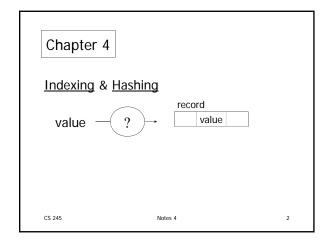
# CS 245: Database System Principles

# **Notes 4: Indexing**

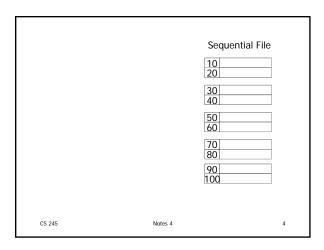
Hector Garcia-Molina

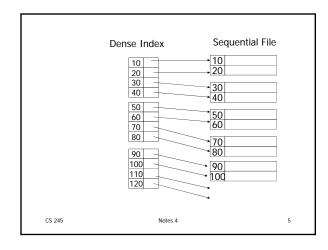
CS 245 Notes 4

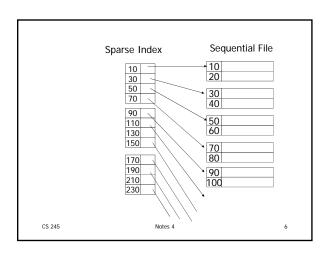


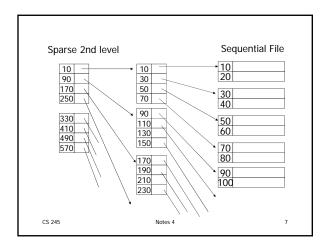
# **Topics**

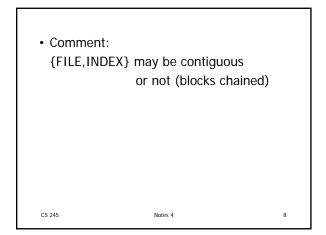
- Conventional indexes
- B-trees
- Hashing schemes







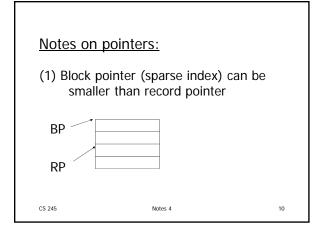




# **Question:**

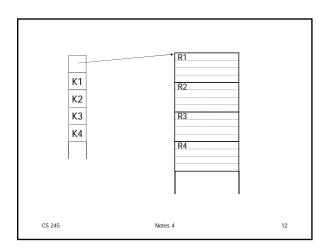
• Can we build a dense, 2nd level index for a dense index?

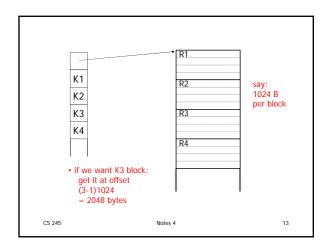
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# Notes on pointers:

(2) If file is contiguous, then we can omit pointers (i.e., compute them)





# Sparse vs. Dense Tradeoff Sparse: Less index space per record can keep more of index in memory Dense: Can tell if any record exists without accessing file

### (Later:

- sparse better for insertions
- dense needed for secondary indexes)

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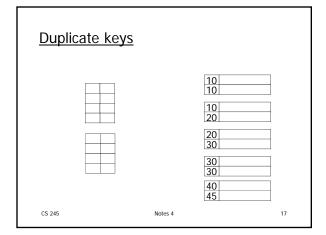
# Terms

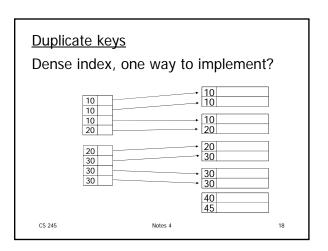
- · Index sequential file
- Search key (≠ primary key)
- Primary index (on Sequencing field)
- Secondary index
- Dense index (all Search Key values in)
- · Sparse index
- Multi-level index

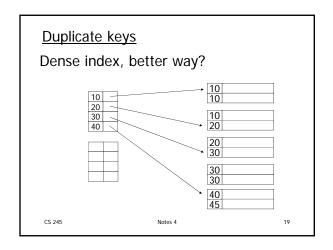
CS 245 Notes 4 15

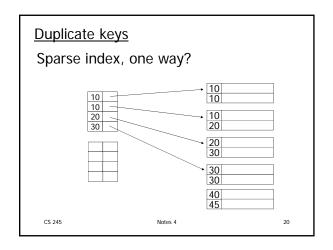
# Next:

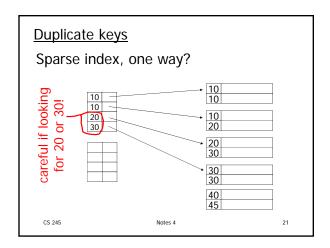
- Duplicate keys
- Deletion/Insertion
- · Secondary indexes

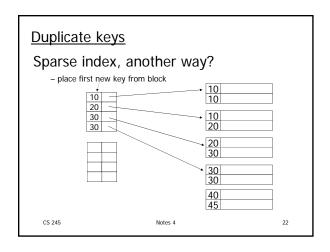


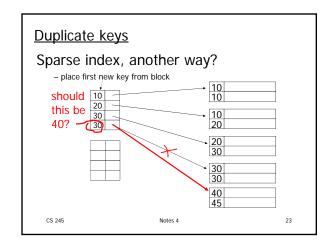


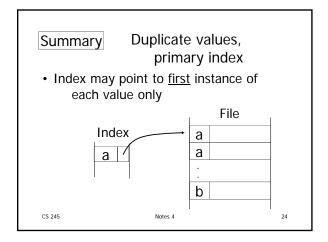


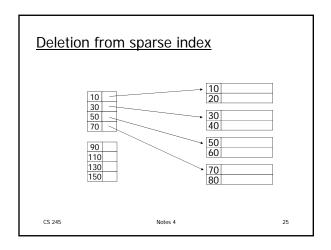


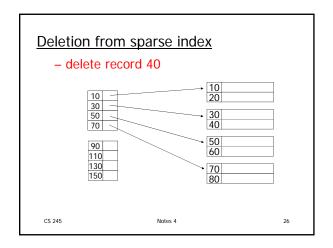


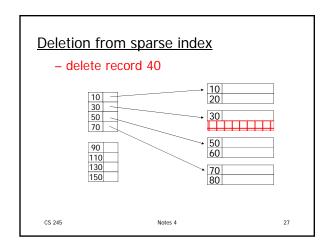


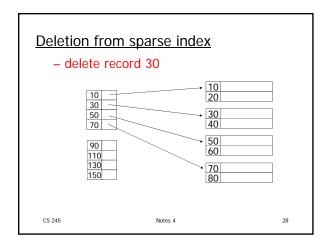


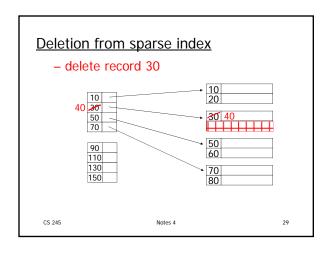


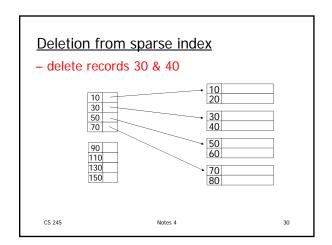


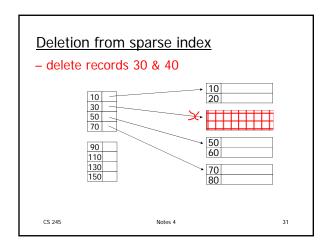


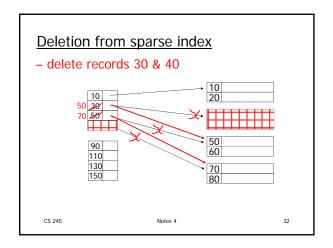


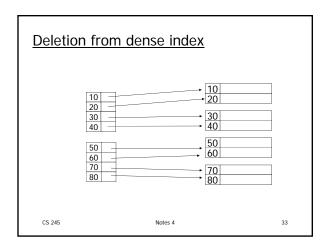


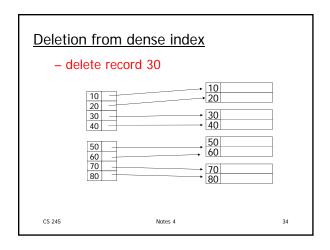


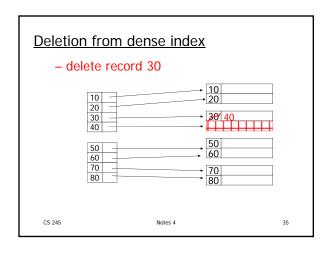


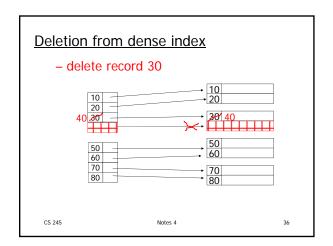


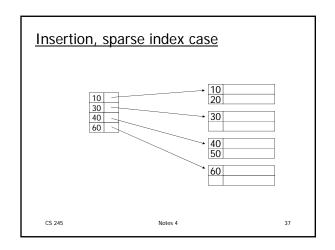


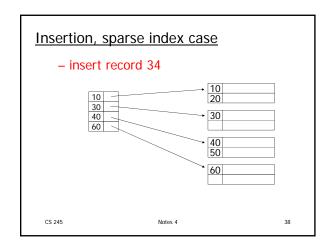


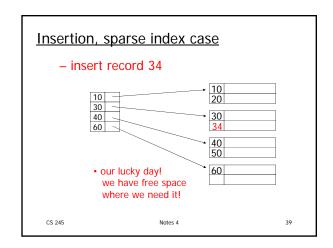


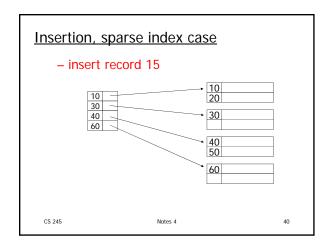


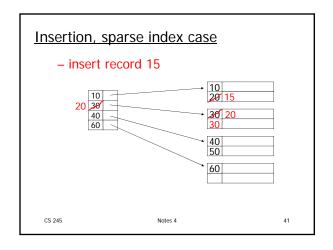


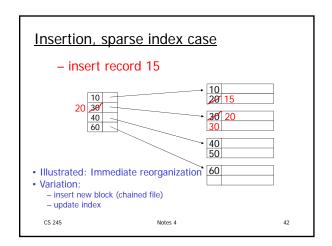


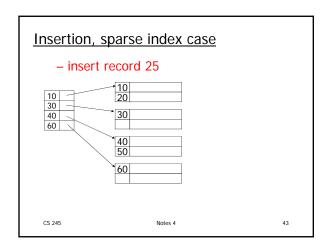


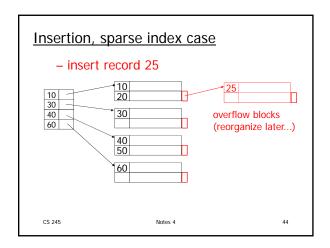






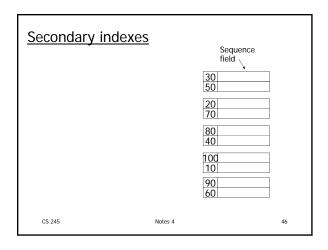


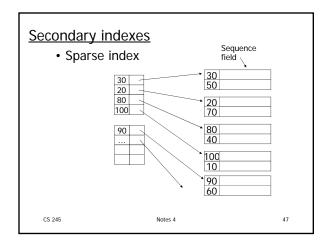


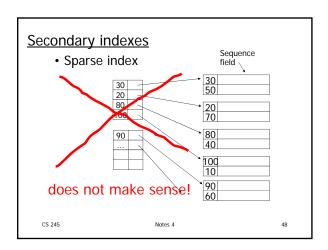


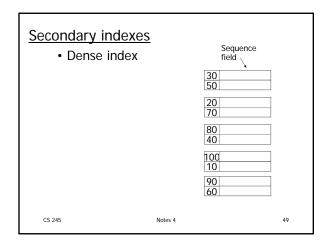
# Insertion, dense index case

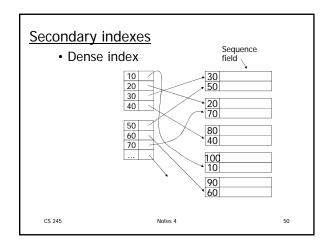
- Similar
- Often more expensive . . .

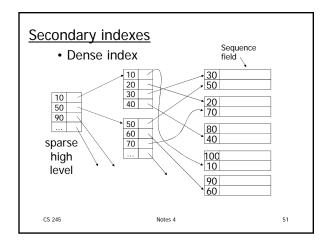


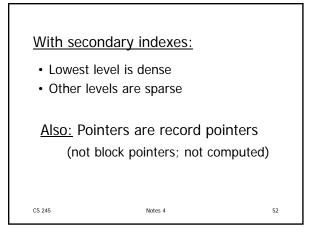


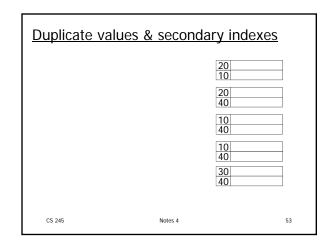


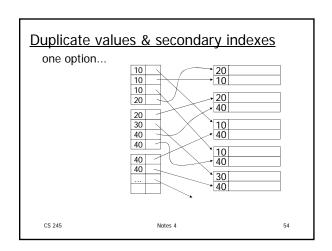


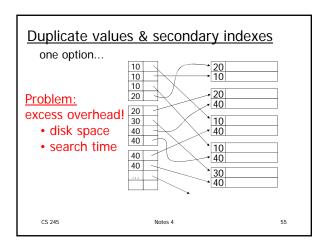


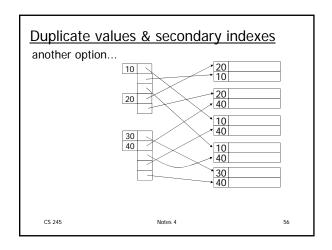


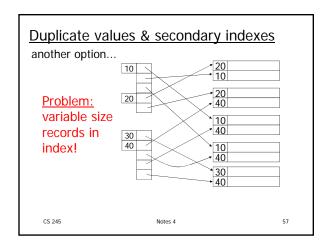


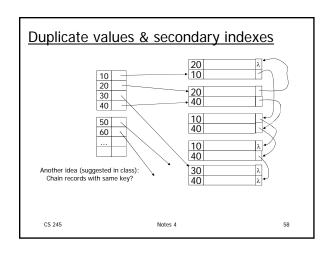


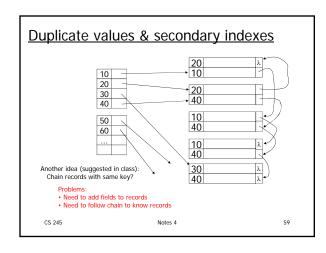


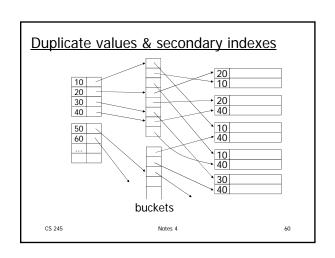


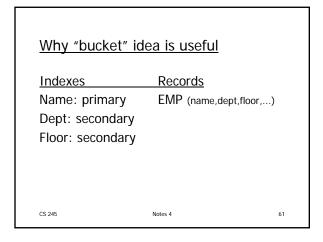


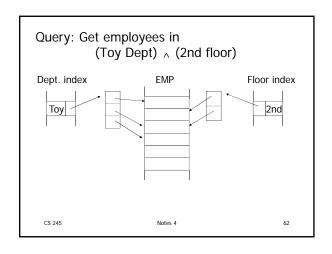


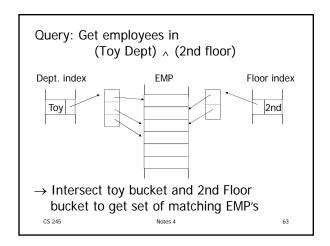


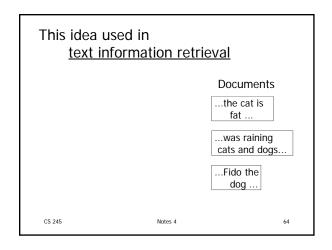


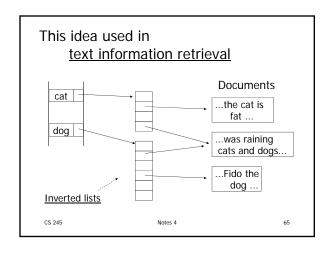










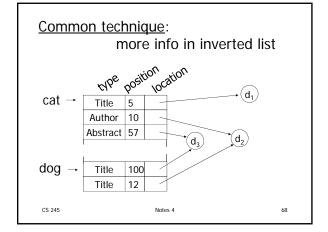


# IR QUERIES Find articles with "cat" and "dog" Find articles with "cat" or "dog" Find articles with "cat" and not "dog"

# **IR QUERIES**

- Find articles with "cat" and "dog"
- Find articles with "cat" or "dog"
- Find articles with "cat" and not "dog"
- Find articles with "cat" in title
- Find articles with "cat" and "dog" within 5 words

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Posting: an entry in inverted list.

Represents occurrence of term in article

Size of a list: 1 (in postings)

Rare words or miss-spellings

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10<sup>6</sup> Common words

Size of a posting: 10-15 bits (compressed)

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IR DISCUSSION

- Stop words
- Truncation
- Thesaurus
- Full text vs. Abstracts
- Vector model

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# Vector space model

w1 w2 w3 w4 w5 w6 w7 ...DOC = <1 0 0 1 1 0 0 ...>

Query= <0 0 1 1 0 0 0 ...>

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# Vector space model

w1 w2 w3 w4 w5 w6 w7 ...DOC = <1 0 0 1 1 0 0 ...>

Query= <0 0 1 1 0 0 0 ...>

PRODUCT = 1 + ..... = score

- Tricks to weigh scores + normalize
- e.g.: Match on common word not as useful as match on rare words...

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• How to process V.S. Queries?

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- Try Stanford Libraries
- Try Google, Yahoo, ...

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# Summary so far

- Conventional index
  - Basic Ideas: sparse, dense, multi-level...
  - Duplicate Keys
  - Deletion/Insertion
  - Secondary indexes

- Buckets of Postings List

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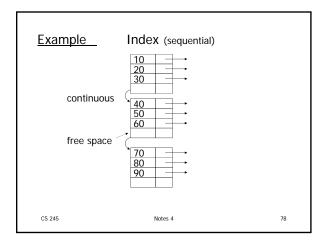
# **Conventional indexes**

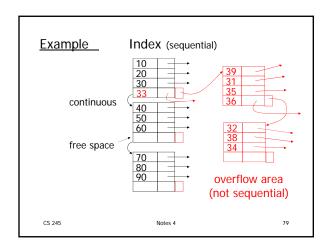
# Advantage:

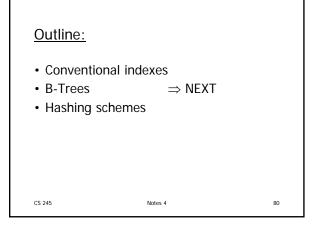
- Simple
- Index is sequential file good for scans

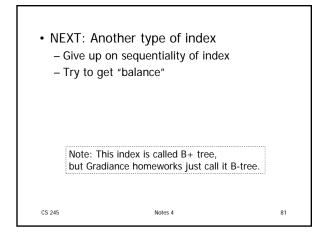
# <u>Disadvantage:</u>

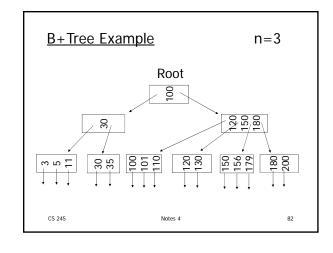
- Inserts expensive, and/or
- Lose sequentiality & balance

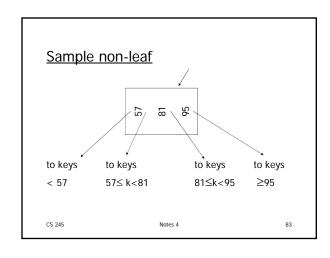


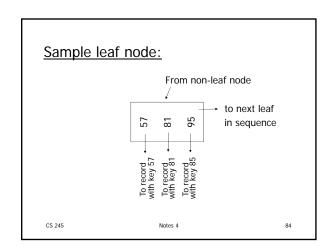


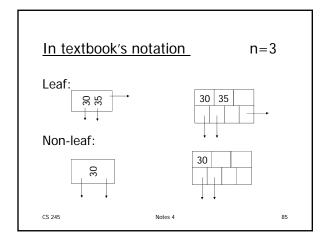


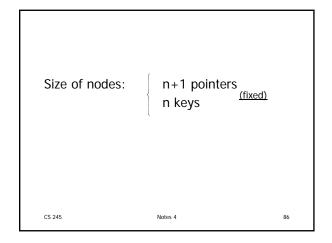












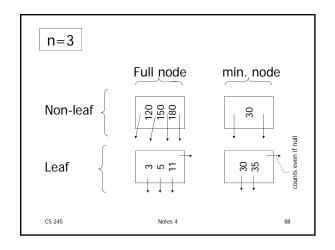
# Don't want nodes to be too empty

· Use at least

Non-leaf:  $\lceil (n+1)/2 \rceil$  pointers

Leaf:  $\lfloor (n+1)/2 \rfloor$  pointers to data

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# B+tree rules tree of order *n*

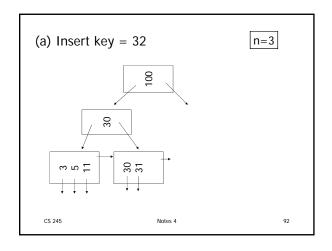
- (1) All leaves at same lowest level (balanced tree)
- (2) Pointers in leaves point to records except for "sequence pointer"

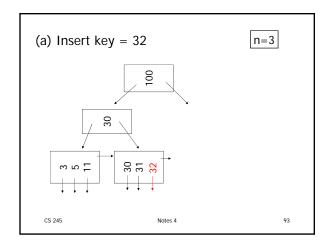
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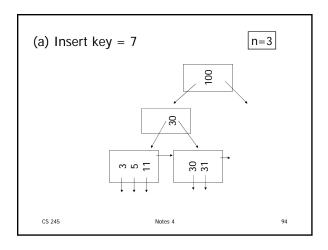
(3) Number of pointers/keys for B+tree

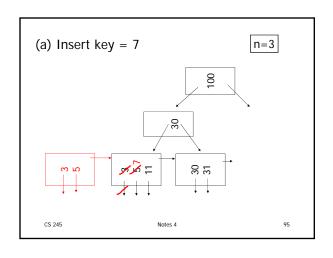
	Max ptrs	Max keys	Min ptrs→data	Min keys
Non-leaf (non-root)	n+1	n	「(n+1)/2	[(n+1)/2]- 1
Leaf (non-root)	n+1	n	[(n+1)/2]	[(n+1)/2]
Root	n+1	n	1	1

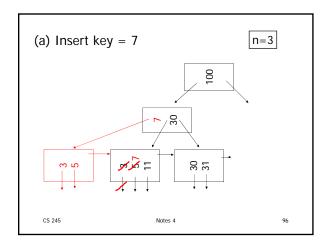
# Insert into B+tree (a) simple case - space available in leaf (b) leaf overflow (c) non-leaf overflow (d) new root

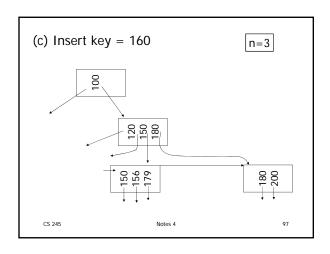


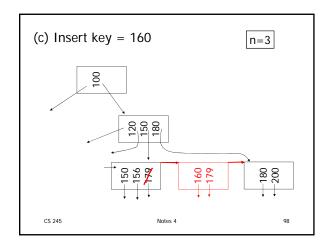


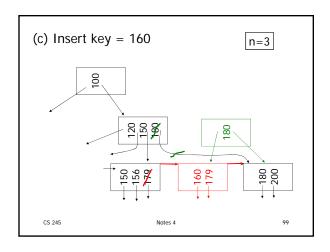


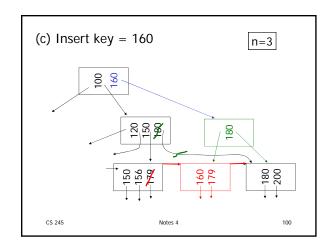


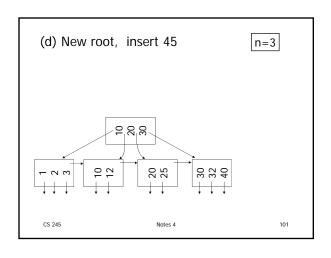


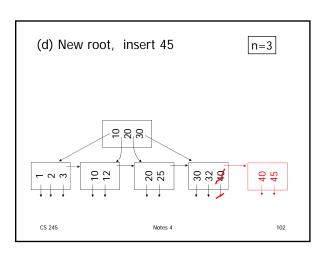


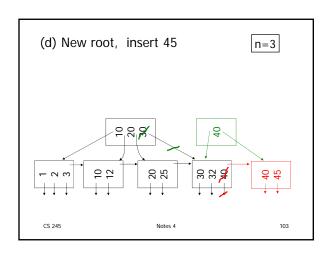


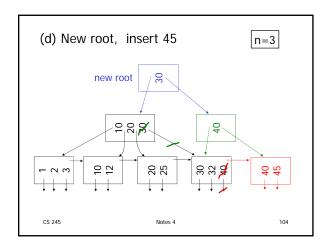




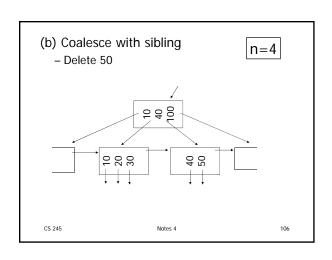


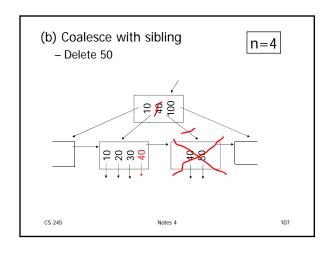


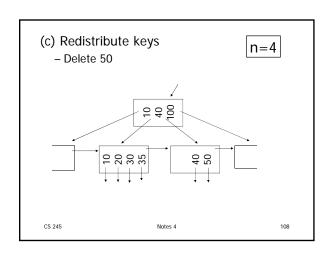


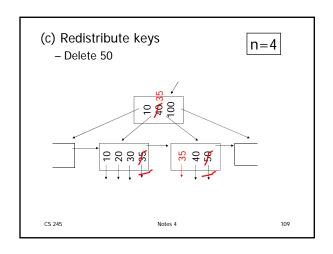


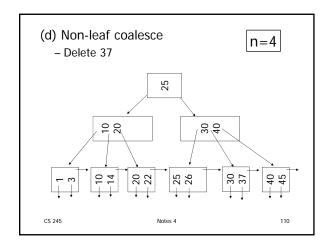
# Deletion from B+tree (a) Simple case - no example (b) Coalesce with neighbor (sibling) (c) Re-distribute keys (d) Cases (b) or (c) at non-leaf

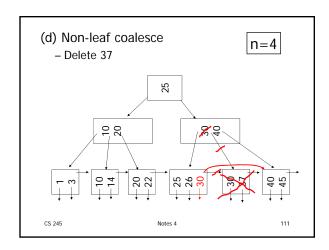


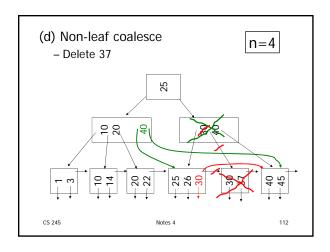


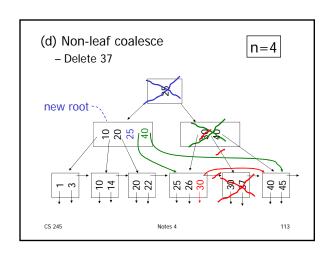


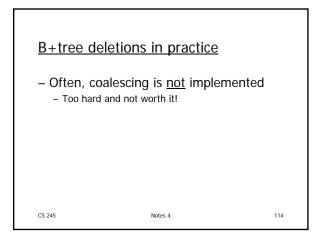












Comparison: B-trees vs. static

indexed sequential file

Ref #1: Held & Stonebraker

"B-Trees Re-examined" CACM, Feb. 1978

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## Ref # 1 claims:

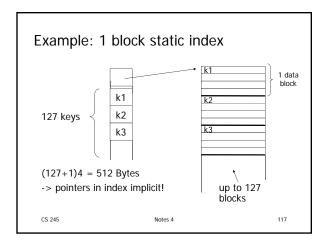
- \_- Concurrency control harder in B-Trees
  - B-tree consumes more space

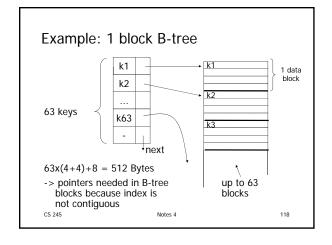
For their comparison:

block = 512 byteskey = pointer = 4 bytes 4 data records per block

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Static Ir	<u>ndex</u>	B-tree	
# data blocks	height	# data blocks	height
2 -> 127	2	2 -> 63	2
128 -> 16,129	3	64 -> 3968	3
16,130 -> 2,048,3	83 4	3969 -> 250,047	4
		250,048 -> 15,752	,961 5
CS 245		ntes 4	1

# Ref. #1 analysis claims

- For an 8,000 block file, after 32,000 inserts after 16,000 lookups
- ⇒ Static index saves enough accesses to allow for reorganization

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# Ref. #1 analysis claims

- For an 8,000 block file, after 32,000 inserts after 16,000 lookups
- ⇒ Static index saves enough accesses to allow for reorganization

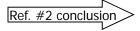
Ref. #1 conclusion Static index better!!

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Ref #2: M. Stonebraker,

"Retrospection on a database system," TODS, June 1980

Ref. #2 conclusion B-trees better!!



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B-trees better!!

- DBA does not know when to reorganize
- DBA does not know <u>how full</u> to load pages of new index

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Ref. #2 conclusion

B-trees better!!

- Buffering
  - B-tree: has fixed buffer requirements
  - Static index: must read several overflow blocks to be efficient (large & variable size buffers needed for this)

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Speaking of buffering...
 Is LRU a good policy for B+tree buffers?

13 Erro a good policy for Brities barrers.

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- Speaking of buffering...
   Is LRU a good policy for B+tree buffers?
- → Of course not!
- → Should try to keep root in memory at all times

(and perhaps some nodes from second level)

# **Interesting problem:**

For B+tree, how large should *n* be?



n is number of keys / node

127

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# Sample assumptions:

(1) Time to read node from disk is (S+Tn) msec.

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# Sample assumptions:

- (1) Time to read node from disk is (S+Tn) msec.
- (2) Once block in memory, use binary search to locate key:  $(a + b LOG_2 n)$  msec.

For some constants a,b: Assume a << S

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Sample assumptions:

- (1) Time to read node from disk is (S+Tn) msec.
- (2) Once block in memory, use binary search to locate key:  $(a + b LOG_2 n)$  msec.

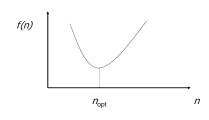
For some constants  $a_i b_i$ : Assume a << S

(3) Assume B+tree is full, i.e., # nodes to examine is  $LOG_n N$ where N = # records

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# 

f(n) = time to find a record



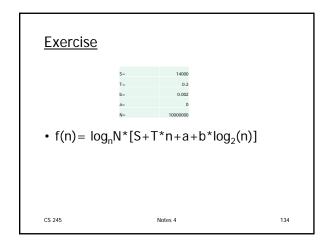
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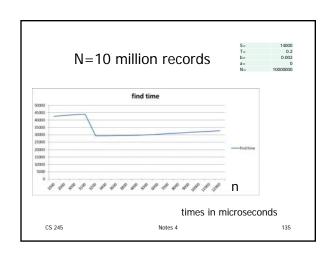
Answer is  $n_{opt} = "few hundred"$ (see homework for details)

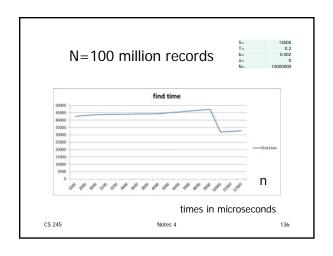
CS 245

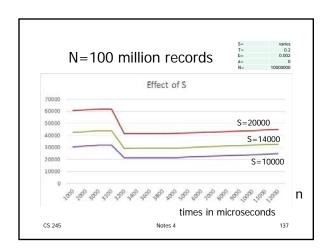
➡ FIND n<sub>opt</sub> by f'(n) = 0
 Answer is n<sub>opt</sub> = "few hundred" (see homework for details)
 ➡ What happens to n<sub>opt</sub> as

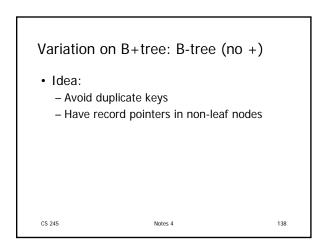
 Disk gets faster?
 CPU get faster?

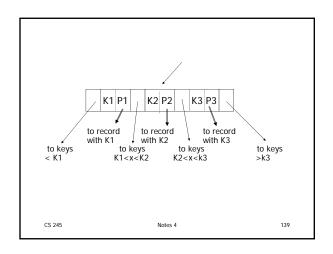


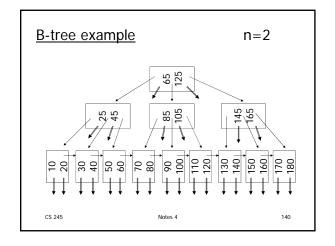


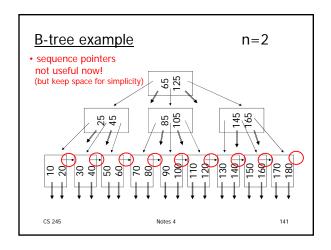


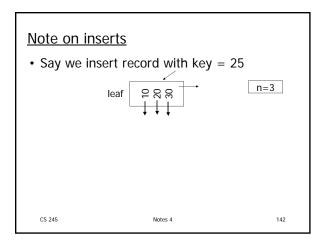


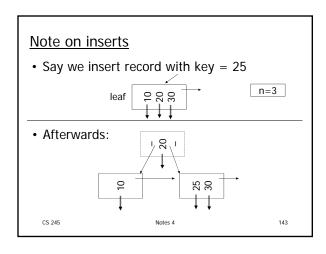


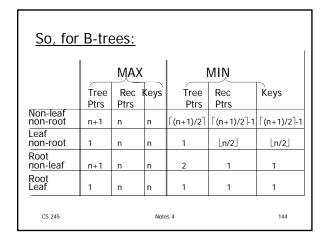












# **Tradeoffs:**

- © B-trees have faster lookup than B+trees
- ☼ in B-tree, non-leaf & leaf different sizes
- ☼ in B-tree, deletion more complicated

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# **Tradeoffs:**

- © B-trees have faster lookup than B+trees
- ☺ in B-tree, non-leaf & leaf different sizes
- ☺ in B-tree, deletion more complicated
  - → B+trees preferred!

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## But note:

If blocks are fixed size
 (due to disk and buffering restrictions)

 Then lookup for B+tree is

actually better!!

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# Example:

\_- Pointers 4 bytes - Keys 4 bytes

- Blocks 100 bytes (just example)

- Look at full 2 level tree

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## B-tree:

Root has 8 keys + 8 record pointers + 9 son pointers = 8x4 + 8x4 + 9x4 = 100 bytes

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# B-tree:

Root has 8 keys + 8 record pointers + 9 son pointers = 8x4 + 8x4 + 9x4 = 100 bytes

Each of 9 sons: 12 rec. pointers (+12 keys) = 12x(4+4) + 4 = 100 bytes

# B-tree:

Root has 8 keys + 8 record pointers  
+ 9 son pointers  
= 
$$8x4 + 8x4 + 9x4 = 100$$
 bytes

Each of 9 sons: 12 rec. pointers (+12 keys)  
= 
$$12x(4+4) + 4 = 100$$
 bytes

$$\underline{\text{2-level B-tree, Max # records}} = 12x9 + 8 = 116$$

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Root has 12 keys + 13 son pointers  
= 
$$12x4 + 13x4 = 100$$
 bytes

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# B+tree:

Root has 12 keys + 13 son pointers  
= 
$$12x4 + 13x4 = 100$$
 bytes

Each of 13 sons: 12 rec. ptrs (+12 keys) = 12x(4 + 4) + 4 = 100 bytes

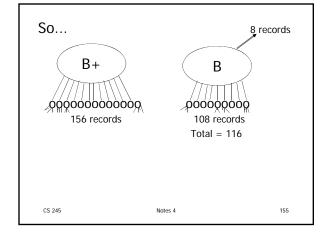
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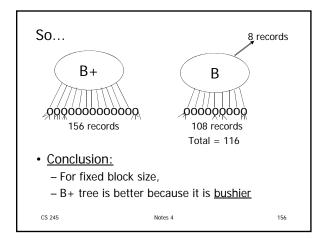
# B+tree:

Root has 12 keys + 13 son pointers  
= 
$$12x4 + 13x4 = 100$$
 bytes

Each of 13 sons: 12 rec. ptrs (+12 keys)  
= 
$$12x(4 + 4) + 4 = 100$$
 bytes

# <u>2-level B+tree, Max # records</u> = 13x12 = 156





# An Interesting Problem...

- What is a good index structure when:
  - records tend to be inserted with keys that are larger than existing values?
     (e.g., banking records with growing data/time)
  - we want to remove older data

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# One Solution: Multiple Indexes

• Example: I1, I2

day	days indexed	days indexed	
	l1	12	
10	1,2,3,4,5	6,7,8,9,10	
11	11,2,3,4,5	6,7,8,9,10	
12	11,12,3,4,5	6,7,8,9,10	
13	11,12,13,4,5	6,7,8,9,10	

•advantage: deletions/insertions from smaller index

disadvantage: query multiple indexes

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# Another Solution (Wave Indexes)

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day	I1	12	13	14
10	1,2,3	4,5,6	7,8,9	10
11	1,2,3	4,5,6	7,8,9	10,11
12	1,2,3	4,5,6	7,8,9	10,11, 12
13	13	4,5,6	7,8,9	10,11, 12
14	13,14	4,5,6	7,8,9	10,11, 12
15	13,14,15	4,5,6	7,8,9	10,11, 12
16	13,14,15	16	7,8,9	10,11, 12

advantage: no deletions

disadvantage: approximate windows

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# Outline/summary

- Conventional Indexes
  - · Sparse vs. dense
  - · Primary vs. secondary
- B trees
  - B+trees vs. B-trees
  - B+trees vs. indexed sequential
- Hashing schemes --> Next