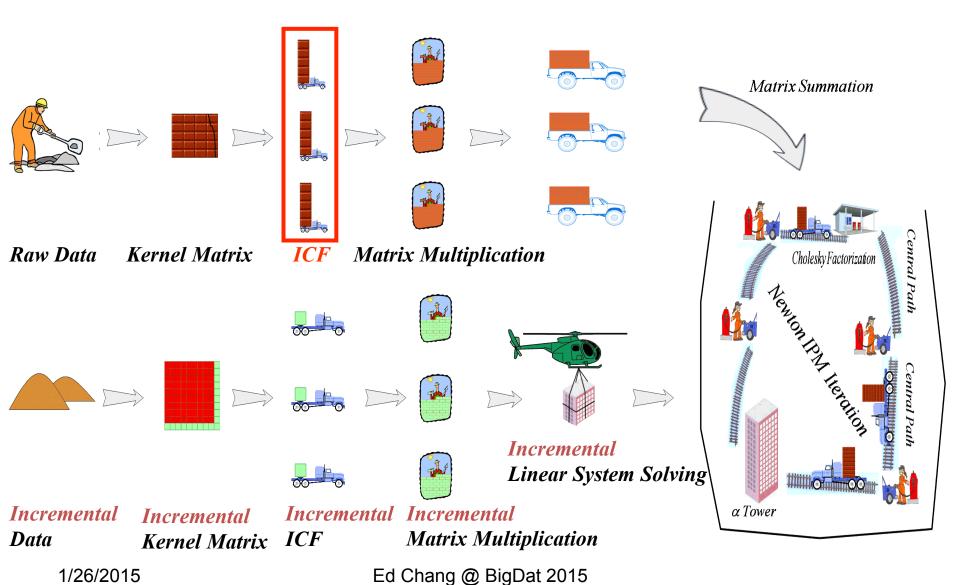
Matrix Factorization Alternatives



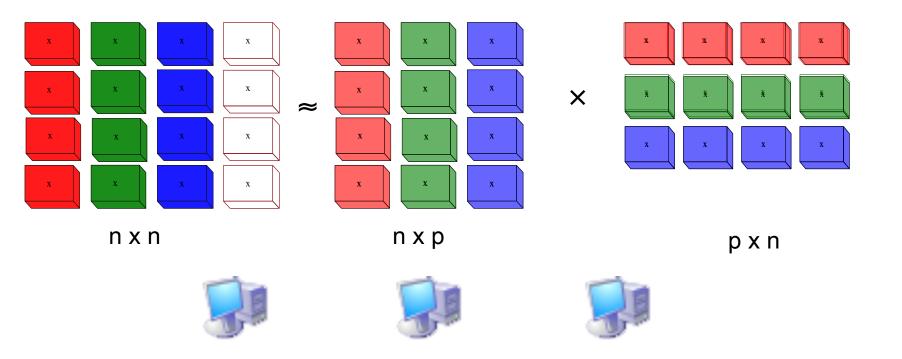
PSVM [E. Chang, et al, NIPS 07]

- Column-based Incomplete Cholesky Factorization (ICF)
 - Slower than row-based on single machine
 - Parallelizable on multiple machines
- Changing IPM computation order to achieve parallelization
 - $-D = (A \times B) \times C$
 - $-D = A \times (B \times C)$

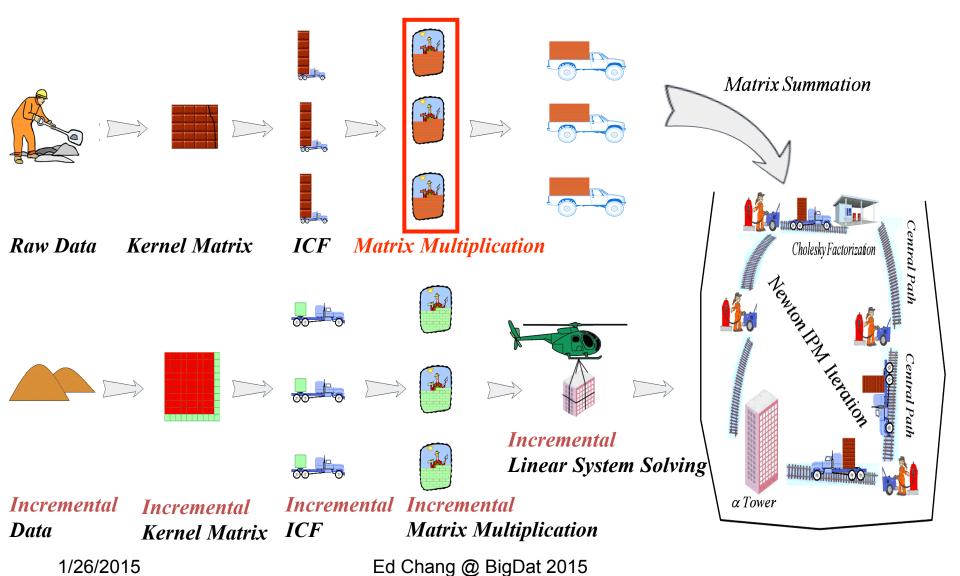
Parallelized and Incremental SVM



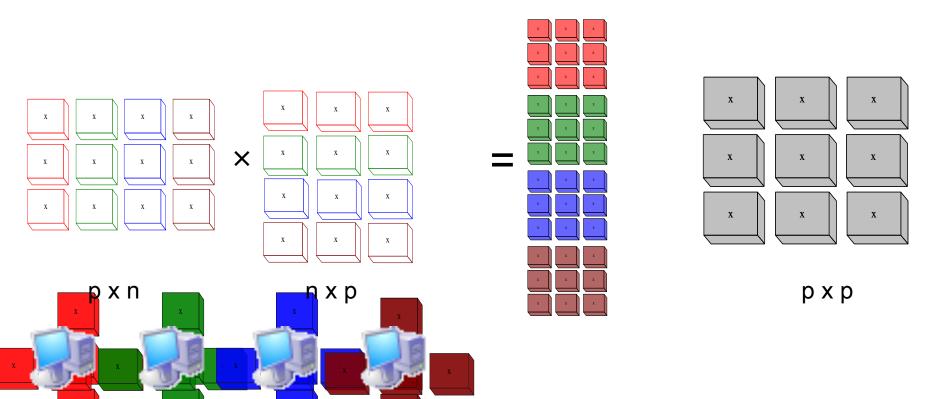
Incomplete Cholesky Factorization (ICF)



Parallelized and Incremental SVM



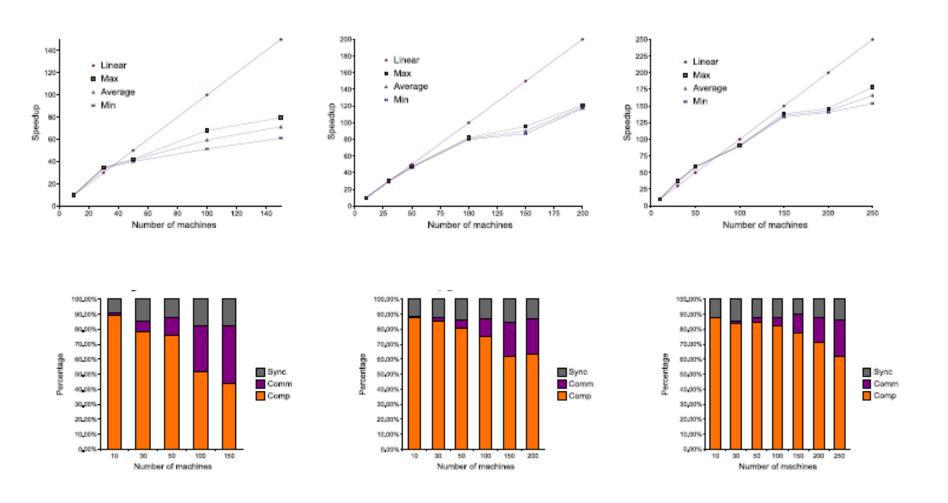
Matrix Product



Speedup

	I	mage (20	0k)	CoverType (500k)			R)	
Machines	Time	e (s)	Speedup	Time (s) Speedup		Time	(s)	Speedup	
10	1,958	(9)	10*	16,818	(442)	10*	45,135	(1373)	10*
30	572	(8)	34.2	5,591	(10)	30.1	12,289	(98)	36.7
50	473	(14)	41.4	3,598	(60)	46.8	7,695	(92)	58.7
100	330	(47)	59.4	2,082	(29)	80.8	4,992	(34)	90.4
150	274	(40)	71.4	1,865	(93)	90.2	3,313	(59)	136.3
200	294	(41)	66.7	1,416	(24)	118.7	3,163	(69)	142.7
250	397	(78)	49.4	1,405	(115)	119.7	2,719	(203)	166.0
500	814	(123)	24.1	1,655	(34)	101.6	2,671	(193)	169.0
LIBSVM	4,334	NA	NA	28,149	NA	NA	184,199	NA	NA

Overheads

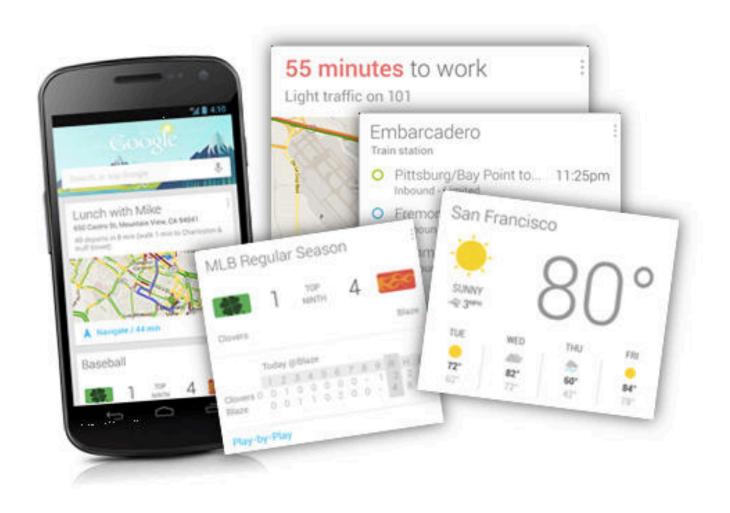


Key Technical Challenges

- Acquire labeled data (most data are unlabeled)
- Formulate distance function
- Train a classifier
- Classify unlabeled data
 - Fast
 - Low power consumption

Context-Aware Computing

[Chang, et al. VLDB 2013, 2014]

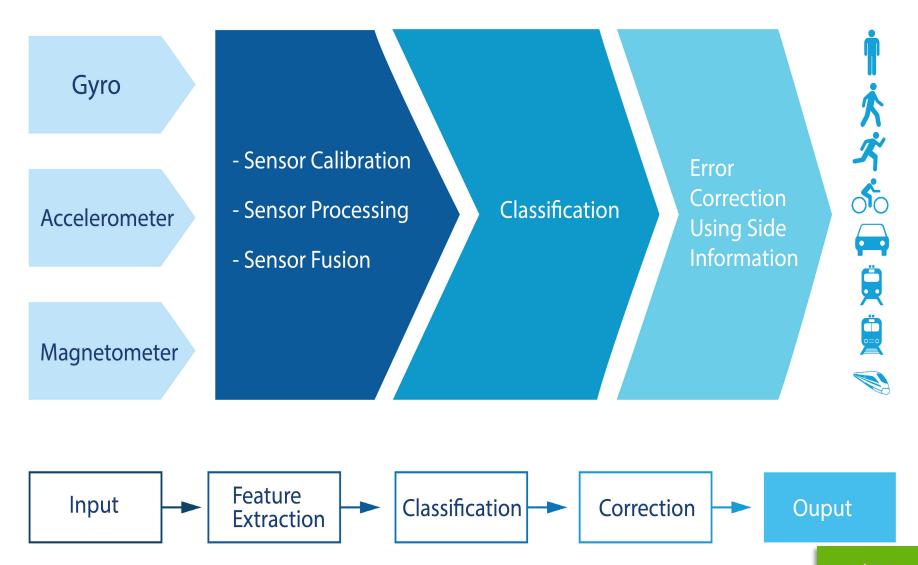


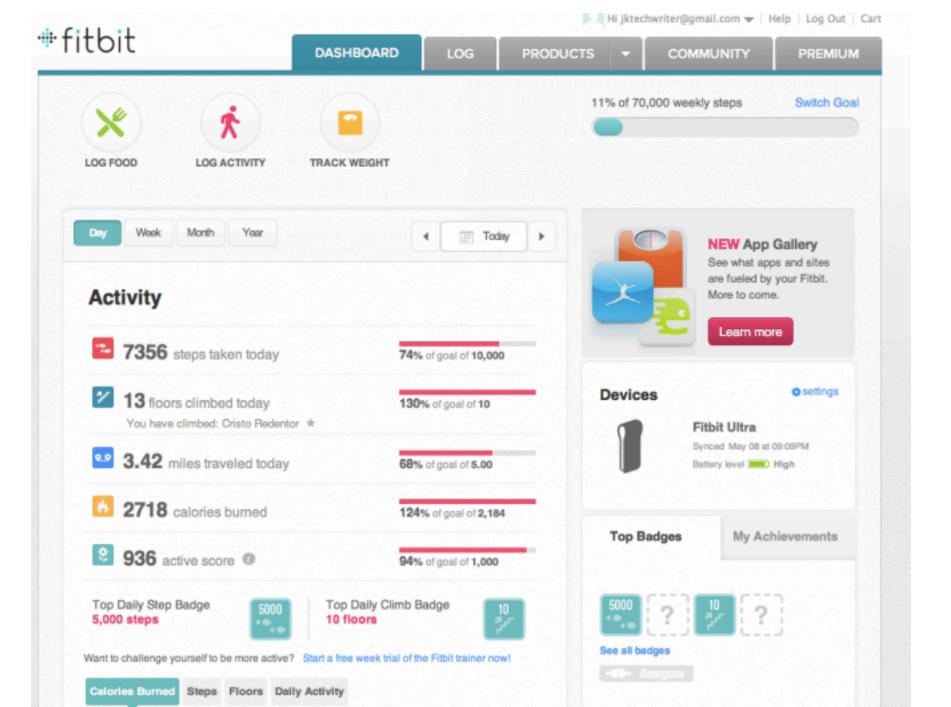
Transportation-mode Detection



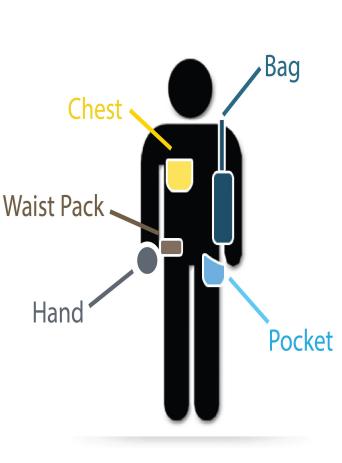
Transportation Mode Detection

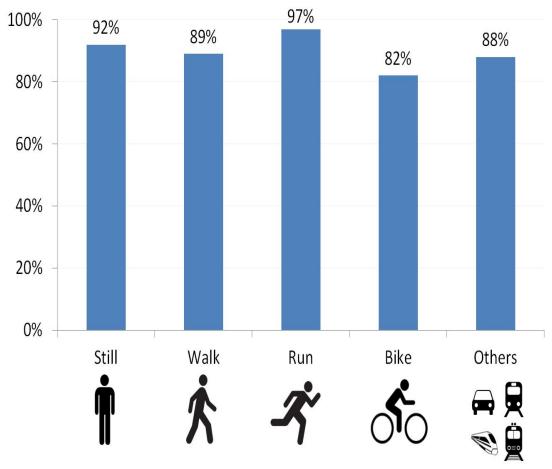
[Chang, et al., VLDB 2013, 2014]





Data Driven Classification

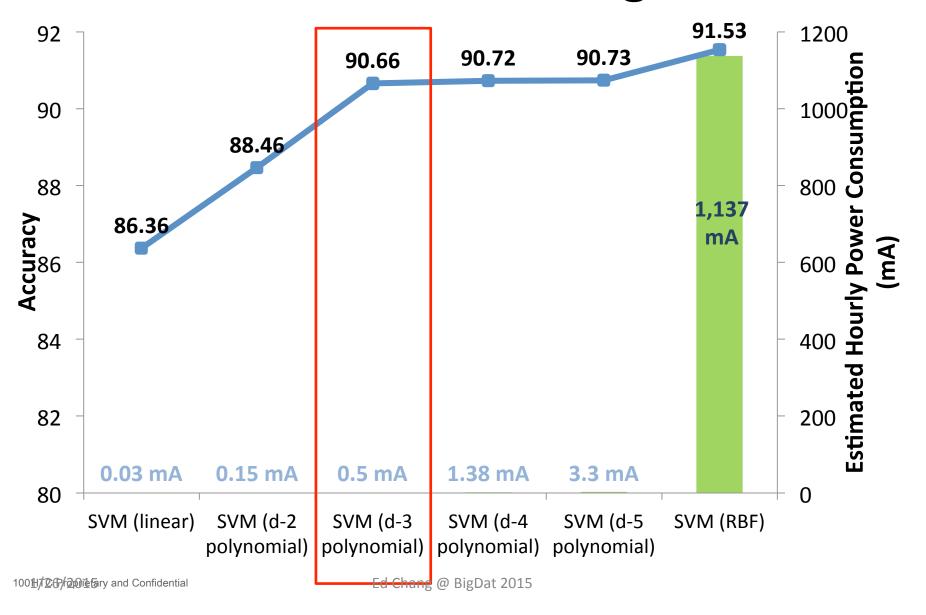




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Sensor Hub Saving 1/2



SVMs → Max Margin M

- Min $|w|^2/2$
 - subject to $y_i(x_iw+b) \ge 1$
 - -i = 1,...,N
- Lp = min_{w,b} $|w|^2/2 + \sum_{i=1..N} \alpha_i [y_i(x_iw+b)-1]$
- $w = \sum_{i=1..N} \alpha_i y_i x_i$
- $0 = \sum_{i=1..N} \alpha_i y_i$

Wolfe Dual

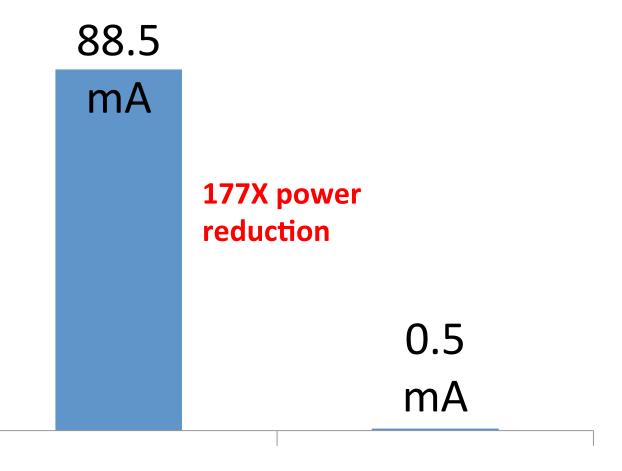
- Ld = $\sum_{i=1..N} \alpha 1/2 \sum_{i,j=1..N} \alpha_i \alpha_j y_i y_j x_i x_j$
- Subject to
 - $-\alpha_i \ge 0$
 - $-\alpha_{i}[y_{i}(x_{i}w+b)-1]=0$
 - KKT conditions
 - $\alpha_i > 0$, $y_i(x_i w + b) = 1$ (Support Vectors)
 - $\alpha_i = 0$, $y_i(x_iw+b) > 1$

Class Prediction

- $y_q = w x_q + b$
- $w = \sum_{i=1..N} \alpha_i y_i x_i$
- $y_q = sign(\sum_{i=1..N} \alpha_i y_i(x_i.x_q) + b)$

Sensor Hub Saving 2/2

- Power Consumption by MCU/CPU
- Classifier: SVM (degree-3 polynomial)



Applications & Algorithms

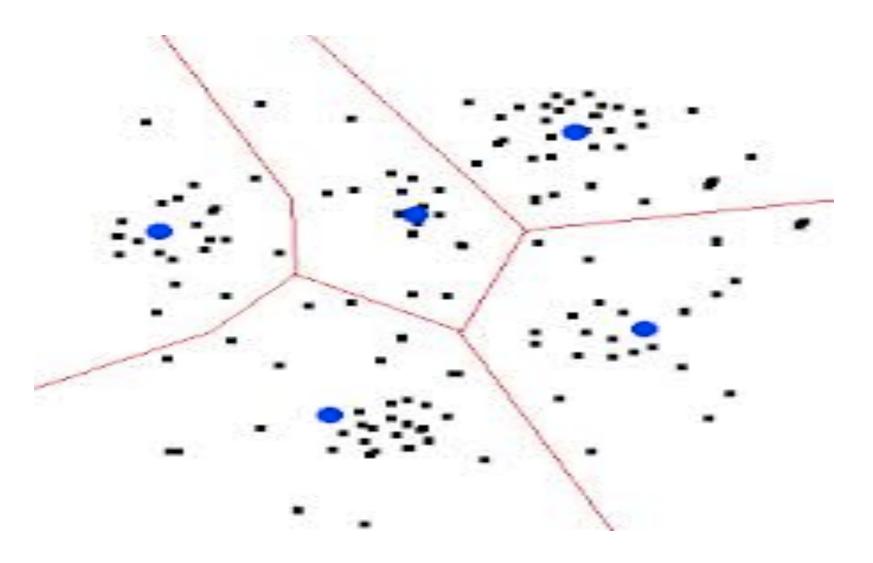
- Applications
 - HTC XPRICE Tricorder
 - Context-aware Computing
- Key Algorithms
 - Frequent Itemset Mining [ACM RS 08]
 - Latent Dirichlet Allocation [WWW 09, TIST 10]
 - Support Vector Machines [MM 01, MS 03, NIPS 07, VLDB 14]
- Spectral Clustering [ECML 08, PAMI 10]
 - Deep Learning [NIPS 12, OSDI 14]
- Perspectives and Opportunities

Clustering

Most Widely Used Pattern Recognition Subroutine

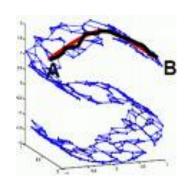
- Microarray Data Analysis
- Ultrasound Image Segmentation
- Document Pattern Discovery
- High-dimensional Data Indexing

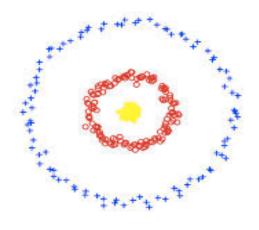
K Means



Spectral Clustering [A. Ng, M. Jordan]

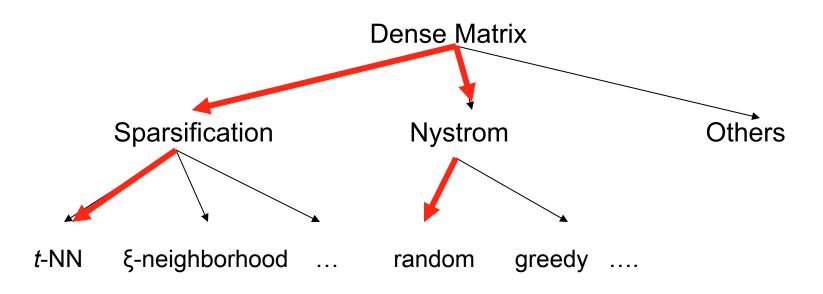
- Exploit pairwise similarity of data instances
- Key steps
 - Construct pairwise similarity matrix
 - e.g., using Geodisc distance
 - Compute the Laplacian matrix
 - Apply eigendecomposition
 - Perform k-means





Scalability Problem

- Quadratic computation of nxn matrix
- Approximation methods



Sparsification vs. Sampling

- Construct the dense similarity matrix S
- Sparsify S
- Compute Laplacian matrix L

$$L = I - D^{-1/2}SD^{-1/2}, \quad D_{ii} = \sum_{j=1}^{n} S_{ij}$$

- Apply ARPACLK on L
- Use k-means to cluster rows of V into k groups

- Randomly sample *l* points, where *l* << *n*
- Construct dense similarity matrix [A B] between *l* and *n* points
- Normalize A and B to be in Laplacian form

$$R = A + A^{-1/2}BB^{T}A^{-1/2};$$

$$R = U\sum U^{T}$$

• *k*-means

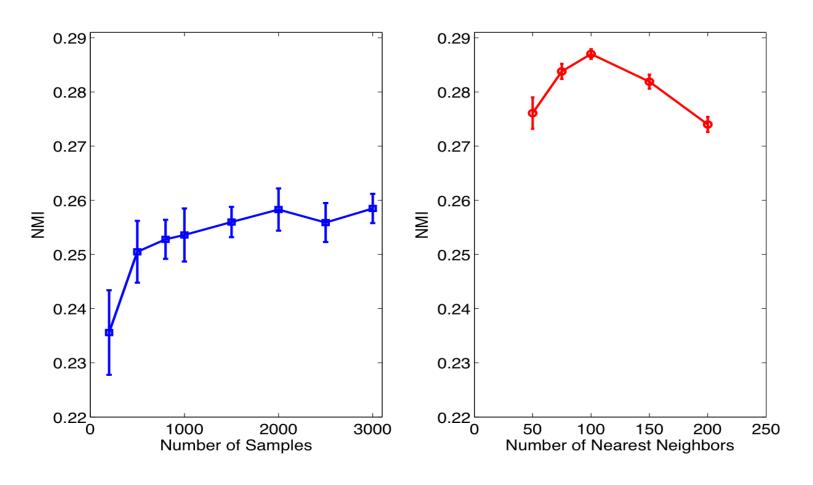
Empirical Study [song, et al., ecml 08]

- Dataset: RCV1 (Reuters Corpus Volume I)
 - A filtered collection of 193,944 documents in 103 categories
- Photo set: PicasaWeb
 - *637,137* photos
- Experiments
 - Clustering quality vs. computational time
 - Measure the similarity between CAT and CLS
 - Normalized Mutual Information (NMI)

$$NMI(CAT; CLS) = \frac{I(CAT; CLS)}{\sqrt{H(CAT)H(CLS)}}$$

Scalability

NMI Comparison (on RCV1)



Nystrom method

Sparse matrix approximation

Speedup Test on 637,137 Photos

K = 1000 clusters

	Eigensolver			k-means		
Machines	Time	(sec.)	Speedup	Time	(sec.)	Speedup
1		177	· · · ·		1	-
2	8.074	$\times 10^4$	2.00	3.609	$\times 10^4$	2.00
4	4.427	$\times 10^4$	3.65	1.806	$\times 10^4$	4.00
8	2.184	$\times 10^4$	7.39	8.469	$\times 10^3$	8.52
16	9.867	$\times 10^{3}$	16.37	4.620	$\times 10^{3}$	15 62
32	4.886	$\times 10^3$	33.05	2.021	$\times 10^3$	35.72
64	4.067			1.433		50.37
128	3.471		46.52	1.090	$\times 10^3$	66.22
256	4.021	$\times 10^3$	40.16	1.077	$\times 10^3$	67.02

 Achiever linear speedup when using 32 machines, after that, sub-linear speedup because of increasing communication and sync time

Sparsification vs. Sampling

	Sparsification	Nystrom, random sampling
Information	Full n x n similarity scores	None
Pre-processing Complexity (bottleneck)	O(n ²) worst case; easily parallizable	O(nl), l << n
Effectiveness	Good	Not bad (Jitendra M., PAMI)

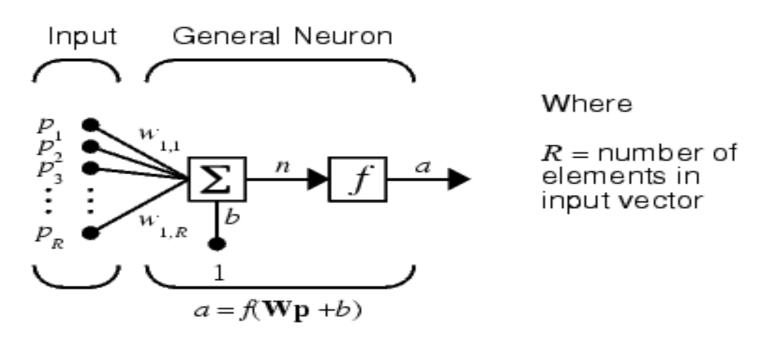
Applications & Algorithms

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Multiple-Layer Networks

Neuron Network (NN) Model

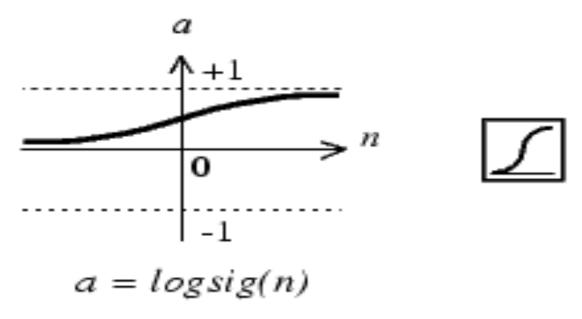
An elementary neuron with R inputs is shown below. Each input is weighted with an appropriate w. The sum of the weighted inputs and the bias forms the input to the transfer function f. Neurons can use any **differentiable transfer function** f to generate their output.



NN Model

Transfer Functions (Activition Function)

Multilayer networks often use **the log-sigmoid** transfer function **logsig**. The function logsig generates outputs between **0** and **1** as the neuron's net input goes from negative to positive infinity

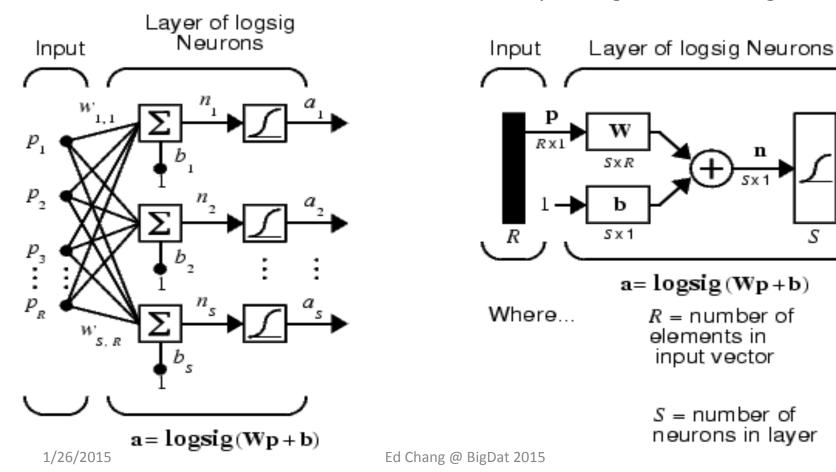


Log-Sigmoid Transfer Function

NN Model

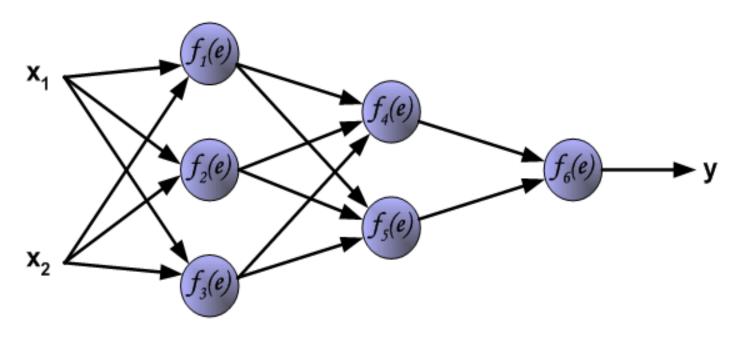
Feedforward Network

A single-layer network of S logsig neurons having R inputs is shown below in full detail on the left and with a layer diagram on the right.

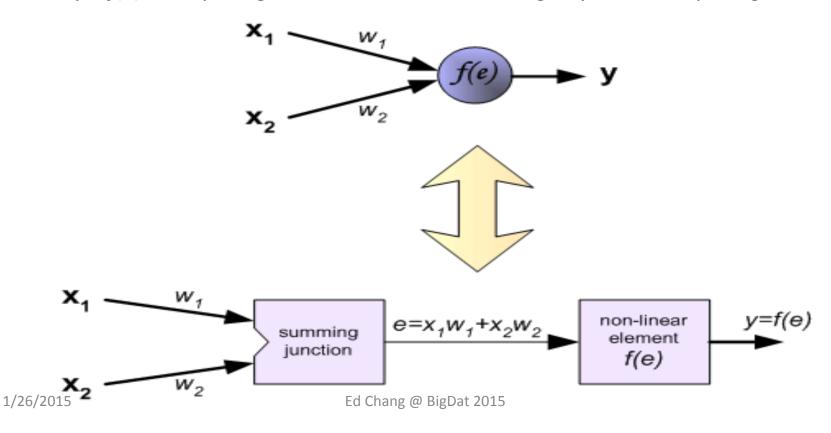


NN Model Learning Algorithm

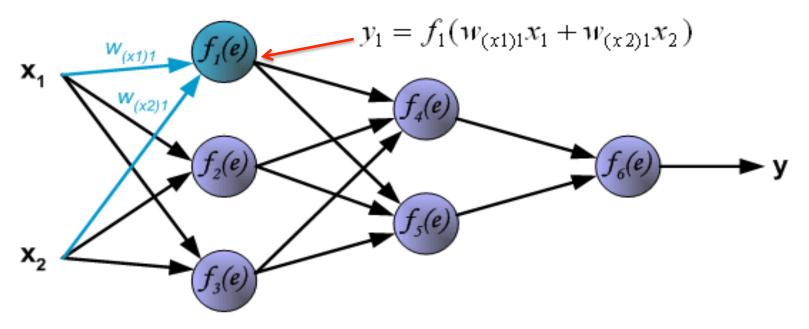
The following slides describes **learning process** of multi-layer neural network employing **backpropagation** algorithm. To illustrate this process the three layer neural network with two inputs and one output, which is shown in the picture below, is used:

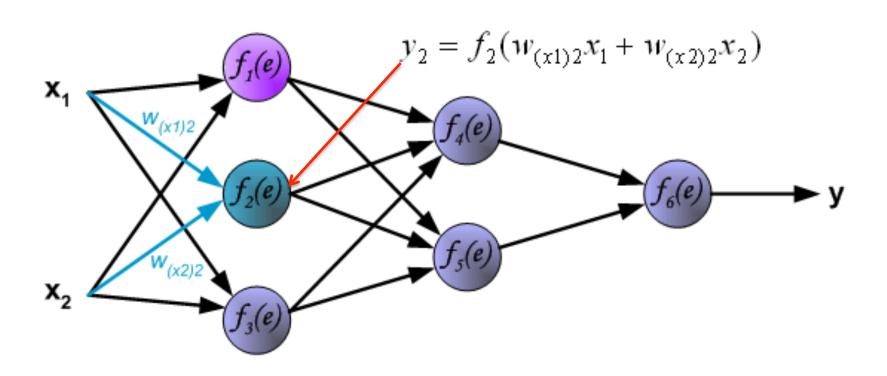


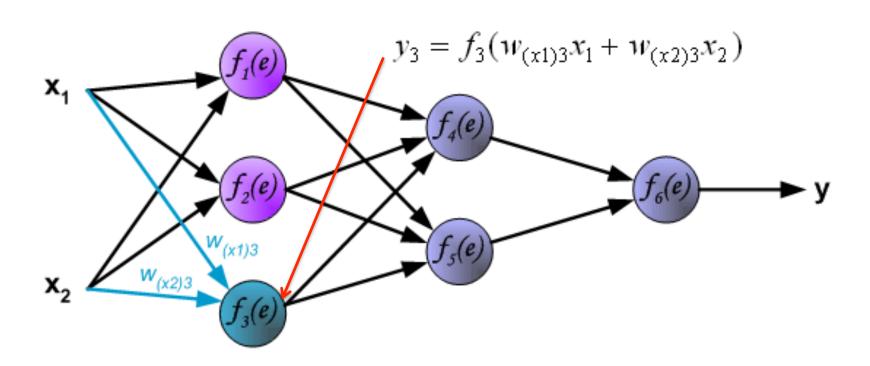
Each neuron is composed of two units. First unit adds products of weights coefficients and input signals. The second unit realizes a nonlinear function, called neuron transfer (activation) function. Signal e is adder output signal, and y = f(e) is output signal of nonlinear element. Signal y is also output signal of



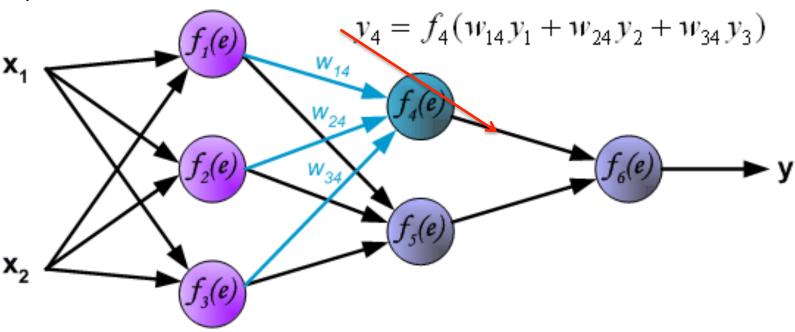
Pictures below illustrate how signal is forward-feeding through the network, Symbols $w_{(xm)n}$ represent weights of connections between network input x_m and neuron n in input layer. Symbols y_n represents output signal of neuron n.

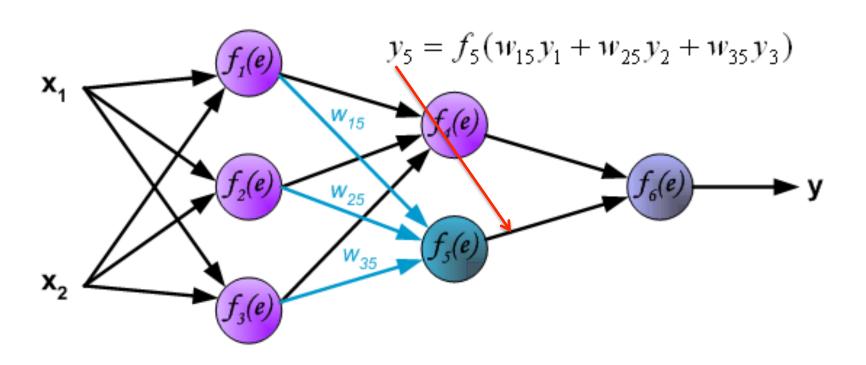






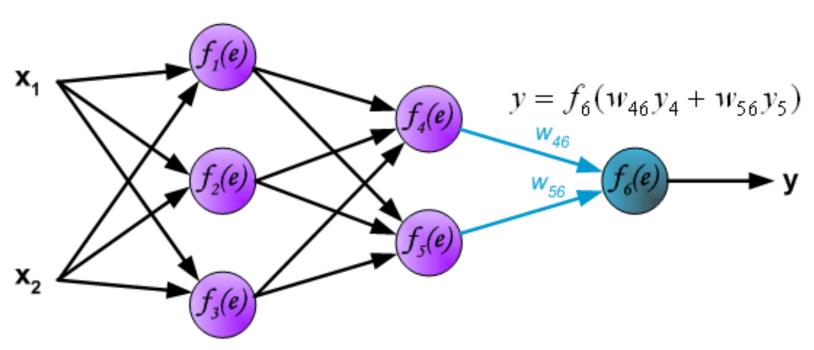
Propagation of signals through the hidden layer. Symbols w_{mn} represent weights of connections between output of neuron m and input of neuron n in the next layer.





Learning Algorithm: Forward Pass

Propagation of signals through the output layer.

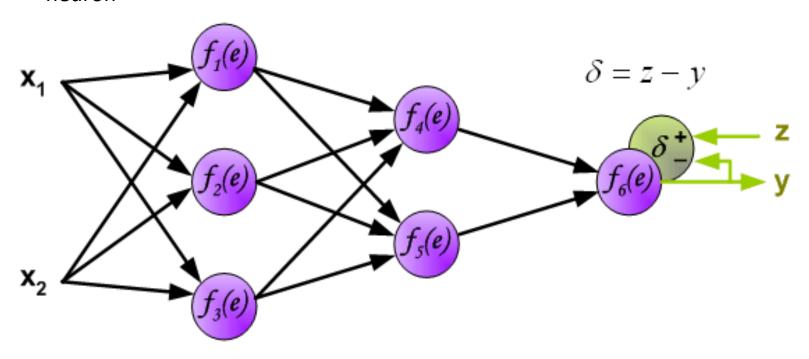


To teach the neural network we need training data set. The training data set consists of input signals (x_1 and x_2) assigned with corresponding target (desired output) z.

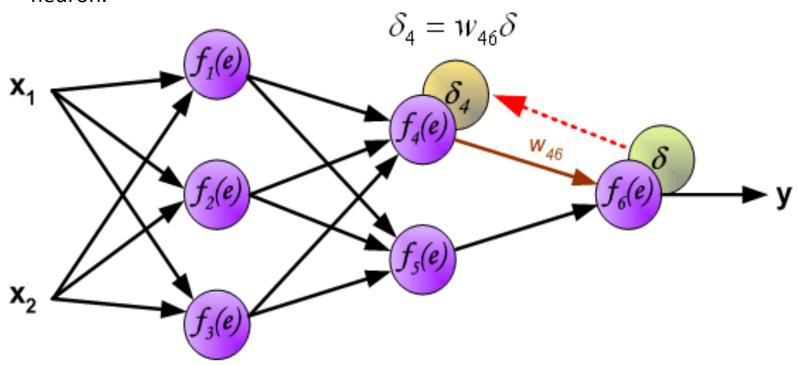
The network training is an iterative process. In each iteration weights coefficients of nodes are modified using new data from training data set. Modification is calculated using algorithm described below:

Each teaching step starts with forcing both input signals from training set. After this stage we can determine output signals values for each neuron in each network layer.

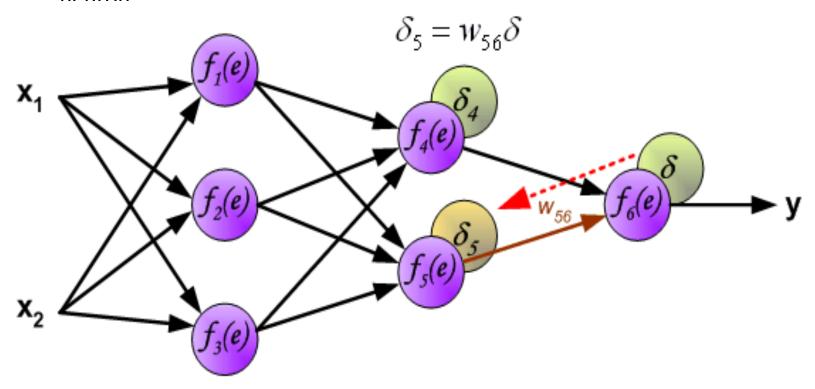
In the next algorithm step the output signal of the network y is compared with the desired output value (the target z), which is found in training data set. The difference is called error signal δ of output layer neuron



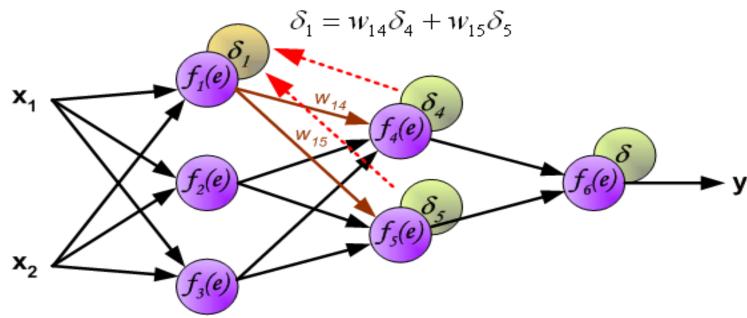
The idea is to propagate error signal δ (computed in single teaching step) back to all neurons, which output signals were input for discussed neuron.



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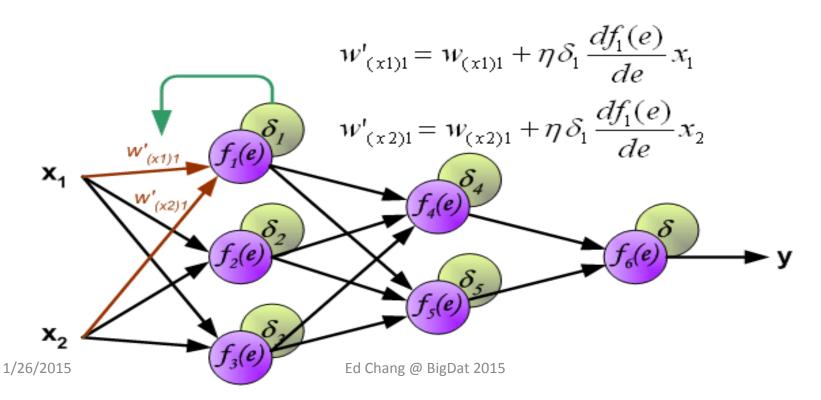


The weights' coefficients w_{mn} used to propagate errors back are equal to this used during computing output value. Only the direction of data flow is changed (signals are propagated from output to inputs one after the other). This technique is used for all network layers. If propagated errors came from few neurons they are added. The illustration is below:

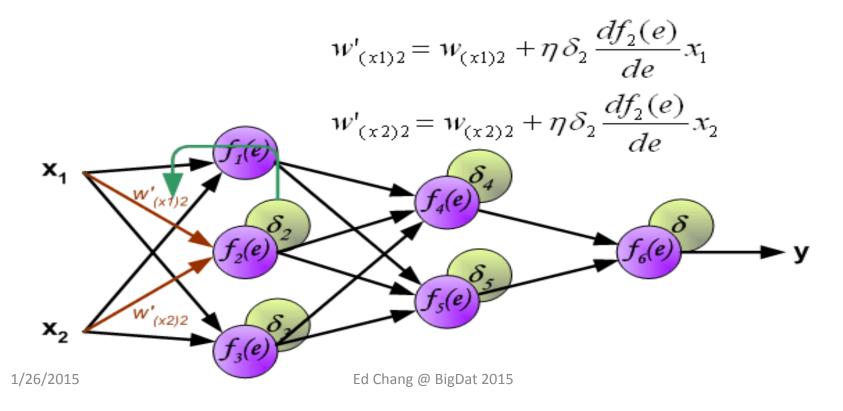


1/26/2015

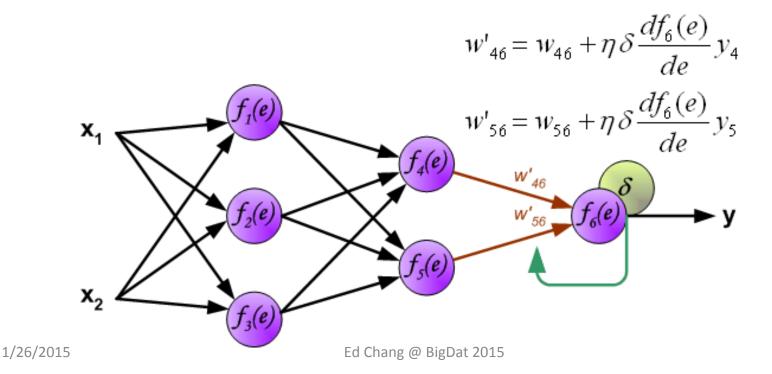
When the error signal for each neuron is computed, the weights coefficients of each neuron input node may be modified. In formulas below df(e)/de represents derivative of neuron activation function (which weights are modified).



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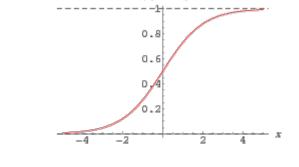
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Sigmoid function f(e) and its derivative f'(e)

$$f(e) = \frac{1}{1 + e^{-\beta e}}$$
, β is the paramter for slope

Hence



$$f'(e) = \frac{df(e)}{de} = \frac{d\left(\frac{1}{1+e^{-\beta e}}\right)}{d(1+e^{-\beta e})} \frac{df(e^{-\beta e})}{de}$$

$$f'(e) = \frac{-\beta}{(1+e^{-\beta e})^2} e^{-\beta e} = \frac{-\beta}{(1+e^{-\beta e})^2} e^{-\epsilon}$$

$$= \frac{1}{(1+e^{-\beta e})} \frac{-\beta e^{-e}}{(1+e^{-\beta e})} = f(e)(1-\beta f(e))$$

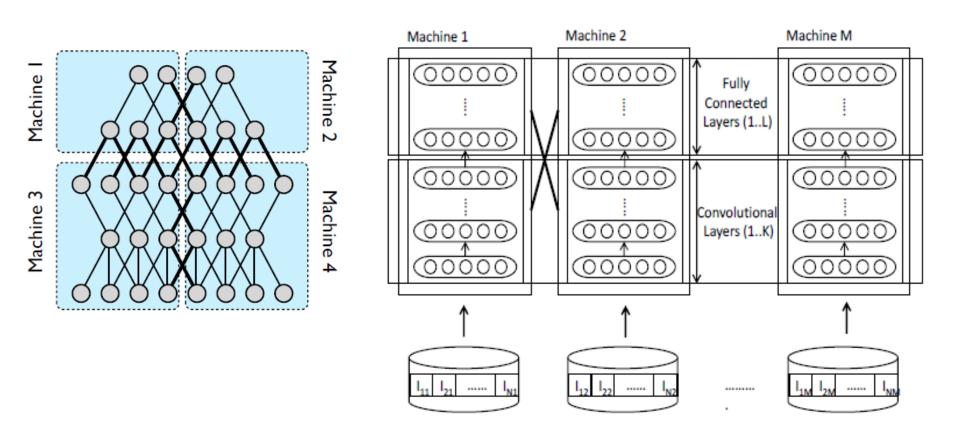
For simplicity, paramter for the slope $\beta = 1$

$$f'(e) = f(e)(1 - f(e))$$

http://link.springer.com/chapter/10.1007%2F3-540-59497-3_175#page-1

Model Parallelism

[J. Dean et al, NIPS 2012]



Scalable Deep Learning Platform

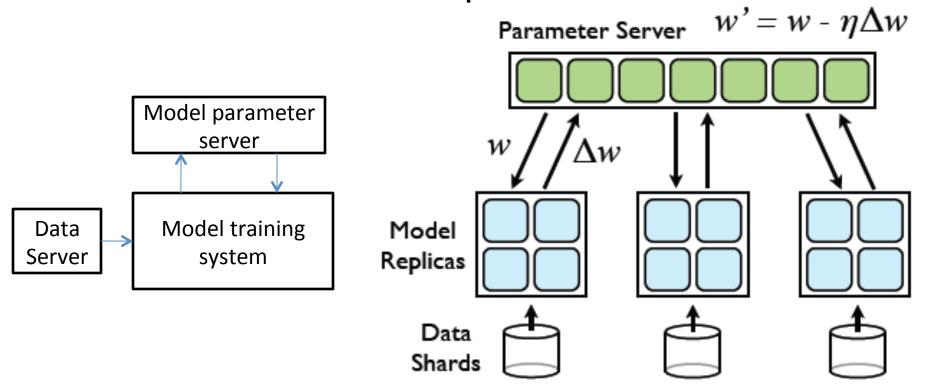
Microsoft Project ADAM

- Scalable training algorithm
 - Asynchronous SDG (stochastic gradient descent)
- Scalable model partitioning
 - Model parallelism
- Scalable model parameter store
 - Data parallelism
- Scalable data transformations
 - Data preprocessing and augmentation

Scalability of Backpropagation

[Project Adam, OSDI 2014]

 Based on the Multi-Spert system and exploits both model and data parallelism



[1/թեթացրել P., and Asanović, K. 199թ Թարթանական network training on Multi-Spert.

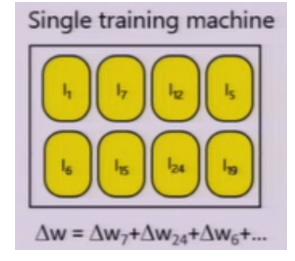
Model Training Optimizations (1/3)

- Multi-threaded training
 - Multiple threads are sharing the same model weights
 - NUMA-aware allocations to reduce cross-memory bus traffic
- Fast weight updates

Update the sharded model weights locally WITHOUT

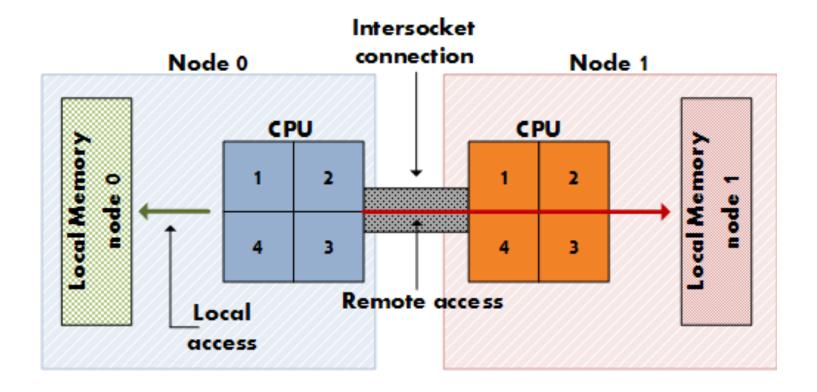
using locks

- Weight updates are commutative and associative
- Neural networks are resilient to the noise introduced



NUMA

Non Uniform Memory Access

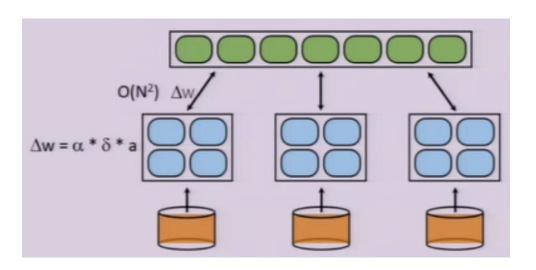


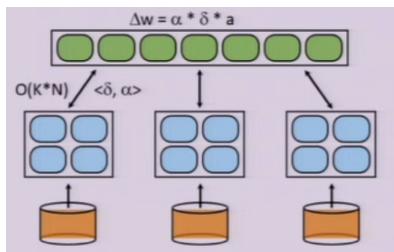
Model Training Optimizations (2/3)

- Reducing memory copies
 - Do not copy the parameters, pass a pointer instead
- Memory system optimizations
 - Fit the working sets in the L3 cache (e.g., 8M)
- Mitigating the impact of slow machines
 - Threads to process multiple images in parallel
 - Training epoch terminates when 75% of the model replicas are done → 20% speed up

Model Training Optimizations (3/3)

- Reduce the communication to the parameter server
 - Can also offload some computation work to the parameter server





Concluding Remarks

- More data is helpful, and hence big data
- Computational time is reduced by using virtually infinitely amount of resources
- Once computation is fully parallelized, IO cost can be reduced via hardware solutions
- Both algorithmic approach and system approach are required to achieve good speedup

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Edward Y. Chang **Foundations of Large-Scale Multimedia Information Management and Retrieval**Mathematics of Perception

Foundations of Large-Scale Multimedia Information Management and Retrieval Mathematics of Perception covers knowledge representation and semantic analysis of multimedia data and scalability in signal extraction, data mining, and indexing. The book is divided into two parts: Part I - Knowledge Representation and Semantic Analysis focuses on the key components of mathematics of perception as it applies to data management and retrieval. These include feature selection/reduction, knowledge representation, semantic analysis, distance function formulation for measuring similarity, and multimodal fusion. Part II - Scalability Issues presents indexing and distributed methods for scaling up these components for high-dimensional data and Web-scale datasets. The book presents some real-world applications and remarks on future research and development directions

The book is designed for researchers, graduate students, and practitioners in the fields of Computer Vision, Machine Learning, Large-scale Data Mining, Database, and Multimedia Information Retrieval.

Dr. Edward Y. Chang was a professor at the Department of Electrical & Computer Engineering, University of California at Santa Barbara, before he joined Google as a research director in 2006. Dr. Edward Y. Chang received his M.S. degree in Computer Science and Ph.D degree in Electrical Engineering, both from Stanford University.

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Mathematics of Perception





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